

Modeling Stand Volume using Landsat TM data for Fir stands (*Abies bornmuelleriana* Matth.) Located in Buyukduz Planning Unit, TURKEY

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Abstract

Remotely sensed data in the form of satellite images have been used for decades to estimate forest parameters in support of forest management planning (Leyk et al., 2002). Since satellite data can be repeatedly acquired with reliable data quality, methods about modeling some stand attributes with data-originated satellite images is appropriate for obtaining information on land cover on forest areas (Wulder and Seemann, 2003). Based on 97 sample plots, it is aiming to model relationships between stand volume and band values based on Landsat TM data for fir stands (*Abies bornmuelleriana* Matth.) located in Buyukduz Planning Unit, TURKEY. Multiple linear regression models were used to predict stand volumes with band values, including TM 1 - TM 5 and TM 7, originated from Landsat TM satellite image. The regression models, including different independent variables alternatives and band values, were compared with some information criteria, e.g. the adjusted coefficient of determination (R^2), with Reduced Akaike's Information Criterion (*AIC*), Sawa's Bayesian Information Criteria (*BIC*), Schwarz Bayesian Criteria (*SBC*), the root mean square error (*RMSE*) and Mallow's C_p , which criteria are measures of goodness of fit for regression models. These statistical analyses were performed by PROC REG and PROC RSQUARE procedures of the SAS/ETS V9 software (SAS Institute Inc, 2004). The best results for predictive performance were obtained by multiple linear regression model including TM 2 and TM 4 as independent variables. This model, statistically significant at 95% level with model parameters, explained 54.09% of the observed stand volume variability with 634.29 of *AIC*, 637.02 of *BIC*, 640.36 of *SBC*, 28.69 of *RMSE* and -0.315 of C_p . The results showed that the Landsat TM data are beneficial to estimate forest stand volume. Thus, forest managers could use remote sensing data, e.g. Landsat TM data, for predicting stand volume and for generating maps necessary for developing forest management plans.

Keywords: Landsat TM satellite image, Multiple regression analysis, Stand volume, *Abies*

Introduction

The estimations of forest stand parameters such as stand volume, basal area, tree density, dominant height and stand diameter are important for forest management planning, and required for effective and successive resource management. Furthermore, estimating changes in forest stand parameters through time is a keystone knowledge for many forest requests, such as decision-making (Zimble et al., 2003), forest planning and management (Sironen et al., 2001).

Sustainable management and utilization of forest resources need accurate information about forest extension and spatial distribution of stand parameters such as volume and tree density. In addition, as forests undertake change it becomes imperative that inventory data be reorganized periodically (Dodge and Bryant, 1976; Sivanpillai et al., 2006). Traditionally, these forest stand parameters

such as stand volume, basal area and tree density data have been collected through national forest inventories, inspections, terrestrial surveys of sample plots and by extrapolating from prior inventories.

Forest national inventories can be carried out at various levels and scales from regional to national or for a small area unit (Chapman et al., 2006). In recent times, remote sensing data have been used to predict forest stand parameters for supporting forest management planning (Leyk et al., 2002). Since remote sensing data can be repeatedly attained with reliable data quality, this method is suitable for obtaining information for land cover on forest areas (Wulder and Seemann, 2003). Since the per-unit area cost is much cheaper, capacity of satellite remote sensing for large-area coverage is another advantage (Malingreau et al., 1992).

Forest resource observing with Landsat satellite images and other moderate

resolution satellite image is an important module for a wide range of forest applications. The attractiveness of Landsat satellite images data can be qualified to several basic characteristics of the Landsat program, including low imagery costs and free data distribution facility widespread use of a spatial resolution enough to characterize typical forest cover dynamics related to forest management (Cohen and Goward, 2004).

The objective of this paper is to investigate and model the relationships between reflectance values recorded by Landsat TM satellite image and stand volume obtained from sample plots, using multiple linear regression analysis for fir stands (*Abies bornmuelleriana* Matth.) located in Buyukduz Planning Unit, TURKEY.

Material and Methods

Study Area

The study area is Buyukduz planning unit located in Karabuk city in the northwestern part of Turkey (45°51'08" E, 45°68'23" N, UTM ED 50 datum Zone 36N) (Figure 1).

