# Application of Social Spider Optimization for Permutation Flow Shop Scheduling Problem 

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#### Abstract

Permutation flow shop scheduling problem (PFSP) is an NP-complete problem with a wide range of applications in many real-world applications. Social spider optimization (SSO) is a swarm intelligence algorithm proposed for continuous optimization problems. Recently, SSO has received increased interest in the field of combinatorial optimization as well. For this reason, in this paper, SSO algorithm is proposed to solve the PFSP with make span minimization. The proposed algorithm has been tested on 141 well-known benchmark instances and compared against six other conventional and best-so-far metaheuristics. The obtained results show that SSO outperforms some of the compared works although they are hybrid methods.


KEYWORDS: Metaheuristic, Optimization, Flow Shop Scheduling, Social Spider, Swarm Intelligence.

## 1. INTRODUCTION

Flow shop is a renowned manufacturing layout in which a set of jobs should be processed, in the same order, on a set of machines. The flow shop scheduling problem considers the sequence of the jobs over the machines with respect to a certain performance measure, such as makespan, maximum lateness, or total weighted completion time. If each machine should process the jobs in the same order, the problem is called as permutation flow shop scheduling problem (PFSP) [1]. PFSP is an NPcomplete problem that has several real-life application fields, such as computing designs, production, information processing, communications, and transportation [2].

Due to its complexity and practical relevance, PFSP has been addressed by a considerable number of metaheuristic algorithms. These algorithms include discrete jaya algorithm [3], genetic-shuffled frog-leaping [4], Iterative beam search [5], evolutionary algorithm [6], hybrid backtracking search [2], shuffled complex evolution [7], genetic algorithm [8-10] bacterial foraging optimization [11], bat algorithm (BA) [12], rhinoceros search [13], biogeography-based optimization [14], differential evolution [15] [16], harmony search [17], cuckoo search [18], scatter search [19], iterated greedy [20], monkey search [21], and ant colony optimization (ACO) [22].

Social spider optimization (SSO) is a new swarm intelligence algorithm that has been proposed for continuous optimization problems [23]. However, recently, there has been an increased interest in applying it for solving combinatorial problems. Works such as [24-28] have shown it as a promising area of research for combinatorial problems.

In this paper, SSO is proposed for the PFSP with makespan minimization. The aim is to examine the effectiveness of SSO on PFSP as it has been widely used as a benchmark problem to validate the effectiveness of many optimization algorithms. To the best of our knowledge, there is no published work to address the PFSP by using this algorithm. The remainder of this paper is structured as follows. The problem definition is given in the next section. Section 3 describes the proposed algorithm. The computational results are reported in Section 4. The conclusion and future works are presented in Section 5.

## 2. PROBLEM DEFINITION

Suppose that $n$ jobs $\left\{J_{i}\right\}_{i=1}^{n}$ need to be sequentially processed on $m$ machines $\left\{M_{k}\right\}_{k=1}^{m}$. Each job $J_{i}$ is composed of $m$ operations $\left(O_{i l}, O_{i 2}, \ldots, O_{i m}\right)$. All jobs should have the same processing order on each machine. $O_{i k}$ represents the operation of job $J_{i}$ on machine $M_{k}$ which needs using $M_{k}$ solely for a specified continued time called $P_{i k}$ ( pre-emption is not allowed). Let $\pi=\left\{\pi_{1}, \pi_{2}, \ldots, \pi_{n}\right\}$ be a permutation of the jobs in which $\pi_{i}$ denotes the index of the job placed at the $i$ th position of $\pi$. Then, the completion time of each job $C\left(\pi_{i}, k\right), i=1, \ldots, n$ can be calculated by the following set of recursive formulas [29].
$C\left(\pi_{1}, 1\right)=p_{\pi_{1} 1}$,
$C\left(\pi_{i}, 1\right)=C\left(\pi_{i-1}, 1\right)+p_{\pi_{i} 1}, \quad i=2, \ldots, n$,
$C\left(\pi_{1}, k\right)=C\left(\pi_{1}, k-1\right)+p_{\pi_{1} k}, \quad k=2, \ldots, \mathrm{~m}$,
$C\left(\pi_{i}, k\right)=\max \left\{C\left(\pi_{i-1}, k\right), C\left(\pi_{i}, k-1\right)\right\}+p_{\pi_{i} k}, \quad i=2, \ldots, n, \quad k=2, \ldots, \mathrm{~m}$,

Then, the makespan is given by

$$
\begin{equation*}
C_{\max }(\pi)=C\left(\pi_{n}, m\right) \tag{5}
\end{equation*}
$$

Therefore, the problem turns into finding a permutation $\pi^{*}$ in the set of all permutations $\Pi$ such that $C_{\text {max }}\left(\pi^{*}\right) \leq C\left(\pi_{n}, m\right) \quad \forall \pi \in \Pi$.

