

International Journal of Informatics and Applied Mathematics e-ISSN:2667-6990 Vol. 5, No. 1, 1-26

# **Optimal Covert Communication Techniques**

Moses Oyaro Okello

#### mosesokellomoses@gmail.com

Abstract. Due to advancements in hacking and reverse engineering tools, threat against transfer of sensitive data or highly classified information is always at risk of being intercepted by an attacker. Covert communication outwits this malicious breach of privacy act better than cryptography as it camouflages secret information inside another innocent looking information, while cryptography shows scrambled information that might arouse attention of an attacker. However, the challenges in Steganography are the modification of carrier that causes some abnormalities, which are detectable and often the methods are not optimized. This paper presents an approach in Covert communication Chanel, which utilizes mathematical concept of combination to optimize time of transmission using sets of multiple transmitters, and receivers addresses where each abstractly represents a set of bits or characters combination without modifying the address. To minimize the number of physical address for use, a combination and permutation concept of virtual address generation from physical address is introduce. The paper in addition presents some technique like relationship and their application in both reenforcing resistivity against Steganalysis and generating combinations. Furthermore, a concept of dynamical clockwise and anti-clockwise rotation of combination over addresses after every transmission is introduced to improve on resistivity against Steganalysis. A simple test was performed for demonstrating relay address, combination and permutation concepts. Based on test results and analysis, the method is effective as expected and it is quite easy to use as it can be implemented in different platforms without much difficulties.

Keywords: Steganography  $\cdot$  Cryptography  $\cdot$  Algorithm  $\cdot$  Combination  $\cdot$  Permutation.

### 1 Background Studies

#### 1.1 Introduction

Information security threats come in many different forms. Some of the most common threats today are software attacks, theft of intellectual property, identity theft, theft of equipment or information sabotage, information extortion etc. In awake of increasing cyber warfare, threat against transfer of sensitive data or highly classified Information is always at great risk of being leak or tap by an attacker. These act is consider as breach of privacy act.

One of the solutions to this is through steganography which sample work is presented by Artz [1], Petitcolas [2] and Provos [3]. Steganography is define as the science of camouflaging secret data in a cover medium in order to produce a stego-medium in which the secret information is imperceptible to all except the recipient. Johannes Trithemus defined this as ?Covered writing presented in a paper by Por et el [4] and Por [5]. It hides a message inside another message without drawing any suspicion to others so that its intended recipient can only detect the message as explained in a paper by Changder et el [6].

Traditional steganography methods hide information in the Noise of the data by distorting original data, just enough to embed a message without this distortion being noticeable. While steganography hide the existence of a message, It is not enough to simply encipher the traffic, as criminals detect, and react to the presence of encrypted communications, But when information hiding is used, even if an attender tap the transmitted object, he or she cannot surmise the communication since it is carried in a hidden way. Limitation of cryptography is that the third party is always aware of the communication because of the unintelligible nature of the text or encrypted contents.

Steganography overcome this limitation by hiding message in an innocent looking object called carrier, cover, or stego-object. In addition, still attacker can be attracted towards encrypted data due to different form of data. Therefore, this limitation can be overcome by using steganography sample work presented by Kumar et el [7].

These is because in some organization or government may not allow encrypted communication by Bobade et el [8]. Therefore, steganography is the best suitable way for confidential communication in case of alarming needs for secret communication. Furthermore, Staganography is an ever-growing research topic as the idea of secret communication attracts many researchers by Seo et el [9]. Although steganography techniques provide us with some more secure communication, the modification is traceable by using some brand-new ?Steganalysis? tools such as the one by Yuan et el [10]. Good Steganography method when mixed with cryptography Ngo et el [11] and Sklavos et el [12] becomes nearly impossible to intercept encrypted contents. Steganography can be classified in many categories such as Network steganography, Image steganography, Audio, text, video etc depending on medium used for carrying hidden message. Network Steganography is preferred over other methods of steganography such as image steganography as image often might get modified or distorted during transmission. This is due to either image filtering, resizing, scaling, transformation or many others. This may distort the hidden information such that the final recipient may not get the right message. For example, Least Significant Bits (LSB) method is very vulnerable to image modification.

### 1.2 Paper Structure and Organization

This paper is structured in the following sections. Section 1: is mainly about background studies of the proposed topic, which comprises of some preliminary basic introduction in sub-section 1.1, about topics of security, cryptography and steganography. Sub-section 1.2 is about structure and organization of this paper to help reader easily know which section is about what before getting to read it. In addition, sub-section 1.3 discusses related work of the proposed topics, methodology, and some of the vulnerability steganography methods through steganalysis. Section 2: Cover the proposed methodology that is sub-divided into several sub-sections, each discusses smaller sub-program into details such as mathematical models and algorithm for automating some process like generating bits/character combination, automation rotation of array, program structural flow and many more. Section 3 is for testing/experiment of the proposed methodology, which attempt to show how the method works. Performance analysis of the methodology such as optimal performance analysis and security performance analysis are presented in section 4. Section 5 presents sample examples of the methodology and section 6 is about discussion and conclusions. Finally, references of related article cited in this manuscript are in section 7.

#### 1.3 Related Works

This sub-section introduces some few related work in the area of covert Communication channel and some method use for detecting those covert communication. In addition, how to overcome these steganalysis.

A paper presented by Sabeti et el [13], introduces two methods based on data packet length. In their first method, the sender encodes a bit of data in each pair that included two non-identical length and the second method where packets are separated into buckets. Only a packet within a bucket can be pairs as indicated by the authors. The drawback however is that the method is applicable in situation where packet length does not have a constant value. Furthermore, since the method relies on swapping of the packets for instance in their first method, it?s prone to being detected as a very small abnormality might be detected.

In addition, Lui et el [14], in their paper presented a method as they treats network traffic as a flow with fixed-length fragment, and calculates the histogram of the packet delays in each fragment. They modulate a message bits into the delays by binary coding method, while keeping the histogram almost unchanged by assigning the matched distribution. However due to advances in technology in the area of detecting hidden methods in the covert channel, there are several methods which do detect such small changes or modification of the network traffics flows. such as those presented by Steven Gianvecchio et el [15] which showed an entropy based method for detecting covert channel and also another one which detect word-base algorithmically generated Domains by using interword and inter-domains correlation using semantics analysis presented by Yang et el [16]. They took into account word embedding and some part of speech in addition to detecting using frequency distribution of words and part of speech.