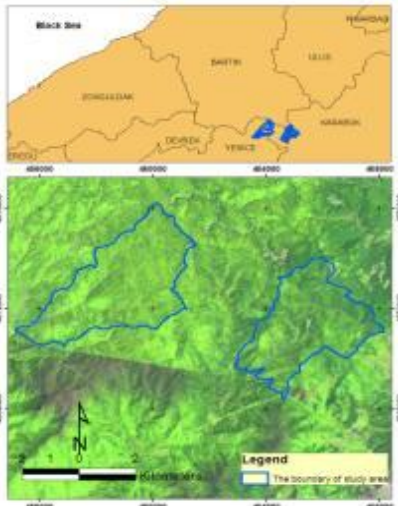


Figure 1. The geographical location of the study area

The study area covers 3020.0 ha. The elevation ranges from 800 to 1,736 m with an average of 1,270 m. The study area has an average slope of 45%. The mean annual temperature is 12.0 °C and the mean rainfall is 650 mm (Anonymous, 2010). The study

area is covered with fir (*Abies bornmuelleriana* Matth.), Scots pine (*Pinus sylvestris* L.), anatolian black pine (*Pinus nigra* Arn. ssp. *pallasiana* (Lamb.) Holmboe), oriental beech (*Fagus orientalis*) and Çoruh oak (*Quercus petraea* ssp. *iberica* (Steven ex Bieb.) Krassilin).

Material

The data used in this paper are forest cover type map at 1/25.000 scale for year 2010, 97 sample plots obtained from data base of forest management planning and Landsat TM satellite image acquired on September 3, 2010. In these ground measurements, the forest inventory plots were distributed by 300x300 m grids. The size of sample plots ranged from 400 m² to 800 m² depending on stand crown closures. In each sample plots, diameter at breast height (dbh) was measured to the nearest 0.1 cm with calipers for every living tree with dbh>8.0 cm. The classical inventory calculations were performed from each sample plot and the tree volume was calculated using local tree volume formulas, single or two-entry volume equations (Forest Plans, Forest agency of Turkey, 2000).

Methods

Data processing, interpreting and analysis were performed using Erdas Imagine 9.1TM version (Erdas, 2002). The Landsat TM data was acquired for September 3, 2010, orthorectified, and geo-referenced using 1/25.000 scale Topographical Maps with UTM projection (ED 50 DATUM, Zone 36) using first order nearest neighbor rules. A total of 20 ground points were used to register the TM image subset a rectification error less than 1 pixel image. Solar zenith angle and atmosphere influence spectral value of satellite image. Thus, radiometric correction must be done to convert digital number to reflectance value. In the process of radiometric correction, the digital number of Landsat TM must be converted to radiance value, and then to reflectance. The information for the coming radiometric correction (solar zenith angle, acquisition date and so on) can be obtained from Landsat TM ancillary data.

Statistical Analysis

The reflectance value of pixels within a 1x1 pixel window (similar to the plot size) was extracted from all Landsat TM bands. To examine and model the relationships between Landsat TM satellite image based on the spectral reflectance values, TM 1-5 and 7, and stand volume values, the multiple linear regression analysis was used in this study. In this study, the following linear relationship was assumed:

$$V = \beta_0 + \beta_1 \cdot X_1 + \beta_2 \cdot X_2 + \dots + \beta_n \cdot X_n + \varepsilon \quad (1)$$

where V is the stand parameter, stand volume, X_1, \dots, X_n are variable vectors corresponding to remote sensing data, e.g. the spectral reflectance factors, TM 1-5 and 7, β_1, \dots, β_n represent model coefficients and ε is the additive error term (Corona et al., 1998; Fontes et al., 2003). The estimate of each parameter for variables of these regression models should be statistically significant at 95% probability level. The null hypothesis $H_0 = \beta_0 = \beta_1 = \dots = \beta_n = 0$, was tested and parameters that were not significantly different from zero were rejected (Fontes et al., 2003). The regression models, including different independent variables alternatives and band values, were compared with some information criteria, e.g. the adjusted coefficient of determination (R^2), the Reduced Akaike's Information Criterion (AIC), Sawa's Bayesian Information Criteria (BIC), Schwarz Bayesian Criteria (SBC), the root mean square error (RMSE) and Mallows' Cp, which criteria are measures of goodness of fit for regression models. Beal (2007) defined and coded these criteria for selecting best subset of independent variables to model stand volume in SAS statistical program.

