# An Integrated Topology of Hybrid Marine Farm & Wind Farm

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Abstract- Renewable energy has been playing an important role to meet power demand and 'Green Energy' market is getting bigger platform all over the world in the last few years. In order to meet the increasing demand of electricity and power, integration of renewable energy is getting highest priorities around the world. Wind is one of the most top growing renewable energy resources and it is the most environmental friendly, cost effective and safe among all renewable energy resources available. Another promising form of renewable energy is ocean energy which covers 70 % of the earth. Offshore Wind farm' (OWF) has already become very popular for large scale wind power integration with the onshore grid. Recently, marine current farm (MCF) is also showing good potential to become mainstream energy sources and already successfully commissioned in United Kingdom. An integration of wind and tidal energy represents a new-trend for large electric energy production using offshore wind generators and marine current generators, respectively. This work first focuses on the modeling of fixed speed IG based marine current farm and variable speed DFIG based wind farm. Detailed modeling and control scheme for the proposed system are demonstrated considering some realistic scenarios. The power system small signal stability analysis is also carried out by eigenvalue analysis for marine current generator topology, wind turbine generator topology and integrated topology. The relation between the modes and state variables are discussed in light of modal and sensitivity analyses. The results of theoretical analyses are verified by MATLAB/SIMULINK.

Keywords- Marine Energy; Wind Energy; Induction Machine; Stability; Eigen Value.

# 1. Introduction

In order to conserve the non-renewable energy resources as well as to reduce Carbon footprint all over the world, science and technology have led us to explore the new resources for electricity generation which is clean, safe and capable of serving the society for a long period. A wind energy system is the most environmental friendly, cost effective and safest among all renewable energy resources available [1]. It has been forecasted that the increase in electricity generation from renewable sources between 2008 and 2035 will be primarily derived from wind and hydro power, which will contribute 36% and 31% of the additional demand respectively [2]. Wind power is projected to supply 8% of global electricity in 2035 up from just 1% in 2008. In the year 2010, the wind capacity has reached 196.630GW worldwide and it will reach 240GW by the end of 2012 [3]. Ocean energy is also considered as an abundant and nonpollution energy resource [4]. Various wave and tidal projects have been established all over the world to harness the energy from the sea. In 2007, the first commercial tidal steam converter, the "SeaGen", started operation in Northern Ireland [5]. Along with the development of researches on wind power technology, the small signal stability of wind power generation is getting remarkable importance, in the recent years. Small signal stability analysis of the power system including the widely used synchronous machine is a well-developed field of study [6-8]. Effect of wind energy conversion system on small signal stability model along with conventional power system equipped with synchronous generator and power system stabilizer (PSS) is presented in [9]. The small signal dynamic models for both fixed and variable speed wind turbine generator systems are available in power system literatures [10-12]. The dynamic and

transient behavior of fixed and variable speed generator is presented in [13]. In [14], oscillatory stability and eigenvalue sensitivity of doubly fed induction generator (DFIG) based wind power generation system is presented. Dynamic behavior analysis and influence of reactive power and speed controller parameters of DFIG is discussed in [15]. Effects of damping controller on the different modes as well as super/sub synchronous modes of operation of DFIG have been investigated in [16]. However, analysis of integrated topology of wind energy generation and marine energy generation and interaction of different dynamic modes based on modal and frequency domain analyses have not been reported much. This work is intended to present a comprehensive study of small signal stability of the IG based fixed speed marine current generator as well as DFIG based variable speed wind turbine generator connected to a power grid.

### 2. Generator Marine Current System

#### 2.1. System Overview

The fixed speed marine current farm comprises a squirrel cage induction generator where the stator winding of IG is directly connected to the power grid through capacitor bank and double-circuit transmission line.



