# LINEAR COMBINATIONS OF $q$-STARLIKE FUNCTIONS OF ORDER ALPHA 

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#### Abstract

In this paper, we introduced a new concept of bounded radius rotation to define the class of $q$-starlike functions of order $\alpha$ using the $q$-derivative, some geometric properties of linear combination of such functions are studied.

Keywords: $q$-derivative, $q$-starlike functions, convex functions, linear combination, bounded radius rotation.

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## 1. Introduction

Let $\mathcal{A}$ denote the class of functions of form

$$
\begin{equation*}
f(z)=z+\sum_{n=2}^{\infty} a_{n} z^{n} \tag{1}
\end{equation*}
$$

which are analytic in the open unit disk

$$
\mathcal{U}=\{z: z \in \mathbb{C} \text { and }|z|<1\}
$$

and $\mathcal{S}$ denote the subclass of $\mathcal{A}$ consisting of all function which are univalent in $\mathcal{U}$. Jackson[5] initiated $q$-calculus and developed the concept of the $q$-integral and $q$-derivative. For a function $f \in \mathcal{S}$ given by (1) and $0<q<1$, the $q$-derivative of $f$ is defined by

$$
\partial_{q} f(z)= \begin{cases}\frac{f(z)-f(q z)}{z(1-q)}, & z \neq 0  \tag{2}\\ f^{\prime}(0), & z=0\end{cases}
$$

Equivalently (2), may be written as

$$
\partial_{q} f(z)=1+\sum_{n=2}^{\infty}[n]_{q} a_{n} z^{n-1}, \quad z \neq 0
$$

where

$$
[n]_{q}=\frac{1-q^{n}}{1-q}
$$

[^0]Note that as $q \rightarrow 1,[n]_{q} \rightarrow n$.
Now, recall the definition of the class of $q$-starlike functions of order $\alpha, 0 \leq \alpha<1$, denoted by $S_{q}^{*}(\alpha)$.

Definition 1.1. [2] A function $f \in \mathcal{A}$ is said to belong to the class $S_{q}^{*}(\alpha)$ if

$$
\begin{equation*}
\left|\frac{\frac{z \partial_{q} f(z)}{f(z)}-\alpha}{1-\alpha}-\frac{1}{1-q}\right| \leq \frac{1}{1-q}, z \in \mathcal{U} \tag{3}
\end{equation*}
$$

where $\partial_{q} f(z)$ is defined by (2) and $0<q<1$.
The following is the equivalent form of Definition 1.1

$$
\begin{equation*}
f \in S_{q}^{*}(\alpha) \Longleftrightarrow\left|\frac{z \partial_{q} f(z)}{f(z)}-\frac{1-\alpha q}{1-q}\right| \leq \frac{1-\alpha}{1-q} \tag{4}
\end{equation*}
$$

We note that as $q \rightarrow 1^{-}$the closed disc $\left|\omega-(1-q)^{-1}\right| \leq(1-q)^{-1}$ becomes the right-half plane and the class $S_{q}^{*}(\alpha)$ reduces to $S^{*}(\alpha)$, the subclass of $\mathcal{A}$ consisting of functions which are starlike of order $\alpha(0<\alpha<1)$ in $\mathcal{U}$. In particular, when $\alpha=0$, the class $S_{q}^{*}(\alpha)$ coincides with the class $S_{q}^{*}:=S_{q}^{*}(0)$, which was first introduced by Ismail et al [4] in 1990 and later it has been considered in $[1,8,10,6,7]$.
Observe that (3) holds if and only if

$$
\begin{equation*}
\frac{z \partial_{q} f(z)}{f(z)} \prec \frac{1+(1-2 \alpha) z}{1-q z} \tag{5}
\end{equation*}
$$