The adjusted coefficient of determination R^2 is the percentage of the variability of the dependent variable that is explained by the variation of the independent variables after accounting for the intercept and number of independent variables (Beal, 2007). Therefore, the adjusted R^2 value ranges from 0 to 1 and is a function of the sum of squares error and total, number of observations n ,

number of independent variables. The equation for the adjusted R^2 is shown as follow:

$$R^2_{adj} = 1 - \frac{(n-1) \cdot SSE}{(n-k) \cdot SST} \quad (2)$$

Akaike (1973) introduced the concept of information criteria as a tool for optimal model selection (Beal, 2007). Other authors using AIC for model selection include Akaike (1987) and Bozdogan (1987, 2000). Akaike's Information Criteria (AIC) is a function of the number of observations n , the SSE, the number of independent variables and looks as follows:

$$AIC = n \cdot \ln\left(\frac{SSE}{n}\right) + 2k \quad (3)$$

The first term in Eqn. is a measure of the model lack of fit while the second term ($2k$) is a penalty term for additional parameters in the model. Therefore, as the number of independent variables k included in the model increases, the lack of fit term decreases while the penalty term increases (Beal, 2007).

Sawa (1978) developed a model selection criterion that was derived from a Bayesian modification of the AIC criterion (Beal, 2007). Bayesian Information Criteria (BIC) is a function of the number of observations n , the SSE, the pure error variance fitting the full model (s^2), and the number of independent variables $k \leq p + 1$ where k includes the intercept. It looks as follows:

$$BIC = n \cdot \ln\left(\frac{SSE}{n}\right) + \frac{2(k+2) \cdot n \cdot \sigma^2}{SSE} - \frac{2 \cdot n^2 \cdot \sigma^4}{SSE^2} \quad (4)$$

The penalty term for BIC is more complex than the AIC penalty term and is a function of n , the SSE and s^2 in addition to k .

Schwarz (1978) developed a model selection criterion that was derived from a Bayesian modification of the AIC criterion (Beal, 2007). Schwarz Bayesian Criteria (SBC) is a function of the number of observations n , the SSE, and the number of independent variables $k \leq p + 1$ where k includes the intercept. It is as follows:

$$SBC = n \cdot \ln\left(\frac{SSE}{n}\right) + k \cdot \ln(n)$$

(5)

The penalty term for SBC is similar to AIC in Equation but uses a multiplier of $\ln n$ for k instead of a constant 2 by incorporating the sample size n .

The RMSE is a function of the sum of squared errors (SSE), number of observations n , and the number of independent variables $k = p + 1$ where k includes the intercept. It looks as follows:

$$RMSE = \sqrt{\frac{SSE}{n - k}} \quad (6)$$

The RMSE is calculated for all possible subset models. Using this technique, the model with the smallest RMSE is declared the best linear model. This approach does include the number of parameters in the model. Additional parameters will decrease the numerator since the SSE decreases as additional variables are included in the model and the denominator decreases as k increases.

Mallows' Cp (Mallows, 1973) is another model diagnostic that is a function of the SSE, the full model pure error estimate s^2 , number of observations n , and the number of independent variables $k \leq p + 1$ where k includes the intercept (Beal, 2007). Mallows' Cp is as follows:

$$Cp = \frac{SSE}{\sigma^2} + 2k - n \quad (7)$$

Mallows' Cp is calculated for all possible subset models (Beal, 2007). Using this technique, the model with the smallest Cp is declared the best linear model. As the number of independent variables k increases, an increased penalty term ($2k$) is offset with a decreased SSE (Beal, 2007).

In these criteria, the more adjusted coefficient of determination (R^2) means

better predictive performance for model, and the less other criteria eventuated in the superior model prediction results. All these statistical analyses were performed by PROC REG and PROC RSQUARE procedures of the SAS/ETS V9 software (SAS Institute Inc, 2004).