Fig. 1. Schematic diagram of marine energy system

#### 2.2. Marine Turbine

The amount of mechanical power Pm captured from ocean can be expressed by the following equation [18].

$$P_m = \frac{1}{2} \cdot \rho_m \cdot A_m \cdot V_m^3 \cdot C_{pm}(\lambda_m, \beta_m)$$
(1)

Where  $\rho_m$  is the ocean current density [kg/m<sup>3</sup>],  $A_m$  is the area of turbine blade [m<sup>2</sup>],  $V_m$  is marine current speed [m/s],  $C_{pm}$  is the power coefficient,  $\lambda_m$  is tip speed ratio and  $\beta$  is pitch angle [degree]. Equation for  $C_{pm}$  is described as below:

$$C_{pm}(\psi_{m},\beta_{m}) = \left[ d_{1}(\frac{d_{2}}{\psi_{m}} - d_{3}\beta_{m} - d_{4}\beta_{m}^{d^{5}} - d_{6}) \right] \exp\left[ -\frac{d_{7}}{\psi_{m}} \right] \quad (2)$$

The relationship between  $\lambda$  ,  $\beta$  and  $\Psi m$  are

$$\lambda_m = \frac{R_{bm}.\omega_m}{V_m} \tag{3}$$

$$\frac{1}{\psi_m} = \frac{1}{\lambda_m + d_8\beta_m} - \frac{d_9}{\beta_m^3 + 1}$$
(4)

where  $\omega_{bm}$  is the blade angular velocity [rad/s],  $R_{bm}$  is the blade radius [m] and  $d_1$ - $d_9$  are the constant coefficient of  $C_{pm}$ . Rated speed of marine turbine is considered as 2.72 m/s.

#### 2.3. Drive Train

The Drive train modeling has been accomplished considering the inertia of generator and turbine while connecting shaft is modeled as a damper and a spring. Figure 2 shows detailed and simplified two-mass drive train models of marine turbine generator system. This study considers the simplified two-mass model which is sufficient for dynamic and transient analyses [19-20]. The two mass model can be expressed by:

$$(2H_{tm})\frac{d\omega_{tm}}{dt} = T_m - K_{sm}\theta_m - D_m(\omega_{tm} - \omega_{rm}) \quad (5)$$

$$(2H_{rm})\frac{d\omega_{rm}}{dt} = T_e + K_{sm}\theta_m + D(\omega_{tm} - \omega_{rm}) \qquad (6)$$

$$\frac{d\theta_m}{dt} = \omega_{bm}(\omega_{tm} - \omega_{rm}) \tag{7}$$

where  $\omega_{tm}$  and  $\omega_{rm}$  is the pu angular speed of the turbine and IG, respectively,  $D_m$ ,  $K_{sm}$ , and  $\theta_m$  are the mechanical damping coefficient [pu], spring constant [pu], and rotor angle [pu] difference between marine turbine and the IG [pu], respectively.  $H_{tm}$  and  $H_{rm}$  are the inertia constants (in seconds) of marine turbine and the IG, respectively.  $T_e$  and  $T_m$  are the electromagnetic and mechanical torques, respectivel.



Fig. 2. Drive train models for marine turbine:simplified twomass model

# 2.4. Drive Train

Figure 3 shows equivalent circuit of squirrel cage induction generator based on synchronously rotating reference frame. The d and q axis stator fluxes and rotor currents are chosen as state variables.



**Fig. 3.** Equivalent model of the induction generator: (a) q-axis and (b) d-axis representation.

The electrical quantities of induction machine can be expressed by the following equations: [21,22]:

$$V_{sd} = R_s I_{sd} - \omega_s \psi_{sq} + \frac{1}{\omega_b} \frac{d\psi_{sd}}{dt}$$
(8)

$$V_{sq} = R_s I_{sq} + \omega_s \psi_{sd} + \frac{1}{\omega_b} \frac{d\psi_{sq}}{dt}$$
(9)

$$V_{rd} = R_r I_{rd} - \omega_2 \psi_{rd} + \frac{1}{\omega_b} \frac{d\psi_{rd}}{dt}$$
(10)

$$V_{rq} = R_r I_{rq} + \omega_2 \psi_{rd} + \frac{1}{\omega_b} \frac{d\psi_{rq}}{dt}$$
(11)

$$\psi_s = L_s I_s + L_m I_r \tag{12}$$

$$\psi_r = L_m I_s + L_r I_r \tag{13}$$

$$T_e = \frac{L_m}{L_s} (\psi_{sq} I_{rd} - \psi_{sd} I_{rq})$$
(14)