where $\prec$ denotes subordination.
Using the definition of the class of $S_{q}^{*}(\alpha)$ and (5) it can be seen that linear transformation $\frac{1+(1-2 \alpha) z}{1-q z}$ maps $|z|=r$ onto the circle with center $C(r)=\frac{1+(1-2 \alpha) q r}{1-q^{2} r^{2}}$ and the radius $\rho(r)=\frac{(1-\alpha)(1+q) r}{1-q^{2} r^{2}}$.
Thus using subordination principle, we can write

$$
\begin{equation*}
\left|\frac{z \partial_{q} f(z)}{f(z)}-\frac{1+(1-2 \alpha) q r^{2}}{1-q^{2} r^{2}}\right| \leq \frac{(1-\alpha)(1+q) r}{1-q^{2} r^{2}} \tag{6}
\end{equation*}
$$

Definition 1.2. Let $p(z)$ be analytic in $\mathcal{U}$ with $p(0)=0$. Then $p \in P_{m}(q, \alpha)$ if and only if,

$$
P(z)=\left(\frac{m}{4}+\frac{1}{2}\right) p_{1}(z)-\left(\frac{m}{4}-\frac{1}{2}\right) p_{2}(z)
$$

where $p_{j}(z) \prec \frac{1+(1-2 \alpha) z}{1-q z}, j=1,2,0<q<1, m \geq 2$.
For $m=2$ and $\alpha=0, P_{2}(q)=P(q)$ consists all functions subordinate to $\frac{1+z}{1-q z}, z \in \mathcal{U}$. Also $\lim _{q \rightarrow 1^{-}} P(q)=P$, the class of functions with positive real part.

Definition 1.3. Let $f \in \mathcal{A}$. Then $f \in R_{q}^{*}(m, \alpha)$, if and only if, $\frac{z \partial_{q} f(z)}{f(z)} \in P_{m}(q, \alpha), z \in \mathcal{U}$.
$f$ in this case, is called a function of $q$-bounded radius rotation.
Observe that $R_{q}^{*}(2,0)=S_{q}^{*}$ and as $q \rightarrow 1^{-}, \alpha=0, R_{q}^{*}(m, \alpha)=R_{m}$, the class of functions with bounded radius rotation.

## 2. Main Results

We need the following lemmas, to prove our main results.
Lemma 2.1. Let $f \in R_{q}^{*}(m, \alpha)$. Then for $m \geq 2,0<q<1$

$$
\begin{equation*}
\left|\frac{z \partial_{q} f(z)}{f(z)}-\frac{1+(1-2 \alpha) q r^{2}}{1-q^{2} r^{2}}\right| \leq \frac{\frac{m}{2}(1-\alpha)(1+q) r}{1-q^{2} r^{2}} \tag{7}
\end{equation*}
$$

Lemma 2.2. If $|u-a| \leq d$ and $|v-a| \leq d$ where $a$ and $d$ are real and $a>d \geq 0$, and

$$
\omega=u \frac{1}{1+A e^{i \beta}}+v \frac{1}{1+A^{-1} e^{-i \beta}}
$$

where $A$ is real and $A>0$ and $\beta \in[0, \beta)$, then

$$
\mathcal{R}(\omega) \geq a-d \sec \left(\frac{\beta}{2}\right)
$$

Lemma 2.3. Let $f \in R_{q}^{*}(m, \alpha)$. Then $f \in S_{q}^{*}(\alpha)$ for $|z|<r_{q}^{*}(\alpha)$. where

$$
\begin{equation*}
r_{q}^{*}(\alpha)=\frac{4(1-2 \alpha)}{m(1+q-2 \alpha)+\sqrt{m^{2}(1+q-2 \alpha)^{2}-16(1-2 \alpha) q}} \tag{8}
\end{equation*}
$$