Furthermore, a paper by Okello [17], and improved and extended version Okello [18] presented a method based on time interval or delays, which takes the interval of the time such as  $\delta t = t_i - t_{(i-1)}$ .  $\delta t$  Is then compared with chosen sequences of keys to decode or encode hidden binary. The improved based on TCP/IP status code and assigning alphabet to numeric of time from zero to fifty-nine. In addition, another method in the improvement encode in  $\delta t$  as explained in the paper. The paper further discusses the drawback of most steganography methods, which are due to modification of carrier, and that it gives loophole for some sophisticated algorithm or statistical method to detect steganography flow. Nevertheless, this problem can be solve in this proposed methods, which does not modify anything. In addition, the fact that most method hides a single bit one after another, it is extremely difficult to attained optimal transmission based on time for transmitting these many bits and this proposed method introduces bit/string and address combination and permutation techniques to overcome such problem.

## 2 Methodology

This paper presents theoretical mathematical approach in security (Network steganography), which utilizes mathematical concept of permutation of address and combination of binary and string, their concatenation. By combining bits to optimize time of transmission, using multiple transmitters and receivers addresses, for example email addresses, mail addresses, phone numbers, or network ports or addresses and many more where each is assigned bits combination. In addition, the paper presents the concept of dynamical clockwise and anti-clockwise rotation of bits combination over the given addresses after every transmission to reinforce resistivity against any form of security analysis like (Steganalysis) or cryptanalysis.

### 2.1 Program Structure flow and Main Stages

This section introduces some main stages in the design of the program from encoding phases to decoding phase. This stage does not include details design but only preliminary design showing main stages. For details including mathematical, algorithm etc. are included in each next sub-sections in section 2. Please see figure 1 on how to prepare and send covert information (info) based on the proposed method, which is further discussed in details in the next section of the paper. In the decoding or extraction phase, it?s expected that receiver have at hand list of addresses for both sender and receiver with their corresponding bit/character

5

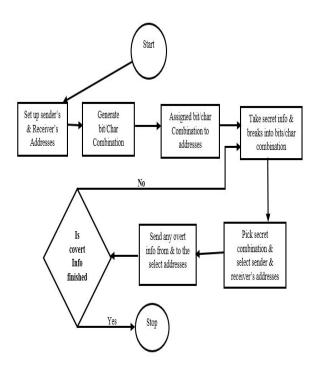


Fig. 1. Encoding/Transmission Phase for Covert Information (info)

combination address assigned to the addresses. For decoding phase, please see figure 2.

#### 2.2 Combination

This section presents the concept of combination of bits or characters such that maximum bits or characters can be send at once by making a given address represent such bit combination. Below shows examples of bits combination. In addition, how a formulae for calculating total number of possible bits or character combination "C" given that a number of bits or character to be combine is "n". Let W be set of string of possible combinations resulting from a given combinatorial such that  $W = \{w_0, w_1, w_2, w_3, ..., w_{(C-2)}, w_{(C-1)}\}$  and C is the total number of elements of W excluding empty set  $w = \{\phi\}$ .

Below indicates bit combination. For base element "w" of a set is defined as the initial member of set when number of combination is one n = 1 for instance for bits,  $w = \{0, 1\}$  One by one bit combination;  $w = \{0, 1\}$  so total combination are c = 2 and n = 1. However, for Two binary combination, the possibility are  $W = \{00, 01, 10, 11\}$  and total combination c = 2 where n = 2. For three binary combination,  $W = \{000, 001, 010, 100, 011, 101, 110, 111\}$  total combination  $C = 2^3$  where n = 3 For four binary combination are;  $W = \{0, 1\}$ 

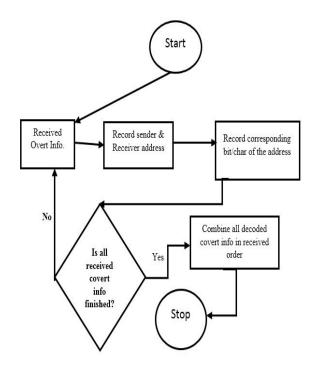


Fig. 2. Decoding/Receiving phase of Covert Information (Info)

 $\{0000, 0001, 0010, 0100, 1000, 0011, 0101, 1111, \ldots\}$  and total combination C=16 where n=4.

Therefore, the pattern keep on increasing such that the power of possible binary combination "C" for a given bit combination "n" can be express as  $C = 2^n$ . From the above, it is clearly evidenced that, for binaries combination, the maximum possible binary combination "C" is as below where "n" is the total number of binaries combination. given that  $W = \{w_0, w_1, w_2, ..., w_{(2^n-2)}, w_{(2^n-1)}\}$ . Total element of set W can be express as follows. We know that total elements (cardinality) of a base set w can be express as v = n(w).  $C = v^n$  For example  $w = \{0, 1\}$ , total elements of set w is two n(w) = 2, meaning binary or base two number system, so  $C = 2^n$ , for  $W = \{00, 01, 10, 11\}, C = v^n = n(W)$  Therefore C can be express as;

$$c = v^n \tag{1}$$

By using Kleene Star formulae by Ebbinghaus et el [19] derived from Kleene plus. Let Kleene plus be  $V^+$  and Kleene star be  $V^*$  Therefore,

$$V^{+} = \bigcup_{(n=1)}^{\infty} V_{n} \text{ implies that } V^{*} = \bigcup_{n \in N \cup \phi} V_{n}$$
(2)

 $V^+ = \{V_1 \cup V_2 \cup V_3 \cup \ldots \cup V_n\} \text{ In addition, given that, } V_0 = \phi \text{ an empty set and Kleene Star is given as } V^* = V_0 \cup V^+ \text{ therefore } V^* = \{V_0 \cup V_1 \cup V_2 \cup V_3 \cup \ldots \cup V_n\}.$ 

If  $V = \{"z", "y"\}$ , then  $V^* = \{\{\phi\}, \{"z", "y", "zz", "zy", "yz", "yy"\}$ ,  $\{"zzz", "zzy", "zyz", "zyy", ...\}$  If  $V = \{"x", "z", "y"\}$ , then

 $V^* = \{\{\phi\}, \{"x", "z", "y"\}", \{"xx", "xy", "xz"...\}, \{"xxx", "xxz", "xxy", "xzz", ...\}\}$ Now substituting z = 0, y = 1 as binary character of string, the above can be rewritten as below.

If V = 0, 1, then  $V^* = \{\{\phi\}, \{0, 1\}, \{00, 01, 10, 11\}, \{000, 001, 010, 011, ...\}, ...\}$ 

Given that,  $V_0 = \phi$  for any alphabet, the set of all strings over V of length n is denoted as  $V_n$ .

If  $V = \{"z", "y"\}$ , then  $V^* = \{\{\phi\}, \{"z", "y"\}, \{"zz", "zy", ""yz", "yy"\}, ...\}$ . Substituting that with binary bit of string, becomes  $V = \{0, 1\}$  then  $V^* = \{\phi, 0, 1, 00, 01, 10, 11\}$ .