Now, from equation (8-14), state space representation of IG can be written as a function of state variables:

$$\frac{1}{\omega_b}\frac{d\psi_{sd}}{dt} = -\frac{R_s}{L_s}\psi_{sd} + \frac{R_sL_m}{L_m}I_{rd} + \omega_s\psi_{sq} + V_{sd}$$
(15)

$$\frac{1}{\omega_b}\frac{d\psi_{sq}}{dt} = -\frac{R_s}{L_s}\psi_{sq} + \frac{R_sL_m}{L_m}I_{rq} - \omega_s\psi_{sd} + V_{sq}(16)$$

$$\frac{L'_r}{\omega_b}\frac{dI_{rd}}{dt} = -R'_r I_{rd} + \frac{R_s L_m}{L_s^2} \psi_{sd} - \frac{L_m}{L_s} \omega_r \psi_{sq} + L'_r \omega_2 I_{rq} - \frac{L_m}{L_s} V_{sd} \quad (17)$$

$$\frac{L'_r}{\omega_b}\frac{dI_{rq}}{dt} = -R'_r I_{rq} + \frac{R_s L_m}{L_s^2} \psi_{sq} + \frac{L_m}{L_s} \omega_r \psi_{sd} - L'_r \omega_2 I_{rd} - \frac{L_m}{L_s} V_{sq} \quad (18)$$

where  $V_s$  and  $V_r$  are stator and rotor pu voltage,  $L_m$  is the pu mutual inductance,  $L_s$  and  $L_r$  are stator and rotor pu self inductance,  $R_s$  and  $R_r$  are stator and rotor pu resistance,  $\Psi_s$  and  $\Psi_r$  are stator and rotor pu flux,  $\omega_s, \, \omega_r, \, \omega_2$  are synchronous angular frequency, rotor angular frequency, and rotor slip frequency (all in pu),  $\omega_b$  is the base angular frequency [377 rad/sec] and  $T_e$  is pu electromagnetic torque.

### 2.5. Transmission Line and Capacitor Bank

A capacitor bank is connected at terminal of induction generator at rated condition which can be expressed by the following state equation in terms of capacitor voltage.

$$C\frac{dV_{sd}}{dt} = \left(-\frac{1}{L_s}\psi_{sd} + \frac{L_m}{L_s}I_{rd} + I_{dt} + C\omega_s V_{sq}\right)\omega_b \quad (19)$$

$$C\frac{dV_{sq}}{dt} = \left(-\frac{1}{L_s}\psi_{sq} + \frac{L_m}{L_s}I_{rq} + I_{qt} - C\omega_s V_{sd}\right)\omega_b \qquad (20)$$

where C is the capacitance bank value,  $I_{dt}$  and  $I_{qt}$  are the pu daxis and q-axis transmission line current, respectively. The dq axis current equations for the equivalent transmission line can be expressed by the following state equation:

$$L_t \frac{dI_{dt}}{dt} = (-V_{sd} - R_i I_{dt} + L_t \omega_s I_{qt} + V_{gd})\omega_b$$
(21)

$$L_t \frac{dI_{qt}}{dt} = (-V_{sq} - R_i I_{qt} - L_t \omega_s I_{dt} + V_{gq})\omega_b$$
(22)

where  $R_t$  and  $L_t$  are equivalent resistance and inductance of the transmission line, respectively and  $V_{gd}$  and  $V_{qd}$  are the d-axis and q-axis pu grid voltages, respectively, all in pu.

#### 3. Generator Marine Current System

#### 3.1. System Overview

The wind turbine generator system comprises a doubly fed induction generator which connected to power grid through the transmission line which may include the impedance of transformer and connection cable. The schematic diagram of DFIG connected with power grid is present in Fig. 4. The DFIG based wind power system is modeled using  $5^{\text{th}}$  order machine model in which stator and rotor dynamics are considered.