## 3. SOCIAL SPIDER OPTIMIZATION

### 3.1 BACKGROUND

The social spider optimization (SSO) suggested by Cuevas et al. [30] is a recent swarm intelligence algorithm inspired by the collaborative behavior of social spider colony. This behavior can be summarized in the following way. A social spider colony is composed of two essential components: spiders and communal web. The spiders are grouped into two different categories: males
and females. Based on its gender, each spider collaborates in different tasks such as building and maintaining the communal web, prey capturing, and mating. Interactions among spiders are either direct or indirect. Direct interactions involve physical contact, such as mating. Indirect interactions take place by using the communal web as a medium of communication that transfers important information, such as the size of the trapped preys and characteristics of the neighboring members. This information, which is encoded as small vibrations, is a crucial portion for the mutual coordination among the spiders. The intensity of these vibrations is dependent on the locations and weights of the spiders that generate them [30].

This collaborative behavior can be utilized for solving optimization problems by simulation as follows. SSO imagines the communal web as the search space. The location of a spider in the communal web symbolizes a solution of the problem in the search space. Each spider is given a value for its weight that depends on the fitness of the solution that is represented by it. Unlike most of the existent swarm algorithms, SSO models two different search agents (spiders): males for performing extensive exploitation and females for performing efficient exploration. This allows not only to imitate the collaborative behavior of the colony in a better realistic way, but also to utilize computational operators that can delay the premature convergence and somehow strike an exploration-exploitation balance [30]. The search process is controlled by three operators: the female cooperative operator that changes the locations of females, the male cooperative operator that changes the locations of males, and the mating operator that produces new spiders that are located on new locations in the search space [30]. Figure 1 describes the general framework of the proposed SSO. As it can be noticed, a supplementary step has been added to the classical SSO, in which the locations of the spiders that exist in the continuous space are converted to their equivalent locations in the combinatorial space. What follows is the mathematical modelling of the proposed SSO [30].


Figure 1. The proposed SSO.

### 3.2 GENDER ASSIGNATION

The first step in SSO is determining the number of female and male spiders. Since social spider colonies are highly female-biased ones, the number of females $N_{f}$ is selected at random in the range $65-90 \%$ of the population. Let $N$ be the total number of spiders, then $N_{f}$ is calculated using the following formula.
$N_{f}=$ floor $[(0.9-\operatorname{rand} \cdot 0.25) \cdot N]$
where rand is a random number in the range $(0,1)$, and the floor function is used to convert a real number into an integer number. The number of male spiders $N_{m}$ is calculated as the complement between $N$ and $N_{f}$ using the following formula.
$N_{m}=N-N_{f}$
For that reason, the entire population of spiders $S$ is split into female spiders group $F=\left\{f_{1}, f_{2}, \ldots f_{N_{f}}\right\}$ and male spiders group $M=\left\{m_{1}, m_{2}, \ldots m_{N_{m}}\right\}$, where $S=F \cup M\left(S=\left\{s_{1}, s_{2}, \ldots s_{N}\right\}\right)$, such that $S=$ $\left\{s_{1}=f_{1}, s_{2}=f_{2}, \ldots, s_{N_{f}}=f_{N_{f}}, s_{N_{f}+1}=m_{1}, s_{N_{f}+2}=m_{2}, \ldots, s_{N}=m_{N_{m}}\right\}$.

### 3.3 COLONY INITIALIZATION

The locations of all spiders are initialized at random. Each spider location, $f_{i}$ or $m_{i}$, is an $n$ dimensional vector that represents the optimization variables, where $n$ is the number of jobs in PFSP. The $n$ components of each vector are uniformly distributed between the predefined lower initial parameter bound $p_{j}^{l o w}$ and upper parameter bound $p_{j}^{\text {high }}$. These values are calculated using the following formulas.
$f_{i, j}^{0}=p_{j}^{\text {low }}+\operatorname{rand}(0,1) \cdot\left(p_{j}^{\text {high }}-p_{j}^{\text {low }}\right) i=1,2, \ldots, N_{f} ; j=1,2, \ldots, n$
$m_{k, j}^{0}=p_{j}^{\text {low }}+\operatorname{rand}(0,1) \cdot\left(p_{j}^{\text {high }}-p_{j}^{\text {low }}\right) k=1,2, \ldots, N_{m} ; j=1,2, \ldots, n$
where $j$ refers to the index of a variable, $i$ refers to the index of a female individual, $k$ refers to the index of a male individual, the value 0 indicates that the individuals belong to the initial population, and $\operatorname{rand}(0,1)$ is a function used to generate a random number in the range $(0,1)$. Hence, $f_{i, j}$ is the $j$ th job of the $i$ th female spider and $m_{k, j}$ is the $j$ th job of the $k$ th male spider.