Proof. Since $f \in R_{q}^{*}(m, \alpha)$, we have

$$
\frac{z \partial_{q} f(z)}{f(z)}=p(z) \in P_{m}(q, \alpha)
$$

This implies that $p(z)$ can be written as

$$
P(z)=\left(\frac{m}{4}+\frac{1}{2}\right) p_{1}(z)-\left(\frac{m}{4}-\frac{1}{2}\right) p_{2}(z)
$$

where $p_{j}(z) \prec \frac{1+(1-2 \alpha) z}{1-q z}, j=1,2,0<q<1, m \geq 2$.
Therefore
$\mathcal{R}\left(\frac{z \partial_{q} f(z)}{f(z)}\right)=\mathcal{R}(p(z)) \geq\left(\frac{m}{4}+\frac{1}{2}\right)\left(\frac{1+(1-2 \alpha) r}{1-q r}\right)-\left(\frac{m}{4}-\frac{1}{2}\right)\left(\frac{1-(1-2 \alpha) r}{1+q r}\right)$

$$
=\frac{1+\frac{m}{2}(1+q-2 \alpha) r+(1-2 \alpha) q r^{2}}{1-q^{2} r^{2}}
$$

and from this, it follows that $\mathcal{R}\left(\frac{z \partial_{q} f(z)}{f(z)}\right) \geq 0$ for $|z|<r_{q}^{*}(\alpha)$. where $r_{q}^{*}(\alpha)$ is given by (8).
Observe that as $\alpha=0, f \in R_{q}^{*}(m)$ and in this case $\mathcal{R}\left(\frac{z \partial_{q} f(z)}{f(z)}\right)>0$ for $|z|<r_{q}^{*}$, where $r_{q}^{*}=\frac{4}{m(1+q)+\sqrt{m^{2}(1+q)^{2}-16 q}}$, see [7] and as $q \rightarrow 1^{-}, \alpha=0, f \in R_{m}$ and in this case $\mathcal{R}\left(\frac{z f^{\prime}(z)}{f(z)}\right)>0$ for $|z|<r^{*}=\frac{2}{m+\sqrt{m^{2}-4}}$, see [3].
Lemma 2.4. Let $f \in R_{q}^{*}(m, \alpha)$. Then
$|\arg f(z)| \leq \frac{m}{2}(1-\alpha)(1+q) \sin ^{-1} r$ and $\left|\arg f^{\prime}(z)\right| \leq m(1-\alpha)(1+q) \sin ^{-1} r$.
Theorem 2.1. Let $f_{1}, f_{2} \in R_{q}^{*}(m, \alpha)$ and let

$$
\begin{equation*}
F(z)=\lambda f_{1}(z)+(1-\lambda) f_{2}(z) \tag{9}
\end{equation*}
$$

where $0 \leq \mu=\arg \frac{\lambda}{1-\lambda}<\pi$. Then $F \in S_{q}^{*}(\alpha)$ in $|z|<r_{q, m}(\alpha)$ where $r_{q, m}(\alpha)$ is the smallest positive value of $r$ satisfying the equation
$g(r)=\left[1+(1-2 \alpha) q r^{2}\right] \cos \left(\frac{\mu}{2}+\frac{m}{2}(1-\alpha)(1+q) \sin ^{-1} r\right)-\frac{m}{2}(1-\alpha)(1+q) r \sin ^{-1} r=0$.

Proof. Using $q$-difference operator of (15), we obtained
$\partial_{q} F(z)=\lambda \partial_{q} f_{1}(z)+(1-\lambda) \partial_{q} f_{2}(z)$,
and therefore
$\frac{\partial_{q} F(z)}{F(z)}=\frac{\lambda \partial_{q} f_{1}(z)+(1-\lambda) \partial_{q} f_{2}(z)}{\lambda f_{1}(z)+(1-\lambda) f_{2}(z)}$

$$
\begin{equation*}
=\frac{z \partial_{q} f_{1}(z)}{f_{1}(z)}\left[1+\left(\frac{\lambda}{1-\lambda} \cdot \frac{f_{1}(z)}{f_{2}(z)}\right)^{-1}\right]^{-1}+\frac{z \partial_{q} f_{2}(z)}{f_{2}(z)}\left[1+\left(\frac{\lambda}{1-\lambda} \cdot \frac{f_{1}(z)}{f_{2}(z)}\right)\right]^{-1} . \tag{10}
\end{equation*}
$$