Fig. 4. Schematic diagram of the variable speed wind turbine generator system

#### 3.2. Wind Turbine, Drive Train and MPPT

The electrical The wind turbine system comprises a prime mover, a shaft and a gearbox unit. The dynamic interaction involving forces from the wind and the responses of wind turbine determines the amount of kinetic energy that can be extracted. The amount of mechanical power  $P_w$  extracted from wind can be expressed by the following equation [23].

$$P_{w} = \frac{1}{2} \cdot \rho_{w} \cdot A_{w} \cdot V_{w}^{3} \cdot C_{pw}(\lambda_{w}, \beta_{w})$$
(23)

where  $\rho_w$  is the air density [kg/m<sup>3</sup>],  $A_w$  is the area of turbine blade [m<sup>2</sup>],  $V_w$  is the wind velocity [m/s],  $C_{pw}$  is the power coefficient,  $\lambda_w$  is the tip speed ratio and  $\beta_w$  is the pitch angle [degree]. The power coefficient  $C_{pw}$  is given by [24]

$$C_{pw}(\lambda_{w},\beta_{w}) = 0.5(\Gamma - 0.02\beta^{2} - 5.6)\exp[-0.17\Gamma] \qquad (24)$$

The tip speed ratio, is defined as

$$\lambda_m = \frac{R_{bw}.\omega_w}{V_w} \tag{25}$$

$$\Gamma = \frac{R.(3600)}{\lambda_w} \tag{26}$$

The turbine torque coefficient  $C_{tw}$  is related with turbine power coefficient  $C_{pw}$  by the equation:

$$C_{tw}(\lambda) = \frac{C_{pw}}{\lambda}$$
(27)

$$T_{mw} = \frac{1}{2} . \rho_w . A_w . R_{bw}^3 V_w^2 . C_{tw}(\lambda)$$
(28)

where  $R_{bw}$  is the blade radius [m],  $\omega_w$  is the rotational speed [rad/s] and  $T_{mw}$  is the wind turbine output torque [Nm].)

Equation 29 and 31 are used to calculate the reference of the active power output and the optimum rotor speed are given in equation 29 and MPPT control block is showed in Figure 6.

$$P_{ref1} = 0.1571 V_w - 1.035[pu]$$
(29)

$$P_{ref2} = 0.214771 V_w - 1.668[pu]$$
(30)

$$\omega_{opt} = 0.0775 [pu] \tag{31}$$

The two mass model can be expressed by:

$$(2H_{tw})\frac{d\omega_{tw}}{dt} = T_m - K_{sw}\theta_w - D_w(\omega_{tw} - \omega_{rw}) \quad (32)$$

$$(2H_{rw})\frac{d\omega_{rw}}{dt} = T_e + K_{sw}\theta_w + D_w(\omega_{tw} - \omega_{rw}) \quad (33)$$

$$\frac{d\theta_{w}}{dt} = \omega_{bw}(\omega_{tw} - \omega_{rw}) \tag{34}$$

where  $\omega_{tw}$  and  $\omega_{rw}$  is the pu angular speed of the turbine and IG, respectively,  $D_w, K_{sw,}$  and  $\theta_w$  are the mechanical damping coefficient [pu], spring constant [pu], and rotor angle [pu]difference between marine turbine and the IG [pu], respectively.  $H_{tw}$  and  $H_{rw}$  are the inertia constants (in seconds) of marine turbine and the IG, respectively.  $T_e$  and  $T_m$  are the electromagnetic and mechanical torques, respectively.