Results

Table 1 presents the information criteria, including the adjusted coefficient of determination (R^2), with Reduced Akaike's Information Criterion (AIC), Sawa's Bayesian Information Criteria (BIC), Schwarz Bayesian Criteria (SBC), the root mean square error (RMSE) and Mallow's Cp, for all possible independent variables, the spectral reflectance factors, TM 1-5 and 7, to model stand volume. The best results for predictive performance were obtained by multiple linear regression model including TM 2 and TM 4 as independent variables. In these selected regression models for stand volume, the F statistics and coefficients were significant at a probability level of 95 percent (Fvalue=33.40, $p < 0.05$). The standard error, t values and the predicted values of model's parameters were presented for the selected best regression sub-group models including TM 2 and TM 4 independent variables in Table 2. This model statistically significant at 95% levels with model parameters explained 54.09 % of the observed stand volume variability with 634.29 of AIC, 637.02 of BIC, 640.36 of SBC, 28.69 of RMSE and -0.315 of Cp.

To further evaluate the quality of the model fit and the parameter estimates, we used the standardized predicted (fitted) values versus standardized observed stand volume values given in Fig. 1. The model values indicate that there are no observable patterns in Fig. 1, and thus there are no serious violations of the assumption of constant variance, such as homoscedasticity.

Table 1. The information criteria for all possible independent variables, the spectral reflectance factors, TM 1-5 and 7, to model stand volume