For,  $V_1 = \{0, 1\}$ . and then the total element of the sets in  $V_1$  is given as  $C = 2, C = 2^1$ . However,  $V_2 = \{00, 01, 10, 11\}$ . and then the total element of the sets in  $V_2$  is given as  $C = 4, C = 2^2$  with the exception of the empty set  $V_0 = \phi$ . Therefore, the total is minus one. From above total summation of elements of sets of Kleene plus for a given "n" bits combination is. C Where  $C = v^n$  For more examples, see Table 1 where a binary combination is assign to addresses. Further, V' is defined as set of cardinality of all  $V_n$  so,  $V' = \{n(V_1), n(V_2), n(V_3), ..., n(V_n)\}$  therefore, for an example, if  $V = \{0, 1\}$  so  $V' = \{2^1, 2^2, 2^3, ..., 2^n\}$  where v = n(V) therefore  $V' = \{v^1, v^2, v^3, ..., v^n\}$ 

#### 2.3 Relationship

Given two sets of addresses A,B such that  $\{(a,b) : a \in A, b \in B\}$  and each element of one set is maximally relating to all the elements of the other sets and the inverse relationship holds true such that  $(A = \{a_0, a_1, a_2, ..., a_i\}: i \in N$  and  $B = \{b_0, b_1, b_2, ..., b_j\}: j \in N$ . The relationship of the two sets "A" and "B" can be describe as;  $R \subseteq AxB = \{(a, b) : a \in A, b \in B\}$ . For the inverse case where the receiver want to reply to the sender, the relationship inverse can be express as  $R^{(-1)} = (a, b) : (a, b) \in R$ . Therefore, x and q are total elements of sets A and B respectively.

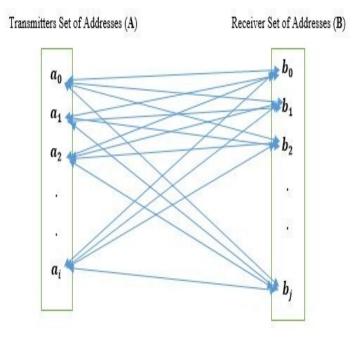
Therefore since the transmission is related, such that,  $a, b \in \Re$ , a  $\Re$  b, Maximum crossing or relationship among addresses "L" for sending information can be express as  $L = n(A) * n(B) \Longrightarrow 0 < L; L \in N$  Or L = n(A)n(B). In addition, to calculate total number of cross transmission is as L. Please see Figure 1 below for the address relationship involving only Transmitters and Receiver addresses. Below here, we classify different type of relationship based on total number of base elements and type of element of sets relating.

**Homogenous Relationship** A relationship involving two or more set where each of the set have same base size and same element type for example a given set  $V_0, V_1, V_2, ..., V_i$  and base set of  $n(V_1) = n(V_2) =, ..., n(V_i)$  and their relationship results in homogenous combination. For example, set V can be set of binary number, so  $V_1, V_2, ..., V_i$  are all binary set, and their base set of all are 0,1 So for an example, given  $v_1 = \{00, 01, 10, 11\}$  and  $v_2 = \{0, 1\}$ . Therefore, relationship

between  $\{v_1, v_2\}$  are homogenous and produces homogeneous combination  $v_3 = \{000, 001, 010, 100, 011, 101, 110, 111\}$ 

**Non-Homogenous relationship** relationship involving two or more sets where each of the set have different base size and different element types for example a give set  $\{v_1, v_2, ..., v_i\} \notin V$  and base set of  $(v_1) \neq (v_2) \neq ..., v_i$  and their relationships results in non-homogenous combination. For example set V can be set of mixture of number, character etc.  $\{v_1, v_2, ..., v_i\}$  their base set of all are different. For example  $v_1 = \{0, 1\}, v_2 = \{x, y, t\}, v_3 = \{0, d, P\}, ...$  So for more example, given  $v_1 = \{00, 01, 10, 11\}$  and  $v_2 = \{x, y, z\}$  so, the results is  $v_3 = \{00x, 01x, 10x, 11x, 00y, 01y, 10y, 11y, 00z, 01z, 10z, 11z\}$  Therefore, relationship between  $\{v_1, v_2\}$  are non-homogenous and produces non-homogeneous combination.

**Transmitters to Receivers Address Relationship** Please see figure 3 for relationship without relay address directly from sender to recipient address without intermediate address.



 ${\bf Fig.~3.}$  Shows Relationship Transmitter and Receivers Addresses

**Transmitter's Receiver's Address Relationship with Relay Addresses** Below Figure 4 shows, relationship-involving relay addresses where multiple relay addresses as intermediate address before final destination address.

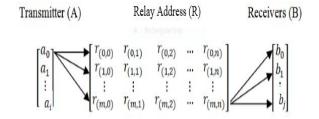


Fig. 4. Shows Relationship Involving Relay Addreses

$$L = f_0 * f_1 * f_2 * \dots * f_n \tag{3}$$

$$d = f_0 + f_1 + f_2 + f_3 + \dots + f_n \tag{4}$$

In Equations (3) and (4),  $f_i = n(r_i)$  and  $n(A) = f_0, n(B) = f_n$  from figure 2 In addition, d is the total number of address involve in relationship from both sender to receiver as well as relay addresses inclusive if at all there is any.

#### 2.4 Maximization of Address

Here, an idea of how to maximize total number of address based on concept of combinatorial and permutation to produce more virtual addresses. This approach is based on an idea that given a set of address (A) with more than one distinct element i.e. $n(A) \ge 2$ , a given combination of virtual address can be generated. For example. Given address such as  $A = \{a, b, c\}$ , virtual address A'can be generated using combination techniques like  $A' = \{ab, ac, bc, abc\}$  and for permutation like  $A' = \{ab, ba, ac, ca, bc, cb, abc, acb, bca, bac, cab, cba\}$ . These are all distinct elements. Although some are virtual and others are real addresses has generated four virtual addresses and in total seven new addresses are available for use when using combination concept, However, for permutation, twelve virtual addresses are generated from three real physical addresses.