#### 3.3. Doubly Fed Induction Generator

According to stator flux orientation  $\Psi_s = \Psi_{sd}$  and  $\Psi_{sq} = 0$  [31]. Stator side of DFIG is presented with the help of rotor current, stator flux and stator voltage. Rotor current and stator flux variables can be used to build the state equations of stator model.

$$\frac{1}{\omega_b}\frac{d\psi_{sd}}{dt} = -\frac{R_s}{L_s}\psi_{sd} + \frac{R_sL_m}{L_s}I_{rd} + V_s\cos\gamma$$
(43)

$$\frac{d\gamma}{dt} = \omega_b(\omega_s - \omega) \tag{44}$$

where  $\omega_s$  is synchronous frequency and  $\omega$  is speed of the dq reference frame, all in pu.  $\gamma$  is denoted as the angle difference between the stator side voltage angle and stator flux angle with respect to stationary reference frame and V<sub>s</sub> is the stator voltage [pu].stator and rotor voltages are depicted in terms of same reference frame.

$$V_r = R_r I_r + \frac{1}{\omega_h} \frac{d\psi_r}{dt} + j(\omega_s - \omega_r)\psi_r$$
(45)

$$V_s = R_s I_s + \frac{1}{\omega_b} \frac{d\psi_{sd}}{dt} + j\omega_s \psi_s$$
(46)

Substituting equation (45) into (46) and including the transient terms of stator flux, the following equation can be obtained

$$\frac{1}{\omega_b}\frac{d\psi_s}{dt} = V_s - \frac{R_s}{L_s}\psi_s + \frac{R_sL_m}{L_s}I_r - j\omega_s\psi_s$$
(47)

$$V_r = R_r I_r + \frac{L_r}{\omega_b} \sigma_r \frac{dI_r}{dt} + \frac{L_m}{L_s} \frac{d\psi_s}{dt} + j\omega_2 \sigma L_r I_r + j\omega_2 \frac{L_m}{L_s} \psi_s \quad (48)$$

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Fig. 5. d-axis rotor current controller



Fig. 6. q-axis rotor current controller

Substituting equation (47) into equation (48),

$$V_r = R'_r I_r + \frac{L_r}{\omega_b} \sigma_r \frac{dI_r}{dt} + j\omega_2 \sigma L_r I_r + \frac{L_m}{L_s} (V_s - \frac{R_s}{L_s} \psi_s + j\omega_r \psi_s) \quad (49)$$

Rotor voltage equations are rewritten in terms of d-q reference frame in the following equations

$$V_{rd} = R'_r I_{rd} + \frac{L_r}{\omega_b} \sigma_r \frac{dI_{rd}}{dt} + j\omega_2 \sigma L_r I_{rd} + E_d$$
(50)

$$V_{rq} = R'_r I_{rq} + \frac{L_r}{\omega_b} \sigma_r \frac{dI_{rq}}{dt} + j\omega_2 \sigma L_r I_{rq} + E_q$$
(51)

where  $E_d$  and  $E_q$  are called rotor back EMF

$$E_{d} = \frac{L_{m}}{L_{s}} (V_{sd} - \frac{R_{s}}{L_{s}} \psi_{sd} + j\omega_{r} \psi_{sd})$$
(52)

$$E_q = \frac{L_m}{L_s} (V_{sq} - \frac{R_s}{L_s} \psi_{sq} + j\omega_r \psi_{sq})$$
(53)

 $E_d$  and  $E_q$  represent effect of stator dynamic in rotor current dynamics. It is possible to decouple the cross coupling between the d and q axis components of the rotor current  $-j\omega_2\sigma L_r I_{rd}$  and  $j\omega_2\sigma L_r I_{rq}$  with the use of rotor current controller [32]. Moreover, a feed forward compensating term is included in the control law that will compensate the tracking error caused by back EMF. Thus the rotor voltage can be stated as:

$$V_{rd} = K_{pid} \cdot e_{rd} + K_{iid} \cdot \int e_{rd} dt + j\omega_2 \sigma L_r I_{rd} + K_E \cdot E_d$$
(54)

$$V_{rq} = K_{pid} \cdot e_{rq} + K_{iid} \cdot \int e_{rq} dt + j\omega_2 \sigma L_r I_{rq} + K_E \cdot E_q (55)$$

where  $e_{rd} = I_{rdref}$ - $I_{rd}$  and  $e_{rq} = I_{rqref}$ - $I_{rq}$  and  $K_p$  and  $K_i$  are proportional gain and integral gain. A generic control law KE is introduced to include feed forward compensation term.