Put

$$
\begin{equation*}
u=\frac{z \partial_{q} f_{2}(z)}{f_{2}(z)}, v=\frac{z \partial_{q} f_{1}(z)}{f_{1}(z)}, A=\left|\frac{\lambda}{1-\lambda} \cdot \frac{f_{1}(z)}{f_{2}(z)}\right| \tag{11}
\end{equation*}
$$

From (10) and (17), we obtained

$$
\begin{equation*}
\omega(z)=\frac{\partial_{q} F(z)}{F(z)}=u \frac{1}{1+A e^{i \beta}}+v \frac{1}{1+A^{-1} e^{-i \beta}} . \tag{12}
\end{equation*}
$$

Using Lemma 2.1 and Lemma 2.2, we obtained

$$
\begin{equation*}
\mathcal{R}\left\{\frac{\partial_{q} F(z)}{F(z)}\right\} \geq \frac{1+(1-2 \alpha) q r^{2}}{1-q^{2} r^{2}}-\frac{\frac{m}{2}(1-\alpha)(1+q) r}{1-q^{2} r^{2}} \sec \left(\frac{\beta}{2}\right) \tag{13}
\end{equation*}
$$

where
$\beta=\arg \left(\frac{\lambda}{1-\lambda} \cdot \frac{f_{1}(z)}{f_{2}(z)}\right)=2 n \pi+\mu+\arg f_{1}(z)-\arg f_{2}(z)$.
Now by Lemma 15,
$|\beta| \leq \mu+m(1-2 \alpha)(1+q) \sin ^{-1} r$,
and this gives us $\sec \left(\frac{\beta}{2}\right) \leq \frac{1}{\cos \left(\frac{\mu}{2}+\frac{m}{2}(1-\alpha)(1+q) \sin ^{-1} r\right)}$.
Therefore
$\mathcal{R}\left\{\frac{\partial_{q} F(z)}{F(z)}\right\} \geq 0$, if

$$
g(r)=\left[1+(1-2 \alpha) q r^{2}\right] \cos \left(\frac{\mu}{2}+\frac{m}{2}(1-\alpha)(1+q) \sin ^{-1} r\right)-\frac{m}{2}(1-\alpha)(1+q) r>0
$$

We note that
$g(r)=\cos \left(\frac{\mu}{2}\right)$, for $r=0$, and
$g(r)=-\frac{m}{2}(1-\alpha)(1+q) \sin \left(\frac{\pi-\mu}{m(1-\alpha)(1+q)}\right)<0$, when $r=\sin \left(\frac{\pi-\mu}{m(1-\alpha)(1+q)}\right)$.
This implies that $g(r)=0$ has a root in the interval $\left(0, \sin \left(\frac{\pi-\mu}{m(1-\alpha)(1+q)}\right)\right)$ and right hand side of (13) is positive in the disc $|z|<r_{q, m}(\alpha)$, where $r_{q, m}(\alpha)$ is the least positive value of $r$ satisfying $g(r)=0$.

As $\alpha=0$, we have the following result, proved by Noor et al [6].
Corollary 2.1. Let $f_{1}, f_{2} \in R_{q}^{*}(m)$ and let

$$
\begin{equation*}
F(z)=\lambda f_{1}(z)+(1-\lambda) f_{2}(z) \tag{14}
\end{equation*}
$$

where $0 \leq \mu=\arg \frac{\lambda}{1-\lambda}<\pi$. Then $F \in S_{q}^{*}$ in $|z|<r_{q, m}$ where $r_{q, m}$ is the smallest positive value of $r$ satisfying the equation

$$
g(r)=\left[1+q r^{2}\right] \cos \left(\frac{\mu}{2}+\frac{m}{2}(1+q) \sin ^{-1} r\right)-\frac{m}{2}(1+q) r=0 .
$$

As $q \rightarrow 1^{-}$and for $\alpha=0$, we get the following result, introduced by Noor et al [6].