**Combination of Addresses** For combination nCr of , to generate virtual address, order of virtual address combination does not matter as transmission is simultaneous, so indexing address is difficult if order of address combination is

to be taken into account such as in permutation. For an address with two real elements, virtual addresses can be generated as  $A = \{a, b\}$  where virtual addresses are  $A' = \{ab\}$ . only one distinct virtual address element can be generated. So formulae for finding total elements of virtual address A' i.e. n(A') based on combination technique that can be used from a given real address A is shown here in Equation (5) where x number of real address total is n(A) and u is Combination  ${}_{x}C_{r}$  of address, r is the selected address in combination. Please note the (s.t)means subject to

$$u = \frac{x!}{r!(x-r)!}, \quad s.t0 \leqslant r \leqslant x \tag{5}$$

Unlike permutation, in combination order of elements or their arrangements does not matter. For instance, ab is the same as bc. Moreover, for three elements, such as abc is the same as acb,cab,bca,bac,cba, etc. So total virtual addresses generated from real distinct address can be as below in Equation (6)

$$n(A') = \sum_{r=2}^{x} \left( \frac{x!}{r!(x-r)!} \right)$$
(6)

However, for the total elements of real and virtual addresses see Equation(7) also known as Grand address G.

$$G = \sum_{r=1}^{x} \left( \frac{x!}{r!(x-r)!} \right) \tag{7}$$

$$G = n(A) + n(A') \tag{8}$$

When (r = x) so equation (5) equals one. In addition, when (r = 1) therefore, equation (5) equals (x) or n(A). So equation (7) can be rewritten as in (9)

$$G = (x+1) + \sum_{r=2}^{x-1} \left( \frac{x!}{r!(x-r)!} \right)$$
(9)

Total possible Relation L from (3) involving virtual addresses generated from combination in (2) can be express as in (10)

$$L = \left( (x_0 + 1) + \sum_{r=2}^{x_0 - 1} \left( \frac{x_0!}{r!(x_0 - r)!} \right) \right) \left( (x_0 + 1) + \sum_{r=2}^{x_1 - 1} \left( \frac{x_1!}{r!(x_1 - r)!} \right) \right)$$
(10)

For relationship involving relay addresses, please see equation (11). In addition, for i = 0 represent address A transmitter for i=n represents Address B Receiver, for  $0 \leq i \leq n$  represent relay addresses.

$$L = \prod_{i=0}^{n} \left( (x_i + 1) + \sum_{r=2}^{x_i - 1} \left( \frac{x_i!}{r!(x_i - r)!} \right) \right)$$
(11)

For address can be express as in Equation (12)

$$d = \left( (x_0 + 1) + \sum_{r=2}^{x_0 - 1} \left( \frac{x_0!}{r!(x_0 - r)!} \right) \right) + \left( (x_1 + 1) + \sum_{r=2}^{x_1 - 1} \left( \frac{x_1!}{r!(x_1 - r)!} \right) \right)$$
(12)

However, for address involving relay address please see Equation (13)

$$d = \sum_{i=0}^{n} \left( (x_i + 1) + \sum_{r=2}^{x_i - 1} \left( \frac{x_i!}{r!(x_i - r)!} \right) \right)$$
(13)

**Permutation of Addresses** In permutation, the order combination of physical address forming virtual address does matter very much because transmissions are sequential not simultaneous, and it is time index i.e. ab is different from ba. So two or more address combination representing one virtual address can be re-arrange in such a way that the order of those address distinctively represents different address. For example, transmissions from physical address a and b can be from the virtual address ab transmission received at  $t_0$  and  $t_1$  respectively given that  $t_0 = t_1$ . For virtual address ba transmission received at  $t_0$  and  $t_1$  respectively given that  $|t_0 - t_1| \leq \gamma$ . Where  $\gamma$  is set limits for different between two received transmission and if the is less than ?, means transmission from a given permutation, else different transmissions, time of transmission from the same combination should be within a defined range ?t or ?t see Equation (14). Where  $\omega$  values set such that  $\Delta t \leq \gamma$ 

$$\Delta t = t_i - t_{i-1} \tag{14}$$

From equation (5), permutation, nPr of such combination is the permutation of entire virtual address plus physical address generated from combination can be written or express in Equation (15).

$$G = \sum_{r=1}^{x} \left( \frac{x!}{(x-r)!} \right) \tag{15}$$

Where x is total number of address and r number of address chosen. Just like in Equations (10 to 13) total relationship and addresses involving relay addresses can be written as in Equation (16) and (17).

$$L = \prod_{i=0}^{n} \left( \sum_{r=1}^{x_i} \left( \frac{x_i!}{(x_i - r)!} \right) \right)$$
(16)

$$d = \sum_{i=0}^{n} \sum_{r=1}^{x_i} \frac{x_i!}{(x_i - r)!}$$
(17)

Please note: handling zero factorial in address here is when its zero. Zero factorial is defined as a mathematical expression for the number of ways to arrange a data set with no value in it, which equals one by definition (0! = 1). So, for this address, since total number of address is greater than zero, so  $r \ge 0$  so (r) much be greater than zero.

#### 2.5 Concatenation

The concept of concatenation is mainly use in formal language theory like in programming languages and pattern. Concatenation of two strings a and b is often denoted as ab, a||b, or, in the Wolfram Language, a <> b Weisstein et el [20]. However, throughout this text, it is denoted as  $a \parallel b$ . From the two sets of strings of binary assigned to addresses A and B, the concatenation  $A \parallel B$  consists of all strings of the form  $a \parallel b$  where "a" is a binary string from A and "b" is a string from B, or formally  $A \parallel B = a \parallel b : a \in A, b \in Bf$  or concatenation of a string set and a single string, and vice versa.  $A \parallel b = a \parallel b : a \in A$  and  $a \parallel B = a \parallel b : b \in B$ . However, as given by the work of Weisstein et el [20], the concatenation of two or more numbers is the number formed by concatenating their numerals. He gave an example, the concatenation of 1, 234, and 5678, which are 12345678. In addition, the value of the result depends on the numeric base. He further presented the formula for the concatenation of numbers p and q in base  $\beta$  as in Equation(18).

$$p \parallel q = p\beta^{l(q)} + q \text{ where } l(q) = \lfloor \log_{\beta} q \rfloor + 1$$
(18)

l(q)Is the number length of "q" in base " $\beta$ " and  $\lfloor x \rfloor$  is the floor function. The above work well when "p" is a non-floating point number or number without decimal point like p=23,p=12 etc but for floating point number like p=5.56,q=34.03, etc., it yield different result when compared with a number concatenation treated as string. In addition, numbers with zero in front like for example q=0045, q=034, q=00018, yield less floor function not as intended as zero before a number is disregarded unless it is before a decimal point. Therefore, throughout this paper, binaries, or stream of bits are treated as string and string concatenation formulae and rules/law are applied as below.

#### 2.6 Associative Law

Rules of Binary operation applicable to string Concatenation are presented here below. For the binary operation, is associative and repeated application of the operation produces the same result regardless of how valid pairs of parenthesis are inserted in the expression. A product of two elements (addresses or bits combination)  $((a,b) : a \in A, b \in B)$  may be written in five possible ways as below.  $1.((a||b)||a)||b \ 2.(a||b)||(a||b) \ 3.(a||(b||a))||b \ 4.a||((b||a)||b) \ 5. a||(b||(a||b))$ Since the product operation is associative, the generalized associative law says that all these formulas will yield the same result, making the parenthesis not relevant. Thus, "the" product is as below: a||b||a||b For example involving bits combination, Binary concatenation and port assignment, for four by four bits, combination and concatenation see Table 1.