### 3.4 CONTINUOUS TO COMBINATORIAL TRANSFORMATION

Since SSO works only on real numbers encoding, the random keys discretization method, which was initially proposed in [31], is utilized to transfer the locations of spiders from the continuous space to their corresponding locations in the combinatorial space.

### 3.5 WEIGHT CALCULATION AND ASSIGNATION

In the biological metaphor, the size of a spider is the characteristic that estimates its ability to do its assigned duties well. In SSO, each individual $i$ of the population $S$ is assigned a weight $w_{i}$ that depends on the quality of the solution it symbolizes (irrespective of gender). The weight of each spider is calculated by using the following formula.
$w_{i}=\frac{C_{\max }\left(s_{i}\right)-C_{\max }^{\text {worst }}}{C_{\text {max }}^{\text {best }}-C_{\text {max }}^{\text {worst }}}$
where $C_{\max }\left(s_{i}\right)$ is the makespan value obtained by decoding the permutation of jobs that corresponds to the location of the spider $s_{i}$, and $C_{\max }^{\text {best }}$ and $C_{\max }^{\text {worst }}$ are the makespan values of the best and worst individuals in the population, respectively.

### 3.6 MODELING OF THE VIBRATIONS

The vibrations observed by a spider depend on the distance and weight of the spiders that generate them. In SSO, the vibrations observed by spider $i$ as a result of the information sent by another spider $j$ are modeled according to the following formula.
$V i b_{i j}=w_{j} \cdot e^{-d_{i, j}^{2}}$
where $d_{i, j}$ is the Euclidean distance between the two spiders. SSO considers that each spider $i$ is supposed to be able to detect vibrations from three other spiders. These spiders are the closest one that has a higher weight $V i b c_{i}$, the best spider in the colony $V_{i b b_{i}}$, and the nearest female spider $V_{i b f_{i}}$.

### 3.7 FEMALE COOPERATIVE OPERATOR

Female spiders are commonly attracted to the other (male or female) spiders in accordance with their vibrations transmitted over the communal web. Strong vibrations are generated by either big spiders or other neighboring spiders lying nearby the spider that is perceiving them. The decision of attraction or repulsion is made according to an internal state which is affected by several factors such as reproduction cycle, curiosity, and other random phenomena. This behavior is modeled by the female cooperative operator which is defined as follows.
$f_{i}^{k+1}=\left\{\begin{array}{c}f_{i}^{k}+\alpha \cdot \operatorname{Vibc}_{i} \cdot\left(s_{c}-f_{i}^{k}\right)+\beta . \operatorname{Vibb}_{i} \cdot\left(s_{b}-f_{i}^{k}\right) \\ +\delta \cdot\left(\operatorname{rand}-\frac{1}{2}\right) \quad \text { if } r_{m}<P F \\ f_{i}^{k}-\alpha \cdot \operatorname{Vibc_{i}} \cdot\left(s_{c}-f_{i}^{k}\right)-\beta . \operatorname{Vibb}_{i} \cdot\left(s_{b}-f_{i}^{k}\right) \\ +\delta \cdot\left(\operatorname{rand}-\frac{1}{2}\right) \quad \text { if } r_{m}>P F\end{array}\right.$
where $\alpha, \beta, \delta, r_{m}$, and rand are random numbers in the range $(0,1), k$ represents the iteration counter, $P F$ represents the threshold value used for determining whether an attraction or repulsion movement is produced, $s_{c}$ is the closest spider to spider $i$ that has a higher weight, and $s_{b}$ is the best spider in the population.