Model Group	R ² adj.	Cp	AIC	BIC	RMSE	SBC	Independent Variables						
1	0.1808	38.3275	665.7609	665.9519	374.9391	669.8116	TM2						
1	0.1157	45.5014	670.0407	669.9758	389.5436	674.0914	TM3						
1	0.0461	53.1842	674.2881	673.9804	404.6002	678.3388	TM1						
1	0.024	55.6217	675.571	675.1922	409.2612	679.6217	TM4						
1	0.0047	58.7769	677.1892	676.7223	415.2172	681.2399	TM5						
1	0.0184	60.2958	677.9518	677.4439	418.0542	682.0026	TM7						
2	0.5409	-0.315	634.2876	637.0179	280.6871	640.3636	TM2	TM4					
2	0.4345	11.204	645.9641	647.4395	311.5298	652.0402	TM2	TM5					
2	0.4115	13.6866	648.1907	649.4374	317.7852	654.2668	TM2	TM7					
2	0.3118	24.4745	656.9538	657.3423	343.6477	663.0298	TM3	TM4					
2	0.2437	31.85	662.2419	662.1475	360.2624	668.318	TM3	TM5					
2	0.2061	35.9144	664.9559	664.6243	369.0988	671.0319	TM3	TM7					
2	0.1796	38.7875	666.798	666.3095	375.2197	672.874	TM1	TM4					
2	0.1769	39.0731	666.9778	666.4742	375.8226	673.0538	TM1	TM2					
2	0.1664	40.2135	667.6902	667.127	378.2208	673.7663	TM2	TM3					
2	0.1239	44.8172	670.4774	669.6859	387.7513	676.5535	TM4	TM7					
2	0.1215	45.0692	670.6261	669.8226	388.2663	676.7022	TM1	TM5					
2	0.1011	47.2834	671.9154	671.009	392.7615	677.9914	TM1	TM3					
2	0.0761	49.9815	673.4474	672.421	398.1709	679.5234	TM1	TM7					
2	0.0676	50.9004	673.9597	672.8937	399.9965	680.0358	TM5	TM7					
2	0.0348	54.4582	675.9003	674.6865	406.9874	681.9763	TM4	TM5					
3	0.5353	1.3467	635.905	638.9472	282.4068	644.0064	TM2	TM3	TM4				
3	0.5344	1.4408	636.0117	639.0378	282.6759	644.1131	TM1	TM2	TM4				
3	0.5331	1.5791	636.168	639.1706	283.0709	644.2695	TM2	TM4	TM7				
3	0.5322	1.6745	636.2758	639.262	283.3432	644.3772	TM2	TM4	TM5				
3	0.4275	12.7878	647.582	648.9395	313.4398	655.6834	TM2	TM5	TM7				
3	0.4245	13.101	647.8698	649.1879	314.2462	655.9712	TM1	TM2	TM5				
3	0.4245	13.1074	647.8756	649.193	314.2627	655.977	TM2	TM3	TM5				
3	0.4003	15.6801	650.185	651.1911	320.81	658.2865	TM1	TM2	TM7				
3	0.4002	15.6862	650.1904	651.1957	320.8252	658.2918	TM2	TM3	TM7				
3	0.3066	25.6273	658.3131	658.2831	344.9573	666.4145	TM3	TM4	TM7				
3	0.3012	26.1939	658.7424	658.6604	346.2822	666.8438	TM3	TM4	TM5				
3	0.3009	26.2322	658.7712	658.6857	346.3714	666.8726	TM1	TM3	TM4				
3	0.2327	33.4763	663.9857	663.2886	362.8787	672.0871	TM3	TM5	TM7				
3	0.231	33.652	664.1063	663.3956	363.2699	672.2077	TM1	TM3	TM5				
3	0.195	37.4739	666.668	665.6716	371.6745	674.7694	TM1	TM4	TM7				
3	0.1928	37.708	666.8211	665.8079	372.183	674.9225	TM1	TM3	TM7				
3	0.1697	40.161	668.4014	667.2168	377.4715	676.5028	TM1	TM4	TM5				
3	0.1613	41.0559	668.967	667.722	379.3825	677.0684	TM1	TM2	TM7				
3	0.1293	44.4551	671.0646	669.5993	386.555	679.1661	TM1	TM5	TM7				
3	0.1215	45.2759	671.5596	670.0432	388.2671	679.661	TM4	TM5	TM7				
4	0.5269	3.2694	637.8171	641.1459	284.9384	647.9439	TM1	TM2	TM3	TM4			
4	0.5267	3.2874	637.837	641.1625	284.9906	647.9644	TM2	TM3	TM4	TM7			
4	0.5264	3.3201	637.8748	641.1925	285.0852	648.0016	TM2	TM4	TM5	TM7			
4	0.5263	3.3257	637.8811	641.1976	285.1013	648.0079	TM2	TM3	TM4	TM5			
4	0.5257	3.3873	637.951	641.2541	285.2793	648.0778	TM1	TM2	TM4	TM7			
4	0.5255	3.4135	637.9807	641.2781	285.3548	648.1074	TM1	TM2	TM4	TM5			
4	0.4168	14.7367	649.5349	650.7428	316.3648	659.6616	TM2	TM3	TM5	TM7			
4	0.4167	14.7391	649.5371	650.7447	316.3711	659.6639	TM1	TM2	TM5	TM7			
4	0.4136	15.0626	649.8345	650.9917	317.2124	659.9613	TM1	TM2	TM3	TM5			
4	0.3885	17.6799	652.1849	652.9498	323.9394	662.3116	TM1	TM2	TM3	TM7			
4	0.294	27.5197	660.2312	659.7346	348.0682	670.3579	TM1	TM3	TM4	TM7			
4	0.2934	27.5813	660.2781	659.7745	348.214	670.4048	TM3	TM4	TM5	TM7			
4	0.2893	28.0052	660.5998	660.0484	349.2157	670.7265	TM1	TM3	TM4	TM5			
4	0.2188	35.348	665.8974	664.5872	366.1305	676.0242	TM1	TM3	TM5	TM7			
4	0.1848	38.8944	668.287	666.6518	374.0261	678.4138	TM1	TM4	TM5	TM7			
5	0.5195	5.0557	639.5737	643.2324	287.149	651.7259	TM2	TM3	TM4	TM5	TM7		
5	0.5187	5.1433	639.6736	643.309	287.4052	651.8257	TM1	TM2	TM4	TM5	TM7		
5	0.5178	5.2282	639.7703	643.3832	287.6535	651.9224	TM1	TM2	TM3	TM4	TM7		
5	0.5177	5.2387	639.7823	643.3924	287.6843	651.9344	TM1	TM2	TM3	TM4	TM5		
5	0.4053	16.7165	651.5162	652.572	319.4596	663.6684	TM1	TM2	TM3	TM5	TM7		
5	0.2803	29.4779	662.1993	661.2318	351.4318	674.3515	TM1	TM3	TM4	TM5	TM7		
6	0.5103	7.0000	641.5101	645.4693	289.8996	655.6876	TM1	TM2	TM3	TM4	TM5	TM7	