Given time series of transmission, as  $T = t_0, t_1, t_2, ..., t_n$  such that  $(t_n > t_n - 1) > t_n - 2 > t_n - 3 > ? > t_1 > t_0)$  By defining sender to receiver order as  $O_{SR}$  and receiver to sender order as  $O_{RS}$  Therefore from sender to receiver order  $O_{SR} = (a||b)_{t_0}||(a||b)_{t_1}||(a||b)_{t_2}||...||(a||b)_{t_n}$  And from receiver to

13

Sender Addresses	Sender's Bits	Receiver Addresses	Receiver's Bit
$a_0$	0000	$b_0$	0000
$a_1$	0001	$b_1$	0001
$a_2$	0010	$b_2$	0010
$a_3$	0100	$b_3$	0100
$a_4$	1000	$b_4$	1000
$a_5$	0011	$b_5$	0011
$a_6$	0110	$b_6$	0110
$a_7$	1100	$b_7$	1100
$a_8$	1001	$b_8$	1001
$a_9$	0101	$b_9$	0101
$a_{10}$	1010	$b_{10}$	1010
$a_{11}$	0111	$b_{11}$	0111
$a_{12}$	1110	$b_{12}$	1110
$a_{13}$	1101	$b_{13}$	1101
$a_{14}$	1011	$b_{14}$	1011
$a_{15}$	1111	$b_{15}$	1111

 Table 1. Four by four bit combination assigned to addresses

sender order  $O_{RS} = (b||a)_{t_0}||(b||a)_{t_1}||(b||a)_{t_2}||...||(b|a)_{t_n}$  Above is an example of bit combination in table form shown in Table 1 based on combination concept, to send letter 'H'=01101001, it can be separated into two 4 by 4 bits combination and sent at once in a single transmission so that each transmission carries one character of 8-bits (1byte) For reply,

$$O_{SR} = (a_6||b_8)_{t_0} \Rightarrow a_6||b_8 = \underbrace{01101001}_{b_6||a_8}$$
$$O_{SR} = (b_6||a_8)_{t_0} \Rightarrow b_6||a_8 = \underbrace{01101001}_{b_6||a_8}$$

Application of Relationship for Generating Combination From the rule of string concatenation given above. Algorithm 1: below shows an automatics generation of bits/character combination based on Homogenous Relationship In sub-section 2.3.1 for an example shown in Table 1 above. This is using computer code and output is shown in figure 5. Please note from the above algorithm 1, function Array\_size(x,y) is for pre-allocation of array x of size y however in some programming language, array size are allocate dynamically and use of this function is not needed. See Figure 5 for example of above algorithm 1 testing. Algorithm 2: below shows an automatics generation of bits/character combination based on non-Homogenous Relationship In sub-section 2.3.2. This is using computer code and output is shown in figure 6 Algorithm 2 for input two relationship with non-homogenous see output in Figure 6

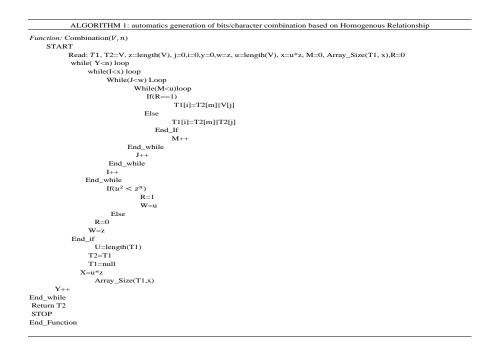




Fig. 5. Shows Output of Algorithm 1

ALGORITHM 2: Automatics generation of bit/char combination based on non-Homogenous Relationship

```
Function: Combination(V1, V2)

START

Read: h=0, i=0, j=0; C_1 = lengtht(V1) C_2 = length(V2), temp

while(i < C_2) loop

while(j < C_1) loop

j=j+1

temp[h]= V2[i]|| V1[j];

h=h+1;

end_while

i=i+1

end_while

Return temp

STOP
```



Fig. 6. Shows Output of Algorithm 2

#### 2.7 Rotation over Addresses

Let W represent sets of bit combination over given set of addresses, for instance A, or B. for subscribe of  $W_I$  "I" is the current position of bit combination over a given addresses A or B of index I, and "J" represent total transmission time such that  $(I \in N, J \in Z)$ . In addition, Q is the maximum addresses  $(Q \in N)$ or in other word, totals elements of set A or B for example if  $w_2 = a_2 = b_2$ Given a bit combination, "C" can rotate over elements of either set A or B after every transmission such that the rotation is either clockwise or anti-clockwise.  $A = \{a_{Q-1}, a_{Q-2}, ..., a_2, a_1, a_0\}$  or  $B = \{b_{Q-1}, b_{Q-2}, ..., b_2, b_1, b_0\}$  so W can be express as  $W = \{w_{Q-1}, w_{Q-2}, ..., w_2, w_1, w_0\}$  Below is the general equation, and conditions for the rotation in the positive direction or clockwise direction and Negative or anti-clockwise direction. See Equations (19) and (20) respectively. Let modular (mod) or remainder operator for dividing a number by another is  $(mod = \emptyset)$  to avoid confusing mod with other letter symbols presented here in the paper. For instance, A mod B=R can be express as  $A \oslash B = R$  or 5 mod 4=1 can be written as  $5 \oslash 4 = 1$  see Algorithm and 4 of (19) and (20). Positive (Clockwise) Rotation

$$f(J, W, Q, I) = \begin{cases} W_{I+J}, & 0 \leq J < Q : (I+J) < Q \\ W_{(I+J) \oslash Q)}, & 0 \leq J < Q : (I+J) \geqslant Q \\ W_{(I+(J \oslash Q)) \oslash Q}, & J \geqslant Q : (I+(J \oslash) Q \geqslant Q \end{cases}$$
(19)

Negative (Anti-Clockwise) Rotation

$$f(J, W, Q, I)^* = \begin{cases} W_{I+J}, & -Q < J \leq 0 : (I+J) \ge 0\\ W_{(I+J)+Q)}, & -Q < J \leq 0 : (I+J) < 0\\ W_{I+(J \oslash -Q)}, & J \leq -Q : (I+(J \oslash -Q)) \ge 0\\ W_{(I+(J \oslash -Q))+Q}, & J \leq -Q : (I+(J \oslash -Q)) < 0 \end{cases}$$
(20)

Algorithm 3 Shows code written to automate generation of index in an array for rotation based on Equation 19. See figure 7 for sample output. For result of above algorithm 3, see figure 7 From figure 5: initial Position is seven and total addresses are sixteen Initialization of variables. Algorithm 4 Shows code written to automate generation of index in an array for rotation based on Equation 20. See figure 8 for sample output. Below are data from the above algorithm 8. In addition, initial Position is five and total addresses are sixteen