$$K_E = \begin{cases} 0 & \text{Without feed forward term} \\ 1 & \text{With feed forward term} \end{cases}$$

σ

Depending on the value of KE compensation level is measured. Introducing active resistance to improve open loop bandwidth of the system, the state equation of rotor current can be stated as:

$$\frac{\sigma . L_r}{\omega_b} \frac{dI_{rd}}{dt} = -R'_r I_{rd} + K_{pid} \cdot e_{rd} + K_{iid} \cdot \int e_{rd} dt + (K_E - 1) \cdot E_d - R_a I_{rd} (56)$$
  
$$\frac{r \cdot L_r}{dt} \frac{dI_{rq}}{dt} = -R'I_r + K_{re} \cdot e_r + K_{re} \int e_r dt + (K_E - 1) \cdot E_r - R_e I_r (57)$$

 $\omega_b dt$   $r_r q$   $\mu a r q$   $\mu a$  r q  $\mu a$  r q r q r q

The third and fourth term in equation (30) and (31) can be written as:

$$\frac{dX_{5}}{dt} = K_{iid} \cdot e_{rd} = K_{iid} \cdot (I_{rdref} - I_{rd})$$
(58)

$$\frac{dX_6}{dt} = K_{iid} \cdot e_{rq} = K_{iid} \cdot (I_{rqref} - I_{rq})$$
(59)



Fig. 7. d-axis rotor current controller with active damping



Fig. 8. q-axis rotor current controller with active damping

# 3.4. Reactive Power Controller

In stator flux orientation, the reactive power and terminal voltage will be controlled by d axis component of rotor voltage and current [33].

$$\alpha_{pf} = \frac{L_m}{L_s} . K_{p-pf} . . \alpha_d . V_s \tag{60}$$

$$K_{i\_pf} = .K_{p\_pf} ..\alpha_d.$$
(61)

where is the  $\alpha_{\text{pf}}$  bandwidth of reactive power control loop and is  $\alpha_d$  the closed loop bandwidth of d axis rotor current.

Now, the equation for d axis reference current for reactive power controller is stated as:

$$I_{rdref} = -K_{pq} \cdot (Q_{ref} - Q) - \int K_{iq} \cdot (Q_{rref} - Q)$$
(62)

$$\frac{dX_8}{dt} = K_{iq} \cdot (Q_{ref} - Q)$$
(63)

where  $Q_{ref}$  is the reference reactive power,  $K_{pq}$  is proportional reactive power gain, and K<sub>iq</sub> is the integral reactive power gain.

### 3.5. Speed Controller

In stator flux orientation, the speed will be controlled by q axis component of rotor voltage and current [34].

$$\frac{K_{i\omega}}{K_{p\omega}} = \frac{D}{2H_r}.$$
(64)

$$\alpha_{\omega} = \frac{L_m}{L_s} \cdot \psi_{so} \cdot \frac{K_{p\omega}}{2H_r}$$
(65)

where  $\alpha_{\omega}$  is the bandwidth of speed control loop and is  $\alpha_{\alpha}$  the closed loop bandwidth of q axis rotor current.

The equation for q axis reference current is stated as:

$$I_{rqref} = -K_{p\omega} \cdot (\omega_{rref} - \omega_r) - \int K_{i\omega} \cdot (\omega_{rref} - \omega_r) + D_a \omega_r$$
(66)

$$\frac{dX_{\gamma}}{dt} = K_{i\omega}.(\omega_{rref} - \omega_r)$$
(67)

#### Dynamic Analysis of Wind and marine Farm 4.

The For fixed tidal speed operation, Squirrel Cage induction generator (SCIG) is considered and dynamic behaviour of this system is simulated using MATLAB/SIMULINK.The parameters chosen for SCIG system are rotor speed, stator voltage, turbine speed and electrical torque.