### 3.8 MALE COOPERATIVE OPERATOR

Male spiders consider themselves as a group of alpha males which dominate the colony resources. Hence, the males are divided into two sets: dominant and non-dominant males. Dominant males usually have superior fitness attributes to non-dominant males. In addition, dominant males are enticed to the nearest female spiders in the communal web. On the hand, non-dominant males tend to localize on the center of the set of males as a strategy to benefit from the resources left over from the dominant males. For implementing such phenomena, the set of males $M=\left\{m_{1}, m_{2}, \ldots m_{N_{m}}\right\}$ is sorted according to their weight values in increasing order. The male spider that is located in the middle, whose weight value is $w_{N_{f}+m}$, is treated as the median male spider. The male spiders whose weight values are bigger the median value are treated as members of the set of dominant males $D$, and the rest of males are treated as members of the non-dominant set $N D$. In accordance to this, the variation of locations for the male spiders is modeled by the following formula.
$m_{i}^{k+1}=\left\{\begin{array}{c}m_{i}^{k}+\alpha \cdot \operatorname{Vibf}_{i} \cdot\left(s_{f}-m_{i}^{k}\right)+\delta \cdot\left(\text { rand }-\frac{1}{2}\right) \\ \text { if } w_{N_{f}+i}>w_{N_{f}+m} \\ m_{i}^{k}+\alpha \cdot\left(\frac{\sum_{h=1}^{N_{m}} m_{h}^{k} \cdot w_{N_{f}+h}}{\sum_{h=1}^{N_{m} w_{N_{f}+h}}}-m_{i}^{k}\right) \\ \text { if } w_{N_{f}+i} \leq w_{N_{f}+m}\end{array}\right.$
where $s_{f}$ is the nearest female spider to the male $i$, and $\sum_{h=1}^{N_{m}} m_{h}^{k} \cdot w_{N_{f}+h} / \sum_{h=1}^{N_{m}} w_{N_{f}+h}$ is the weighted mean of the set of male spiders $M$.

### 3.9 MATING OPERATOR

Mating is performed by dominant males and females. A dominant male spider $m_{g}\left(m_{g} \in D\right)$ can mate with a set of female spiders $E^{g}$ if they exist within a specific radius $r$ (range of mating). This radius, which depends on the size of the search space, is calculated by the following formula.
$r=\frac{\sum_{j=1}^{n}\left(p_{j}^{\text {high }}-p_{j}^{\text {low }}\right)}{2 \cdot n}$
If $E^{g}=\emptyset$, the mating process is revoked. Otherwise, mating occurs and a new brood $s_{\text {new }}$ is generated by taking in consideration all elements of the set $T^{g}$ which is the union $m_{g} \cup E^{g}$. During the mating process, the weight of each element of the set $T^{g}$ controls the probability of its impact on the new brood. The members with higher weight values have higher probabilities to impact the new spider than those with lighter weight values. The impact probability $P s_{i}$ of each member is calculated by the roulette wheel method, which is defined as follows.
$P s_{i}=\frac{w_{i}}{\sum_{j \in T^{g}} w_{j}}$
where $i \in T^{g}$. When a new spider is born, it is immediately compared to the spider holding the worst
weight of the whole colony. If the new spider is superior to the worst spider, it replaces it. Otherwise, the worst spider is kept and the new spider is neglected.

## 4. COMPUTATIONAL RESULTS

SSO has been implemented in C++. The tests have been run on a personal computer with 3.4 GHz CPU and 8 GB RAM. Two well-known benchmark sets were used for the evaluation. The first set is Reeves's set [32]. This set is composed of 21 instances that are divided into 7 equal subsets of different sizes. These sizes range from 20 jobs and 5 machines up to 75 jobs and 20 machines. The second set is Taillard's set [33]. This set is composed of 120 instances that are divided into 12 equal subsets of different sizes. These sizes range from 20 jobs and 5 machines up to 500 jobs and 20 machines. In order to tune the parameters, preliminary experiments have been done on 19 instances selected randomly from the two benchmark sets (one of each subset). Consequently, the parameters have been set as follows: $N=100, P F=0.7, \alpha, \beta, \delta$, and $r_{m}$ are as assigned random values between zero and one, and the maximum number of iterations is 10000 .

SSO was compared with conventional and best-so-far metaheuristics. The metaheuristics that were compared using Reeves's set are chaotic local search based bacterial foraging algorithm (CLS-BFO) [11], shuffled complex evolution algorithm with opposition-based learning (SCE-OBL) [7], and Genetic algorithm integrated with artificial chromosomes (ACGA) [34]. The metaheuristics that were compared using Taillard's set are memetic algorithm with novel semi-constructive evolution operators (MASC) [8] which is one of the best-so-far approaches for the problem, hybrid whale optimization algorithm based on local search strategy (HWA) [35], and self-guided differential evolution with neighborhood search (NS-SGDE) [16]. SSO was run 10 independent times and the best solution (BS) among them was considered for the comparison. Table 1 presents the results on Reeves's set. It lists instance name, instance size (number of jobs * number of machines), best known solution (BKS), BS of each algorithm. From Table 1, it can be seen that SSO is able to obtain better solutions than the others on most of the instances. However, to make a precise comparison, the relative error of BS for each instance (PE), and the average of PE for the whole set of instances (APE) were calculated for each algorithm as follows.
$P E=100 \times\left(\frac{B S-B K S}{B K S}\right)$
$A P E=\left(\sum_{i=1}^{21}\left(\frac{B S_{i}-B K S_{i}}{B K S_{i}}\right) \times 100\right) / 21$
Table 2 presents the results. It lists $A P E$ values for SSO and the other algorithms (OA), and the percentage improvement (PI) achieved by SSO in APE values with respect to each of the other algorithms, which was calculated as follows.
$P I=100 \times\left(O A_{A P E}-S S O_{A P E}\right) / O A_{A P E}$