#### 2.8 Application of Rotation Functions to Rotate Array of String

Below Algorithm 5 is pseudo-code created functions that uses the above two function in algorithm 3 and algorithm 4 for rotation, to rotate array of string. Since stream of bits (binary) are treated as string, so it can be converted into it subsequence array and the array index manipulated such that it is rotated as prescribe above. The idea creates two functions where each is input initial index I,J,Q and the function returns a numeric index after rotation for each element of the array. Furthermore, another function which call the two rotation function

ALGORITHM 3: Clockwise rotation of Array index of bit/char based on equation 19	
$Q;p;I;J;W_t;$	
for J from 1 to p loop	
if J>=0&& J <q td="" then<=""><td></td></q>	
if $(I+J) \ge Q$ then	
$T_J \leftarrow ((I+J \oslash Q))$	
else	
$T_{I} \leftarrow (I+J)$	
endif	
else	
$if((J \oslash Q)+I) \ge Q$ then	
$T_{I} \leftarrow (((I \oslash Q) + I) \oslash Q)$	
else	
$T_I \leftarrow (J \oslash Q) + I$	
endif	
endif	
endloop	

Data of Clockwise Rotation

8 9 10 11 12 13 14 15 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 0 1 2 3 4 5

Fig. 7. Shows Data for Clockwise Rotation

ALGORITHM 4: Array for Anti-clockwise rotation based on formulae 2.40

$Q;J;I;i;P;W_t;$
for i from 1 to P loop
J←(-i)
if J>-Q&&J<=0 then
if $(I+J)>=0$ then
$T_i \leftarrow (I+J)$
else
$T_i \leftarrow ((I+J)+Q)$
endif
else
$if(I+(J\bigcirc-Q))>=0$ then
$T_i \leftarrow (I+ (JO-Q))$
else
$T_i \leftarrow ((I + (J \oslash -Q)) + Q)$
endif
endif
endloop

Dat	a of A	Antio	clock	wise	Rotat	tion																	
4	3	2	1	0	15	14	13	12	11	10	9	8	7	6	5	4	3	2	10	15	14	13	12
11	10	9	8	7																			

Fig. 8. Shows Data for anticlockwise Rotation  $\$ 

19

is created which determines the value of J Where if it is negative, it calls anticlockwise rotation in Algorithm 4, else it calls clockwise rotation Algorithm 3, and the function returns array of all string after its rotation. See Fig 9 for the output of the algorithm 5 being tested. The algorithm 5 is about automation of rotation of bits or character combination over address. The figure below see Fig

Function:clockwise(I,J,Q)	character combination over address.
START	
read: I, J, Q ;	
if (J>=0&& J <q) th="" then<=""><th></th></q)>	
if ((I+J)>=Q)then	
$T=(I+J) \oslash Q$	
else	
T=(I+J);	
end_if else	
if(( $(J \oslash Q) + I$ )>=Q) then	
$T=(((J \oslash Q)+I) \oslash Q);$	
else	
$T=(J \oslash Q)+I;$	
end_if	
end_if	
return T;	
STOP	
Function: Anti_clockwise(I, J,Q)	
START	
read: I, J, Q	
if (J>-Q &&J<=0) then if ((I+J)>=0) then	
T=(I+J);	
else	
T=((I+J)+Q);	
end_if	
else	
if ((I+(JØ-Q))>=0) then	
$T=(I+(J\oslash -Q));$	
else	
$T = (I + (J \oslash -Q) + Q);$	
end_if	
return T;	
STOP	
Function: Rotation(W, Q, J)	
START	
Read:I=0;W = { $w_0, w_1, w_2 \dots w_{Q-1}$ }; J.	
While( I <q) loop<="" td=""><td></td></q)>	
if(J<0)	
R[Anti_clockwise(I, J, Q)] = W[I];	
else	
R[clockwise(I, J, Q)] = W[I];	
$m_{ij} = m_{ij}$	
I++;	
end_while	
return R:	
STOP	

9 which display results after rotating array string of addresses

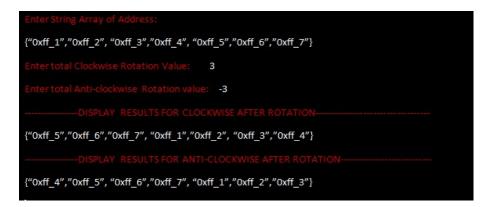


Fig. 9. Shows Clockwise and Anti-clockwise Rotation

## 3 Test and Result

In this section, three experimental/test results are presented where the first one is done in a very simple environment to make it easily understandable by nonspecialist in covert channel communication and easy to perform the experiment. It is based on the idea of using many phone numbers from two different locations where the confidential information is to be transmitted from and to a given location with those numbers representing the address. The second experiment was done using multiple Electronic mail (e-mail) located in given sender place and information is to be send to another location where recipient is located. In the recipient location are located multiple Electronic mail (e-mail). Through this, use of email forwarding functionality and rotation technique is used.

### 3.1 Test Result Based on Rotation

In this, at the sender side, six phone numbers was set up as sender addresses and receiver side six phone numbers also was set up as receiver addresses. At sender side, only two bit combination were used and the same four at the receiver side. See Table 2 To withhold the identity of the users phone number from exposing,

Sender phone	Bit combination	Receiver Phone	Bit combination
+256-788-011	00	+256-789-001	Null
+256-789-081	Null	+256-777-222	00
+256-711-022	01	+256-772-412	10
+256-777-187	10	+256-777-011	01
+256-772-101	Null	+256-772-111	11
+256-777-787	11		

Table 2. Phone number at sender and receiver assigned bit combination

only six digits are shown without their location of calls only just labeled as sender and receivers location. Furthermore an extra phone number is used in addition to the one assigned bit combination, those phone number are label as null which means it does not carries any bit combination and any phone called from or to such carries no bit combination whether it is directed to the one with assigned bit combination see Table 2 for more details. The following phone calls were recorded at receiver sides with their respective time of call see Table 3 From

Table 3. Extracted time of calls from phone number

Sender phone	Receiver Phone	Time of call	Extracted Bit Combination
+256-711-022	+256-772-412	09:39	(null-01)
+256-772-101	+256-772-111	09:40	(01-null)
+256-777-187	+256-772-111	10:53	(00-00)
+256-788-011	+256-772-412	10:59	(01-00)
+256-777-787	+256-772-111	11:28	(00-11)
+256-777-18	+256-777-011	11:29	(10-11)

table 3, the extracted bit combination can be concatenated excluding the any combination from null phone number (Null-01)+ (01-null) + (00-00) + (01-00) + (00-11) + (10-11) Therefore, the stream of bits is (0000010000111011)