Corollary 2.2. Let $f_{1}, f_{2} \in R(m)$ and let

$$
\begin{equation*}
F(z)=\lambda f_{1}(z)+(1-\lambda) f_{2}(z), \tag{15}
\end{equation*}
$$

where $0 \leq \mu=\arg \frac{\lambda}{1-\lambda}<\pi$. Then $F \in S^{*}$ in $|z|<r_{m}^{*}$ where $r_{m}^{*}$ is the smallest positive value of $r$ satisfying the equation $g_{m}(r)=B\left(1+r^{2}\right)-m r=0, B=\cos \left(\frac{\mu}{2}+m \sin ^{-1} r\right)$.
This gives us $r_{m}^{*}=\frac{m+\sqrt{m^{2}-4 B^{2}}}{2 B}$. As a special case of Corollary 2.2, we take $m=2$. Therefore $B=B_{2}=\cos \left(\frac{\mu}{2}+2 \sin ^{-1} r\right)$, and $\lim _{q \rightarrow 1^{-}} R_{q}^{*}(2)=S^{*}$.
From these observations, we deduce the radius of starlikeness of linear combination of two starlike functions is given by $r_{2}^{*}=\frac{1-\sqrt{1-B_{2}^{2}}}{B^{2}}$.
Corollary 2.3. As $\alpha=0$, and $m=2$. Then, in Theorem 2.1, $f_{1}, f_{2} \in S_{q}^{*}$ and it follows that

$$
\mathcal{R}\left\{\frac{\partial_{q} F(z)}{F(z)}\right\} \geq 0 \text { in }|z|<r_{q}^{*} .
$$

where $r_{q}^{*}$ is the least positive root of
$g_{q}(r)=D_{1} q r 2-(1+q) r+D_{1}=0$, where $D_{1}=\cos \left(\frac{\mu}{2}+(1+q) \sin ^{-1} r\right)$.
and hence $r_{q}^{*}=\frac{(1+q)-\sqrt{(1+q)^{2}-4 q D_{1}^{2}}}{2 q D_{1}}$.
Theorem 2.2. Let $f_{1}, f_{2} \in \bigcap_{0<q<1} S_{q}^{*}(\alpha)$ and let

$$
\begin{equation*}
F(z)=\lambda f_{1}(z)+(1-\lambda) f_{2}(z) \tag{16}
\end{equation*}
$$

where $0 \leq \mu=\arg \frac{\lambda}{1-\lambda}<\pi$. Then $F$ maps the disc $|z|<r_{\mu}$ onto a convex domain, where $r_{\mu}$ is the least positive value of $r$ that satisfies the equation
$g_{\mu}(r)=D r^{2}-2 r_{1} r+D r_{1}^{2}$, where $r_{1}=\frac{2-\sqrt{3+\alpha^{2}}}{1+\alpha}, D=\cos \left(\frac{\mu}{2}+2(1-\alpha) \sin ^{-1}\left(\frac{r}{r_{1}}\right)\right)$.
Proof. It has been shown in [2] that