From Table 2, it can be seen that SSO has the lowest $A P E$ value and produces relative improvements to all the other algorithms. This shows that SSO is an effective approach since the compared works are hybrid methods. To further verify the effectiveness of SSO, the one-way ANOVA test was applied on the $P E$ values. Figure 2 shows the results. From Figure 2, it can be seen that SSO outperforms the compared algorithms, and the resulting $p$-value is 0,009 which implies that the algorithms are significantly statistically different with each other

Table 1. The computational results on Reeves's set.

| Instance | $n * m$ | BKS | SSO | SCE-OBL | CLS-BFO | ACGA |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Rec1 | 20x5 | 1245 | 1247 | 1249 | 1249 | 1249 |
| Rec3 | 20x5 | 1109 | 1109 | 1111 | 1111 | 1109 |
| Rec5 | 20x5 | 1242 | 1245 | 1245 | 1245 | 1245 |
| Rec7 | 20x10 | 1566 | 1566 | 1584 | 1584 | 1566 |
| Rec9 | 20x10 | 1537 | 1537 | 1545 | 1545 | 1537 |
| Rec11 | 20x10 | 1431 | 1431 | 1431 | 1449 | 1431 |
| Rec13 | 20x15 | 1930 | 1935 | 1963 | 1968 | 1935 |
| Rec15 | 20x15 | 1950 | 1968 | 1993 | 1993 | 1950 |
| Rec17 | 20x15 | 1902 | 1923 | 1944 | 1954 | 1911 |
| Rec19 | $30 \times 10$ | 2093 | 2117 | 2156 | 2139 | 2099 |
| Rec21 | $30 \times 10$ | 2017 | 2017 | 2064 | 2059 | 2046 |
| Rec23 | $30 \times 10$ | 2011 | 2030 | 2067 | 2073 | 2021 |
| Rec25 | 30x15 | 2513 | 2566 | 2584 | 2638 | 2545 |
| Rec27 | $30 \times 15$ | 2373 | 2397 | 2445 | 2443 | 2396 |
| Rec29 | $30 \times 15$ | 2287 | 2333 | 2364 | 2408 | 2304 |
| Rec31 | $50 \times 10$ | 3045 | 3104 | 3179 | 3180 | 3105 |
| Rec33 | $50 \times 10$ | 3114 | 3118 | 3154 | 3187 | 3140 |
| Rec35 | $50 \times 10$ | 3277 | 3277 | 3281 | 3292 | 3277 |
| Rec37 | $75 \times 20$ | 4890 | 5096 | 5327 | 5422 | 5193 |
| Rec39 | $75 \times 20$ | 5043 | 5185 | 5391 | 5465 | 5276 |
| Rec41 | $75 \times 20$ | 4910 | 5135 | 5334 | 5436 | 5208 |

Table 2. $A P E$ of SSO and the other works on Reeves's set.

| Algorithm | APE |  |  |  |
| :--- | :---: | :---: | :--- | :---: |
|  | OA (\%) | SSO (\%) |  |  |
| CLS-BFO | 2,675 |  | SSO (\%) |  |
| SCE-OBL | 3,255 |  |  | 58 |
| ACGA | 1,247 | 1,123 |  | 65 |
| Annnn | 1,123 |  | 10 |  |



Figure 2. Means and 95\% confidence intervals on Reeves's set.