### 3.2 Test Result 2 Based on Relay Address and Permutation Without rotation

Here from the email address sender, send an open message to recipient via relay email by forwarding the email. Please see table 4 below contains sample email for transmission through relay address. To withhold the identity of email address involved in this practically, notation is use to represent email address such as A1@email.com. In Table 4 The following message were recorded from the above

Sender Email	Bits	Relay Email	Bits	Receiver	Bits
A1	00	R1	00	B1	00
A2	01	R2	01	B2	01
A1A2	10	R1R2	10	B1B2	10
A2A1	11	R2R1	11	B2B1	11

Table 4. Number of Email address with email forwarding as relay address

emails address in the order (A2-R2 R1-B1)+ (A1-R2-B1 B2) + (A2-R1-B2 B1) + (A1 A2-R1-B2) decoding this into binary (011100000110010011010001)

### 4 Analysis

Since this combine bits/character such that two or more bit can be send at once, so time of transmission reduces significantly, as many bits can be send at once and not sequential. Let "t" be time required for sending total of n bit or character combination for both relay and or without relay address at once. In addition, "k" is a constant unit time per one-bit transmission such that;  $nt\infty k \Rightarrow nt = k$  and  $t = \frac{k}{n}$ 

$$t = k\eta^{-1} \tag{21}$$

Therefore  $\lim_{\eta \to \infty} \left( t = \frac{k}{\eta} \right) \approx 0$ ; given that k=1 From the above, it is evidence that when number of bits combination increases, so does time required for transmission reduces.

#### 4.1 Secure Analysis Using Probability

This section shows how resistive the method is from someone or a program that need to detect it by applying probability theory. Probability without Relay Address Let sample space be  $\tau$  for a total address at either sender or receiver's side where a bit combination can occupy at a given time. Therefore, the probability that a chosen bit combination occupy such address is as below:probability  $(P) = \frac{1}{\tau} | \tau = n(A), \tau = n(B), \Longrightarrow P = \frac{1}{\tau}$ . For the probability that it is not is given as  $P' = (1 - \frac{1}{\tau}) \lim_{\tau \to \infty} (1 - \frac{1}{\tau}) \approx 1$  However, the probability that a chosen transmission line carries the right bits combination is different from above as the sample space is from equation and equal to maximum crossing, a combination of bits between sender and receiver's addresses probability  $(P) = \frac{1}{L}$  Probability that it is not, is given as P' = (1 - P). For instance, if  $L = \frac{1}{n(A)n(B)}$  substitute in the above probability equation.

For instance, if  $L = \frac{1}{n(A)n(B)}$  substitute in the above probability equation.  $\sum_{L\to\infty}^{\prime} (1-\frac{1}{L}) \approx 1$  This indicates that, increase in number of bit combination n", makes probability  $P' \approx 1$  Probability with Relay Address In this part, we shows the probability that a chosen line of transmission from sender to receiver through relay addresses are as below, it's an expansion of the probability for a chosen line transmission above. Here find the probability within each relay from the sender up to receiver. Consider the following:  $A - R_1 - R_2 - R_3 - \ldots - R_m - B$  From transmitter address A to relay address  $R_1$  the probability that the line carries hidden information is  $p_A$  else the probability that it does not carries is denoted as  $p'_A$  for the next node of relay address it is given as  $p_{R_1}$  and  $p'_{R_1}$  respectively this continues up to the last point of receiver. Overall probability P that the entire transmission carries hidden message involving relay addresses can expressed as an independent probability which is the product of all individual probability by Stephanie Glen [21] and express as below (22):

$$P = (p_A)(p_{R_1})(p_{R_2})...(p_{R_m})$$
(22)

In addition, the probability that it does not carries is given as Equation (22)

$$P' = (P'_{A})(P'_{R_{1}})(P'_{R_{2}})...(P'_{R_{m}})(P'_{B})$$
(23)

From above it can be noted that as more relay address is added, the probability that a chosen line of transmission caries hidden information tend to almost zero proving theoretically that this approach is good.

### 5 Sample Example

Example 1: Given a bits combination n=3 after J=11 times of transmission in clockwise rotation. In addition, an initial position of the bits I=3.

a) What is the new position of the bits combination  $W_3$ ? Solution: Therefore:

$$Q = 2^{3}?n = 3andQ < Jf(J, w, n.I) = W_{(J \otimes 2^{n}) + I}, J \ge 2^{n}f(J, w, n.I) = W_{(11 \otimes 2^{3}) + 3}f(J, w, n.I) = W_{6}(J \otimes 2^{n}) + 2^{n}f(J, w, n.I) = W_{6}(J \otimes 2^{n}) + 2^{n}f(J \otimes 2^{$$

The new position or index is six (6). So if on sender addresses is  $a_3$  to  $a_6$  or for receiver address, it is from  $b_3$  to  $b_6$ .

b) Assuming after example 1, and rotating in anti-clockwise for 19 times transmission. What is the new position of the bits? Solution: Therefore:  $Q = -2^3$ ; n=3 and  $J \leq -Q$  and position I=6 is a new

position after clockwise rotation. And since anti-clockwise, J=-19

$$f(J, w, n, I) = W_{(J \otimes -2^n) + I}, J \leq -2^n$$

$$f(J, w, n, I) = W_{(-19 \otimes -2^3)+6}$$

 $f(J, w, n, I) = W_{-3+6=3}$  So new position = 3 The new position or index is six (6). So if on sender addresses is  $a_6$  to  $a_3$  or for receiver address, it is from to  $b_3$ .

Example 2: A person want to send a hidden message by post office mail, from country "A" to country "B" using 8-bits binary system such that the mail carries normal message without being modified:

a) How many mail addresses are requires from sender and receiver country so that at least each mail sent carries a character of 8-bits?

Solution: This can be separated into two 4 by 4 bits where n=4 see Table 1 for reference, such that at sender carries 4-bits and receiver's carries 4-bits. Given total address is d = n(A) + n(B) and substituting it with  $n(A) = n(B) = 2^n d = 2^n + 2^n 2 * 2^4 = 16 + 16 = 32$  addresses. Thirty-two addresses, sixteen mail addresses at both sender and receiver's side. From Table 1 As a references for the initial bit combination position for both address at sender and receiver's, what is the new position of the bits such that at sender address, bits are rotated clockwise while at the receiver's address, bits are rotated anti-clockwise? Sender wants to send a word of 50 characters ending with character 'o'. Solution: 8-bit for letter "o"=01101111 breaking into 4 by 4 its 0110 and 1111

- 24M.O Okello
- b) From Table 1, initial position of  $0110 = a_6 = 6$  and for  $1111 = b_{15} = 15$ . Sender side Rotation Clockwise.