Table 2. Parameters of the ‘Best fit’ regression models of stand volumes based on the spectral reflectance values, TM 2 and TM 4

Model Group	Model description		Coefficients of Independent Variables	S.E. of Variables	t statistics	Pr > t
	Dependent Variables	Independent Variables				
2	Stand Volume	Constant	5020.8902	624.8097	8.04	0.0001
		TM 2	-294.3667	37.4444	-7.86	0.0001
		TM 4	28.3923	4.3121	6.58	0.0001

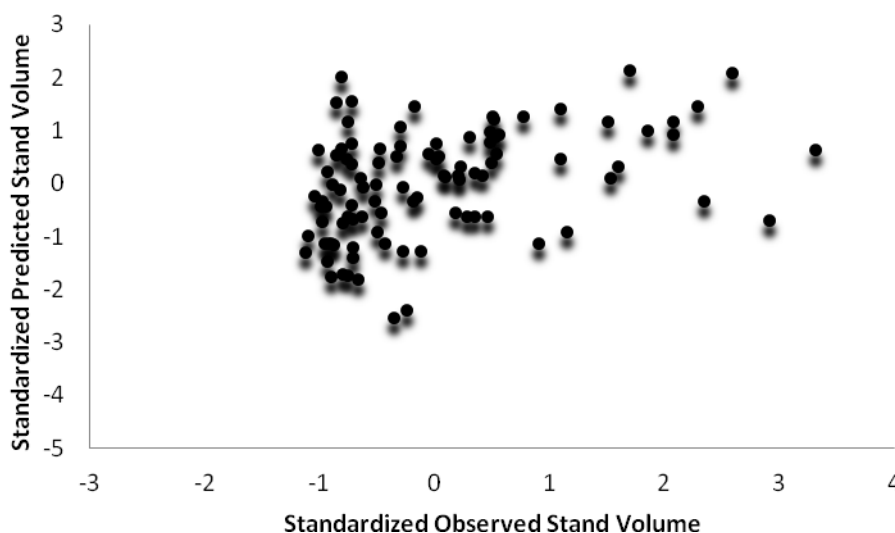


Fig. 1. The standardized predicted stand volume values versus standardized observed values

Discussion

In this paper, we evaluated the relationships between stand volume and reflectance values obtained from Landsat TM satellite image. Results obtained from this study show the significant relationship between stand volume and Landsat TM reflectance values and the utility of transformed bands in modeling stand volume. A linear combination of TM 2 and TM 4 described more variance in stand volume than other combinations of TM bands. The important relationship at the 95% possibility level, normality of the residuals, $R^2=0.5409$ and RMSE of $280.6871 \text{ m}^3 \text{ ha}^{-1}$. R^2 values obtained from this study were higher than the ones obtained through direct estimation to forecast stand volume ($R^2=0.43$, Mohammadi et al., 2010; $R^2=0.3$, Hall et al., 2006; $R^2= 0.3$, Trotter et al., 1997). Makela et al. (2004) predicted forest stand volume using Landsat TM imagery and stand-level field-inventory data. They predicted total stand volume using Landsat

TM images with an estimated RMSE of about 48%. Huiyan et al. (2006) have studied the possibility of estimation of forest volume by integrating Landsat TM imagery and forest inventory data. They estimated RMSE of about 44.2%. Mallinis et al. (2003) found that multiple regression analysis with TM 2-5; TM 2, TM 3 and TM 5; TM 1-5 and TM 7 as independent variables could better and low predict ($R^2=0.183$), ($R^2=0.172$) and ($R^2=0.117$), respectively for stand volume.

Conclusion

Forest stand parameters can be defined by many stand parameters such as stand volume, basal area, age, tree density and height. However, these data gathering are time- and labor-consuming by conventional forest inventory. Remote sensing is alternatively a better method for obtaining vision of forest characteristics. Results obtained from this study showed that the TM data are beneficial to estimate stand volume and could be used by source directors to advantage visions about variations within managed stands.

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