Table 3. The computational results on ST1.

| Instance | $n * m$ | BKS | SSO | NS-SGDE | HWA | MASC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ta001 | 20x5 | 1278 | 1282 | 1278 | 1278 | 1278 |
| Ta002 | 20x5 | 1359 | 1359 | 1359 | 1359 | 1359 |
| Ta003 | 20x5 | 1081 | 1088 | 1081 | 1081 | 1081 |
| Ta004 | 20x5 | 1293 | 1300 | 1293 | 1293 | 1293 |
| Ta005 | 20x5 | 1235 | 1237 | 1235 | 1235 | 1235 |
| Ta006 | 20x5 | 1195 | 1195 | 1195 | 1195 | 1195 |
| Ta007 | 20x5 | 1239 | 1243 | 1239 | 1239 | 1239 |
| Ta008 | 20x5 | 1206 | 1206 | 1206 | 1206 | 1206 |
| Ta009 | 20x5 | 1230 | 1231 | 1230 | 1230 | 1230 |
| Ta010 | 20x5 | 1108 | 1108 | 1108 | 1108 | 1108 |
| Ta011 | 20x10 | 1582 | 1598 | 1582 | 1582 | 1582 |
| Ta012 | 20x10 | 1659 | 1682 | 1659 | 1659 | 1659 |
| Ta013 | 20x10 | 1496 | 1513 | 1496 | 1496 | 1496 |
| Ta014 | 20x10 | 1377 | 1395 | 1377 | 1377 | 1377 |
| Ta015 | 20x10 | 1419 | 1440 | 1419 | 1419 | 1419 |
| Ta016 | 20x10 | 1397 | 1404 | 1397 | 1397 | 1397 |
| Ta017 | 20x10 | 1484 | 1493 | 1484 | 1484 | 1484 |
| Ta018 | 20x10 | 1538 | 1555 | 1538 | 1538 | 1538 |
| Ta019 | 20x10 | 1593 | 1606 | 1593 | 1593 | 1593 |
| Ta020 | 20x10 | 1591 | 1611 | 1591 | 1591 | 1591 |
| Ta021 | 20x20 | 2297 | 2329 | 2297 | 2297 | 2297 |
| Ta022 | 20x20 | 2099 | 2125 | 2099 | 2099 | 2099 |
| Ta023 | $20 \times 20$ | 2326 | 2350 | 2326 | 2326 | 2326 |
| Ta024 | 20x20 | 2223 | 2244 | 2223 | 2223 | 2223 |
| Ta025 | 20x20 | 2291 | 2309 | 2291 | 2291 | 2291 |
| Ta026 | $20 \times 20$ | 2226 | 2244 | 2228 | 2226 | 2226 |
| Ta027 | 20x20 | 2273 | 2296 | 2273 | 2273 | 2273 |
| Ta028 | 20x20 | 2200 | 2229 | 2200 | 2200 | 2200 |
| Ta029 | $20 \times 20$ | 2237 | 2252 | 2237 | 2237 | 2237 |
| Ta030 | 20x20 | 2178 | 2195 | 2178 | 2178 | 2178 |
| Ta031 | 50x5 | 2724 | 2724 | 2724 | 2724 | 2724 |
| Ta032 | $50 \times 5$ | 2834 | 2839 | 2834 | 2834 | 2834 |
| Ta033 | 50x5 | 2621 | 2621 | 2621 | 2621 | 2621 |
| Ta034 | 50x5 | 2751 | 2753 | 2751 | 2751 | 2751 |
| Ta035 | 50x5 | 2863 | 2863 | 2863 | 2863 | 2863 |
| Ta036 | 50x5 | 2829 | 2832 | 2829 | 2829 | 2829 |
| Ta037 | 50x5 | 2725 | 2725 | 2725 | 2725 | 2725 |
| Ta038 | 50x5 | 2683 | 2703 | 2683 | 2683 | 2683 |
| Ta039 | 50x5 | 2552 | 2561 | 2552 | 2552 | 2552 |
| Ta040 | 50x5 | 2782 | 2782 | 2782 | 2782 | 2782 |
| Ta041 | 50x10 | 2991 | 3053 | 3021 | 3021 | 3024 |
| Ta042 | $50 \times 10$ | 2867 | 2938 | 2896 | 2891 | 2882 |
| Ta043 | 50x10 | 2839 | 2890 | 2888 | 2869 | 2852 |
| Ta044 | 50x10 | 3063 | 3071 | 3075 | 3063 | 3063 |
| Ta045 | 50x10 | 2976 | 3024 | 3027 | 3001 | 2982 |
| Ta046 | 50x10 | 3006 | 3050 | 3029 | 3006 | 3006 |
| Ta047 | 50x10 | 3093 | 3133 | 3124 | 3126 | 3099 |
| Ta048 | 50x10 | 3037 | 3046 | 3055 | 3046 | 3038 |
| Ta049 | 50x10 | 2897 | 2927 | 2928 | 2897 | 2902 |
| Ta050 | 50x10 | 3065 | 3131 | 3092 | 3078 | 3077 |
| Ta051 | $50 \times 20$ | 3850 | 3974 | 3916 | 3876 | 3889 |
| Ta052 | 50x20 | 3704 | 3808 | 3744 | 3715 | 3720 |
| Ta053 | $50 \times 20$ | 3640 | 3772 | 3702 | 3653 | 3667 |
| Ta054 | 50x20 | 3720 | 3849 | 3793 | 3755 | 3754 |
| Ta055 | $50 \times 20$ | 3610 | 3746 | 3677 | 3649 | 3644 |
| Ta056 | $50 \times 20$ | 3681 | 3795 | 3743 | 3703 | 3708 |
| Ta057 | $50 \times 20$ | 3704 | 3835 | 3784 | 3723 | 3754 |
| Ta058 | $50 \times 20$ | 3691 | 3829 | 3757 | 3704 | 3711 |
| Ta059 | $50 \times 20$ | 3743 | 3870 | 3795 | 3763 | 3772 |
| Ta060 | $50 \times 20$ | 3756 | 3875 | - | 3767 | 3778 |