$$
\bigcap_{0<q<1} S_{q}^{*}(\alpha)=S^{*}(\alpha)
$$

It is well known [9] that $f \in S^{*}(\alpha)$ is convex of order $\alpha$ in the disc $|z|<r_{1}=\frac{2-\sqrt{3+\alpha^{2}}}{1+\alpha}$. with these facts, we proceed to find the radius of convexity for the function $F$ following the technique used in Theorem 2.1.
We can write
$1+\frac{z F^{\prime \prime}(z)}{F^{\prime}(z)}=\left[1+\frac{z f_{1}^{\prime \prime}(z)}{f_{1}^{\prime}(z)}\right]\left[1+\left(\frac{\lambda}{1-\lambda} \cdot \frac{f_{1}^{\prime}(z)}{f_{2}^{\prime}(z)}\right)^{-1}\right]^{-1}+\left[1+\frac{z f_{2}^{\prime \prime}(z)}{f_{2}^{\prime}(z)}\right]\left[1+\left(\frac{\lambda}{1-\lambda} \cdot \frac{f_{1}(z)}{f_{2}(z)}\right)\right]^{-1}$.
Put

$$
\begin{equation*}
u=\left[1+\frac{z f_{1}^{\prime \prime}(z)}{f_{1}^{\prime}(z)}\right], v=\left[1+\frac{z f_{2}^{\prime \prime}(z)}{f_{2}^{\prime}(z)}\right], A=\left|\frac{\lambda}{1-\lambda} \cdot \frac{f_{1}^{\prime}(z)}{f_{2}^{\prime}(z)}\right|, \beta=\arg \left(\frac{\lambda}{1-\lambda} \cdot \frac{f_{1}^{\prime}(z)}{f_{2}^{\prime}(z)}\right) . \tag{17}
\end{equation*}
$$

Now, for $r_{1}=\frac{2-\sqrt{3+\alpha^{2}}}{1+\alpha}$, we have

$$
\left\{\begin{array}{l}
\left|u-\frac{r_{1}^{2}+r^{2}}{r_{1}^{2}-r^{2}}\right| \leq \frac{2 r r_{1}}{r_{1}^{2}-r^{2}}, \\
\left|v-\frac{r_{1}^{2}+r^{2}}{r_{1}^{2}-r^{2}}\right| \leq \frac{2 r r_{1}}{r_{1}^{2}-r^{2}} .
\end{array}\right.
$$

Therefore

$$
\begin{equation*}
\omega(z)=1+\frac{z F^{\prime \prime}(z)}{F^{\prime}(z)}=u \frac{1}{1+A e^{i \beta}}+v \frac{1}{1+A^{-1} e^{-i \beta}} . \tag{18}
\end{equation*}
$$

where
$\beta=\arg \left(\frac{\lambda}{1-\lambda} \cdot \frac{f_{1}^{\prime}(z)}{f_{2}^{\prime}(z)}\right)=2 n \pi+\mu+\arg f_{1}^{\prime}(z)-\arg f_{2}^{\prime}(z)$, and so
$|\beta| \leq \mu+4(1-\alpha) \sin ^{-1}\left(\frac{r}{r-1}\right)$,
Therefore
$\mathcal{R}\left\{1+\frac{z F^{\prime \prime}(z)}{F^{\prime}(z)}\right\}>0$, if $T_{\mu}(r)=\left(r_{1}^{2}+r^{2}\right) \cos \left(\frac{\mu}{2}+2(1-\alpha) \sin ^{-1}\left(\frac{r}{r-1}\right)-2 r_{1} r=0\right.$, where $r_{1}=\frac{2-\sqrt{3+\alpha^{2}}}{1+\alpha}$.
That is
$T_{\mu}(r)=D r^{2}-2 r_{1} r+D r_{1}^{2}, D=\cos \left(\frac{\mu}{2}+2(1-\alpha) \sin ^{-1}\left(\frac{r}{r_{1}}\right)\right)$.
Hence

$$
\begin{equation*}
r_{\mu}=\frac{r_{1}-\sqrt{r_{1}^{2}-D^{2} r_{1}^{2}}}{D} \tag{19}
\end{equation*}
$$

Hence $F$ maps the disc $|z|<r_{\mu}$ onto a convex of order $\alpha$ domain, where $r_{\mu}$ is given by (19).

Remark As $\alpha=0$ Theorem 2.1 reduces to Theorem 2 in [6].
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