For variable wind speed operation, Doubly Fed induction generator (DFIG) is considered and dynamic behaviour of this simulated system is using MATLAB/SIMULINK.The parameters chosen for DFIG system are rotor speed, turbine speed, electrical torque and daxis flux.



# 5. Integrated Topology

The This section presents the proposed small scale model of integrated OWF and MCF which is connected with the existing grid in the mainland or isolated island using high voltage cable. Total capacities of OWF and MCF are considered as 6 and 4 MVA, respectively. OWF is composed of 4 DFIGs of 1.5 MVA each. On the other hand, 4 IGs of MCF are rated at 1 MVA each.



Fig. 16. Integrated topology combining marine current generator and wind turbine generator system

In this scheme, offshore wind and marine current generation units are connected with each other using undersea cable. From the point of connection (PCC) power is transmitted to the grid through offshore step up transformer and high voltage transmission line. The distance between adjacent DFIG and IG of the integrated wind and marine current farm is kept 150 m and distance from PCC and the grid is chosen as 15 km.

# 5.1. Modal Analysis

In The modal analysis is performed on the hybrid system consisting marine current generator and wind turbine generator. The studied system is linearized around a nominal operating point. Eigenvalues of the studied system are listed in Table 1.

Table 1. Eigenvalue of the integrated system

| No.            | Eigenvalue      | Modes                       |
|----------------|-----------------|-----------------------------|
| $\lambda_1$    | -14.0 + j3906.4 | IG electrical mode          |
| $\lambda_2$    | -14.0 + j3906.4 | IG electrical mode          |
| $\lambda_3$    | -13.1+ j3151.1  | IG electrical mode          |
| $\lambda_4$    | -13.1+ j3151.1  | IG electrical mode          |
| $\lambda_5$    | -376.7          | DFIG rotor current mode     |
| $\lambda_6$    | -373.4          | DFIG rotor current mode     |
| $\lambda_7$    | -5.3+ j373.6    | DFIG stator mode            |
| $\lambda_8$    | -5.3- j373.6    | DFIG stator mode            |
| λ9             | -15.5+j376.9    | IG stator mode              |
| $\lambda_{10}$ | -15.5-j376.9    | IG stator mode              |
| $\lambda_{11}$ | -1.8+j24.2      | IG electromechanical mode   |
| $\lambda_{12}$ | -1.8-j24.2      | IG electromechanical mode   |
| $\lambda_{13}$ | -1.6+j13.2      | DFIG electromechanical mode |
| $\lambda_{14}$ | -1.6-j13.2      | DFIG electromechanical mode |
| $\lambda_{15}$ | -13.5           | DFIG rotor electrical mode  |
| $\lambda_{16}$ | -13.4           | DFIG rotor electrical mode  |
| $\lambda_{17}$ | -3.8            | DFIG real mode              |
| $\lambda_{18}$ | -4.5            | IG monotonic mode           |
| $\lambda_{19}$ | -0.5-j4.1       | IG mechanical mode          |
| $\lambda_{20}$ | -0.5-j4.1       | IG mechanical mode          |
| $\lambda_{21}$ | -0.5            | DFIG weak mechanical mode   |
| $\lambda_{22}$ | -0.01           | DFIG weak mechanical mode   |

# 6. Conclusion

The In this paper small signal analysis modelof hybrid topology consisting of fixed speed marine current generator system and variable speed wind turbine generator has been reported. A detailed small signal stability analysis model has been developed for the grid connected fixed speed MTGS which includes two-mass drive train, induction generator, capacitor bank, transmission line. Also a detailed small signal stability model of VSWT including two mass drive train, rotor current controller, speed controller, reactive power controller has been designed. Eventually the main feature of this study is to study small signal analysis of this integrated topology. In the proposed hybrid topology both fixed and variable speed generators are considered where the primary focus was to reduce the investment cost. The modal analysis of the integrated farm is investigated as well as different modes are defined for the integrated topology. A salient co-operate control strategy can also be implemented to stabilize a small scale hybrid power system composed of offshore wind farm and marine current farm during grid fault condition.

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