Table 4. The computational results on ST2.

| Instance | $n * m$ | BKS | SSO | NS-SGDE | HWA | MASC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ta061 | 100x5 | 5493 | 5493 | 5493 | 5493 | 5493 |
| Ta062 | 100x5 | 5268 | 5284 | 5283 | 5268 | 5268 |
| Ta063 | 100x5 | 5171 | 5193 | 5182 | 5175 | 5175 |
| Ta064 | 100x5 | 5014 | 5023 | 5018 | 5018 | 5014 |
| Ta065 | 100x5 | 5250 | 5250 | 5253 | 5250 | 5250 |
| Ta066 | 100x5 | 5135 | 5137 | 5135 | 5135 | 5135 |
| Ta067 | 100x5 | 5246 | 5259 | 5246 | 5246 | 5246 |
| Ta068 | 100x5 | 5094 | 5106 | 5094 | 5094 | 5094 |
| Ta069 | 100x5 | 5448 | 5467 | 5448 | 5448 | 5448 |
| Ta070 | 100x5 | 5322 | 5338 | 5322 | 5324 | 5322 |
| Ta071 | 100x10 | 5770 | 5787 | 5784 | 5776 | 5770 |
| Ta072 | 100x10 | 5349 | 5379 | 5362 | 5362 | 5349 |
| Ta073 | 100x 10 | 5676 | 5691 | 5691 | 5691 | 5677 |
| Ta074 | 100x10 | 5781 | 5849 | 5826 | 5825 | 5781 |
| Ta075 | 100x10 | 5467 | 5513 | 5503 | 5491 | 5467 |
| Ta076 | 100x10 | 5303 | 5328 | 5308 | 5308 | 5304 |
| Ta077 | 100x10 | 5595 | 5662 | 5610 | 5608 | 5596 |
| Ta078 | 100x10 | 5617 | 5695 | 5630 | 5630 | 5625 |
| Ta079 | 100x10 | 5871 | 5916 | 5882 | 5891 | 5875 |
| Ta080 | 100x10 | 5845 | 5903 | 5881 | 5848 | 5845 |
| Ta081 | 100x 20 | 6202 | 6377 | 6360 | 6280 | 6257 |
| Ta082 | $100 \times 20$ | 6183 | 6360 | 6278 | 6278 | 6223 |
| Ta083 | $100 \times 20$ | 6271 | 6450 | 6405 | 6368 | 6325 |
| Ta084 | 100x20 | 6269 | 6393 | 6394 | 6350 | 6303 |
| Ta085 | $100 \times 20$ | 6314 | 6477 | 6452 | 6377 | 6380 |
| Ta086 | $100 \times 20$ | 6364 | 6544 | 6461 | 6430 | 6431 |
| Ta087 | 100x20 | 6268 | 6439 | 6385 | 6354 | 6306 |
| Ta088 | $100 \times 20$ | 6401 | 6603 | 6496 | 6515 | 6472 |
| Ta089 | 100x20 | 6275 | 6451 | 6428 | 6396 | 6330 |
| Ta090 | $100 \times 20$ | 6434 | 6625 | 6538 | 6527 | 6456 |
| Ta091 | 200x 10 | 10862 | 10947 | 10887 | 10885 | 10872 |
| Ta092 | 200x 10 | 10480 | 10542 | 10555 | 10512 | 10487 |
| Ta093 | 200x 10 | 10922 | 11005 | 10980 | 10965 | 10922 |
| Ta094 | 200x10 | 10889 | 10939 | 10917 | 10889 | 10889 |
| Ta095 | 200x 10 | 10524 | 10537 | 10537 | 10524 | 10526 |
| Ta096 | 200x 10 | 10326 | 10377 | 10357 | 10375 | 10330 |
| Ta097 | 200x10 | 10854 | 10908 | 10929 | 10868 | 10868 |
| Ta098 | 200x 10 | 10730 | 10798 | 10798 | 10751 | 10731 |
| Ta099 | 200x10 | 10438 | 10478 | 10465 | 10465 | 10454 |
| Ta100 | 200x 10 | 10675 | 10758 | 10727 | 10727 | 10680 |
| Ta101 | 200x 20 | 11195 | 11418 | 11468 | 11335 | 11280 |
| Ta102 | $200 \times 20$ | 11203 | 11488 | 11487 | 11517 | 11272 |
| Ta103 | 200x 20 | 11281 | 11559 | 11549 | 11481 | 11378 |
| Ta104 | 200x 20 | 11275 | 11465 | 11553 | 11405 | 11376 |
| Ta105 | 200x 20 | 11259 | 11444 | 11438 | 11374 | 11310 |
| Ta106 | 200x 20 | 11176 | 11421 | 11445 | 11335 | 11265 |
| Ta107 | 200x 20 | 11360 | 11593 | 11596 | 11438 | 11430 |
| Ta108 | 200x 20 | 11334 | 11597 | 11592 | 11530 | 11398 |
| Ta109 | 200x 20 | 11192 | 11457 | 11485 | 11439 | 11266 |
| Ta110 | 200x 20 | 11288 | 11567 | 11607 | 11499 | 11355 |
| Ta111 | 500x20 | 26059 | 26493 | 26420 | 26388 | 26187 |
| Ta112 | $500 \times 20$ | 26520 | 26953 | 26942 | 26714 | 26779 |
| Ta113 | $500 \times 20$ | 26371 | 26787 | 26729 | 26648 | 26496 |
| Ta114 | $500 \times 20$ | 26456 | 26817 | 26751 | 26656 | 26618 |
| Ta115 | $500 \times 20$ | 26334 | 26698 | 26643 | 26579 | 26500 |
| Ta116 | $500 \times 20$ | 26477 | 26874 | 26832 | 26666 | 26647 |
| Ta117 | $500 \times 20$ | 26389 | 26691 | 26609 | 26594 | 26529 |
| Ta118 | $500 \times 20$ | 26560 | 26913 | 26925 | 26711 | 26772 |
| Ta119 | $500 \times 20$ | 26005 | 26425 | 26326 | 26228 | 26223 |
| Ta120 | $500 \times 20$ | 26457 | 26905 | 26766 | 26695 | 26617 |