I=6, Q=C=16, J=50 times.

$$f(J, w, n, I) = W_{(J \oslash Q) + I}, J \ge Q; (J \oslash Q) < Q$$

So,  $f(J, w, n, I) = W_{(50 \otimes 16) + 7) = W_9}$  new position = 8 Receiver side Rotation Anti-Clockwise. I=15, Q= -C=-16, J=-50 times.

$$f(J, w, n, I) = W_{(J \oslash Q) + I)}, J \leqslant -Q; (J \oslash Q) < 0$$

 $Sof(J, w, n, I) = W_{15-(-50-16)} = W_{(15-2)}$  new position = 13 Overall position for the bit combination over address after 50 times transmission bits rotation is as below: from  $(a_6||b_15)to(a_8||b_13)$ .

c) What is the percentage reduction in time of transmitting the bits? Solution:

 $t = \frac{k}{2n}$ ; n = 4, k = 1. Time of transmission percentage decrease  $\frac{1}{(2*4)}$ 0.125 percentage.

What is the probability that a chosen address contains the right bits combination given that total bits combination n = 4? Solution:

Sample spaces (total addresses over which a bit combination can occupy is as below)  $C = n(A) = 2^n; n = 4 \Longrightarrow n(B) = 2^4 = 16$   $Probability = \frac{1}{n(B)}; n(B) = 2^n \Longrightarrow \frac{1}{2^n} = \frac{1}{60} = 0.0625.$ 

How many address and bit combination is required such that each mail sent carries two characters of 8-bit system at once or at a single transmission? Solution:

Total bits for two character implies one-character at sender and another one at receiver side At sender and receiver each, need a total of n = 1 \* 8 = 8bitscombination Bit combination is given  $C = 2^n$ ;  $n = 8 \implies 2^8 = 256 - bits$ combination and addresses needed at both side of sender and receiver

#### 6 Conclusion

Base on proves, examples, test results and analysis, it is practically difficult to detect hidden information flow. Decrypting hidden message is extremely hard as nothing modifies like in most steganography methods, which involve modification of the carrier. Besides that, due to the rotation of bits, characters or strings combination over given addresses after every transmission, make it difficult to decipher hidden contents, In addition, the use of methods such as relay address, homogenous and non-homogenous combination further strengthen this methods in term of security and optimal performance. Lastly, by using combination and permutation technique enable transmitting many bits/character at once, unlike in some methods where a single bit is transmitted one after another and it allows used of fewer physical addresses as more virtual addresses are generated and used. In addition, combination technique allows generation of many

virtual addresses from few physical addresses hence reducing number of physical addresses in use also improving on security. However transmission is based on multiple Sender-receiver's addresses, it should be sequential not simultaneous to avoid confusion.

### References

- 1. Artz, D. (2001). Digital steganography: hiding data within data. IEEE Internet computing, 5(3), 75-80.
- Petitcolas, F., Anderson, R., & Kuhn, M. (1999). Information Hiding?A Survey: IEEE Special Issue on Protection of Multimedia Content.
- Provos, N., & Honeyman, P. (2003). Hide and seek: An introduction to steganography. IEEE security & privacy, 1(3), 32-44.
- 4. Por, L. Y., & Delina, B. (2008, April). Information hiding: A new approach in text steganography. In WSEAS international conference. Proceedings. Mathematics and computers in science and engineering (Vol. 7). World Scientific and Engineering Academy and Society.
- Por, L. Y., Ang, T. F., & Delina, B. (2008). Whitesteg: a new scheme in information hiding using text steganography. WSEAS transactions on computers, 7(6), 735-745.
- Changder, S., Ghosh, D., & Debnath, N. C. (2010, November). Linguistic approach for text steganography through Indian text. In 2010 2nd international conference on computer technology and development (pp. 318-322). IEEE.
- Kumar, A., & Pooja, K. (2010). Steganography-A data hiding technique. International Journal of Computer Applications, 9(7), 19-23.
- Bobade, S., & Goudar, R. (2015, February). Secure data communication using protocol steganography in IPv6. In 2015 International Conference on Computing Communication Control and Automation (pp. 275-279). IEEE.
- Seo, J. O., Manoharan, S., & Mahanti, A. (2016, July). Network steganography and steganalysis-a concise review. In 2016 2nd International Conference on Applied and Theoretical Computing and Communication Technology (iCATccT) (pp. 368-371). IEEE.
- Yuan, C., Xia, Z., & Sun, X. (2017). Coverless image steganography based on SIFT and BOF. Journal of Internet Technology, 18(2), 435-442.
- Ngo, H. H., Wu, X., Le, P. D., Wilson, C., & Srinivasan, B. (2010). Dynamic Key Cryptography and Applications. Int. J. Netw. Secur., 10(3), 161-174.
- Sklavos, N. (2014). Book Review: Stallings, W. Cryptography and Network Security: Principles and Practice: Upper Saddle River, NJ: Prentice Hall, 2013, 752p, 142.40. ISBN: 13: 978-0133354690.
- Sabeti, V., & Shoaei, M. (2020). New High Secure Network Steganography Method Based on Packet Length. The ISC International Journal of Information Security, 12(1), 24-44.
- Liu, G., Zhai, J., & Dai, Y. (2012). Network covert timing channel with distribution matching. Telecommunication Systems, 49(2), 199-205.

- 26 M.O Okello
- Gianvecchio, S., & Wang, H. (2007, October). Detecting covert timing channels: an entropy-based approach. In Proceedings of the 14th ACM conference on Computer and communications security. (pp. 307-316).
- Yang, L., Zhai, J., Liu, W., Ji, X., Bai, H., Liu, G., & Dai, Y. (2019). Detecting word-based algorithmically generated domains using semantic analysis. Symmetry, 11(2), 176.
- 17. Okello, M. (2018, October). A New Timing Steganography Algorithm in Real-Time Transmission Devices. In 2018 IEEE 18th International Conference on Communication Technology (ICCT) (pp. 880-884). IEEE.
- Okello, M. O. (2021). Transmission of Secret Information Based on Time Instances. The Eurasia Proceedings of Science Technology Engineering and Mathematics, 16, 209-218. DOI: 10.55549/epstem.1068612 19. Ebbinghaus, H. D., Flum, J., Thomas, W., & Ferebee, A. S. (1994). Mathematical logic (Vol. 1910). New York: Springer.
- 19. Weisstein, Eric W. ?Concatenation.? From MatheWorld?A Wolfram WebResource. http://mathworld.wolfram.com/Concatenation.html.
- 20. Stephanie Glen. "Probability of Two Events Occurring Together" From StatisticsHowTo.com: Elementary Statistics for the rest of us!. https://www.statisticshowto.com/how-to-find-the-probability-of-two-events-occurring-together/