For the clarity of presentation, the benchmark set of Taillard was divided into two subsets. The first subset is named ST1 and contains the instances where the number of operations $<=100$. The second subset is named ST2 and contains the instances where the number of operations $>100$. Table 3 and Table 4 show BS obtained by the compared works on these two subsets

From Table 3 and Table 4, it can be seen that the performance of SSO deteriorates on this set. However, in order to provide a more thorough comparison, the one-way ANOVA test was applied on the $P E$ values over the whole set of instances. Figure 3 shows the results. From Figure 3, it can be noticed that MASC performs better than all the compared works. This is because MASC combines the complementary strengths of population-based (global search), constructive methods, and single-point (local search) methods. The four works can be sorted according to the resulting APE values from the best to the worst as follows: MAC 0,278 , HWA 0,460 , NS-SGDE 0,750 , SSO 1,268 . It can be also noticed that the resulting $p$-value is $3,83 \mathrm{E}-22$ which indicates that there is a statistically significant difference between the compared algorithms.

The deterioration of SSO performance on this set can be due to two reasons. First, Taillard's set is more difficult to solve than Reeves's set. Second, SSO didn't use any problem-specific operators or external single-point mechanisms. Therefore, it cannot intensify the search in the promising areas of the search space, i.e. the neighborhood of good solutions.


Figure 3. Means and 95\% confidence intervals on Taillard's set.

## 5. CONCLUSION AND FUTURE WORKS

In this work, SSO algorithm is proposed to solve the permutation flow shop problem with makespan minimization. The aim is to investigate the effectiveness of SSO in solving this combinatorial problem. The well-known benchmark sets of Reeves and Taillard were used for the evaluation. Six other conventional and best-so-far algorithms were used for the comparison. The computational results show that SSO outperforms three of them although they are hybrid methods. However, the results also show that it fails to compete with the best-so-far algorithms. This is due to the fact that the best-so-far approaches are memetic algorithms that combine the advantages of
population-based and single-point algorithms. Therefore, it is expected that SSO will perform very well if it is hybridized with a single-point algorithm, and this hybridization could be one of the future works of this research.

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