

## Comparison Of Anomalous Higgs Couplings at the Large Hadron Collider and at Proton-Proton Collider with 100 TeV Energy

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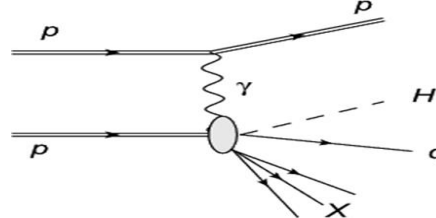
**Abstract**  $\gamma p$  and  $\gamma\gamma$ , called photon induced processes, have been examined in various colliders like Large Hadron Collider (LHC) and proton-proton collider with 100 TeV energy. One of the importance of these processes is that they allow for probing the anomalous Higgs couplings. The anomalous Higgs couplings constitute a testing ground for electroweak symmetry breaking (EWSB) mechanism and mass production system. For measuring anomalous  $H\gamma\gamma$  and  $HZ\gamma$  couplings at the LHC and at the proton-proton collider with 100 TeV energy, the potential of the  $pp \rightarrow p\gamma p \rightarrow pHqX$  has been examined. Sensitivity bounds on anomalous Higgs couplings have been obtained at %95 confidence level. The analyses have been done for various integrated luminosities and different scenarios. Then the results of them have been compared. Model-independent effective Lagrangian technique has been used, and the Higgs boson couplings to gauge bosons have been examined by dimension-six operators.

### 1. Introduction

The Large Hadron Collider (LHC) which has a center of mass energy with 14 TeV and luminosity of  $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$  is one of the the most important accelerator of the world.

ATLAS and CMS Collaborations discovered the Higgs boson estimated by Standard Model (SM) of particle physics at the LHC [1,2]. The next stage is to examine the features of this significant particle and its couplings to other SM particles. These studies have a great importance for supporting SM and investigating new physics. On the other hand the future 100 TeV proton-proton collider ensures an ideal venue to examine new physics. [3-5]. Such studies on anomalous Higgs couplings at LHC and at future 100 TeV proton-proton collider have been speedily increasing in the literature. (6-18) In this paper Higgs boson production via the main process  $pp \rightarrow p\gamma p \rightarrow pHqX$  haven been examined at the LHC

and at future 100 TeV collider. This process can be shown as follow diagram(40):



**Figure 1.** Representation of the process  $pp \rightarrow p\gamma p \rightarrow pHqX$ .

Here, q and X constitute quarks and proton remnants respectively.

The top quark distribution has been ignored and 10 independent subprocess for  $q = u, d, s, c, b, \bar{u}, \bar{d}, \bar{s}, \bar{c}, \bar{b}$  have been considered. In the existence of anomalous  $H\gamma\gamma$  and  $HZ\gamma$  couplings the Feynmann diagrams of subprocess  $\gamma q \rightarrow Hq$  is drawn as follows(40):

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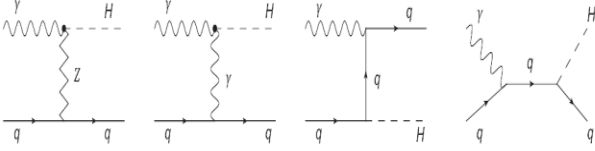


Figure 2. Feynman diagrams of  $\gamma q \rightarrow Hq$  at the tree-level.

At last studies, the presence of these photon-induced processes have been confirmed by CMS ATLAS Collaborations [19-23]. And also it is verified that these reactions have an important potential to examine new physics [21-23]. In such a process, photon-proton collision takes place when a quasi-real photon has been emitted from one of the incoming protons. So that it can be thought that proton-photon collision is a subprocess of the proton-proton collision. In that paper equivalent photon approximation (EPA) [24-26] has been taken into account. According to this approximation, emitted photons are accepted to be real because of having a very low virtuality. The protons which emit quasi-real photons do not divide into partons and they keep to be intact [27-28].

## 2. Material and Method

### 2.1. Anomalous $H\gamma\gamma$ and $HZ\gamma$ Couplings And The Cross Section

For examining anomalous  $HZ\gamma$  and  $H\gamma\gamma$  couplings one of the ways is to employ effective Lagrangian formalism. [7-9,29-33]

In this formalism total effective Lagrangian can be expressed as follows:

$$L_{eff} = \sum_n \frac{f_n}{\Lambda^2} O_n \quad (1)$$

Here  $f_n$  indicates the anomalous couplings and the scale of new physics is described by  $\Lambda$ . Also  $O_n$  indicates five dimension- six operators which alter the Higgs boson couplings to  $Z$  and  $\gamma$  bosons [7-9,29-33] They can be explicitly expressed as follows:

$$\begin{aligned} O_{ww} &= \phi^\dagger W_{\mu\nu} W^{\mu\nu} \phi \\ O_W &= (D_\mu \phi)^\dagger W^{\mu\nu} (D_\nu \phi) \\ O_{BB} &= \phi^\dagger B_{\mu\nu} B^{\mu\nu} \phi \\ O_B &= (D_\mu \phi)^\dagger B^{\mu\nu} (D_\nu \phi) \\ O_{BW} &= \phi^\dagger B_{\mu\nu} W^{\mu\nu} \phi \end{aligned} \quad (2)$$

Here,  $\Phi$  indicates the scalar doublet and  $D_\mu$  indicates the covariant derivative. Also the other fields can be expressed as follows:

$$\begin{aligned} W_{\mu\nu} &= i \frac{g}{2} (\vec{\sigma} \cdot \vec{W}_{\mu\nu}) \\ B_{\mu\nu} &= i \frac{g'}{2} \vec{B}_{\mu\nu} \end{aligned} \quad (3)$$

where  $g$  is the  $SU(2)_L$  gauge coupling and  $g'$  is the  $U(1)_Y$  gauge coupling. Also  $\sigma$  is the Pauli matrices. The effective Lagrangian in Eq-1 can be described as follows after the symmetry breaking. :

$$L_{eff} = g_{H\gamma\gamma} H A_{\mu\nu} A^{\mu\nu} + g_{HZ\gamma}^1 A_{\mu\nu} Z^\mu \partial^\nu H + g_{HZ\gamma}^2 H A_{\mu\nu} Z^{\mu\nu} \quad (4)$$

Here,  $V_{\mu\nu} = \partial_\mu V_\nu - \partial_\nu V_\mu$  with  $V=A(\text{photon})$  and  $Z$  field. Also  $g_{H\gamma\gamma}$ ,  $g_{HZ\gamma}^1$  ve  $g_{HZ\gamma}^2$  are anomalous couplings which involve the couplings  $f_n$  as follows:

$$g_{H\gamma\gamma} = - \left( \frac{g m_w}{\Lambda^2} \right) \sin^2 \theta_w \left( \frac{f_{BB} + f_{ww} - f_{BW}}{2} \right) \quad (5.1)$$

$$g_{HZ\gamma}^1 = \left( \frac{g m_w}{\Lambda^2} \right) \sin \theta_w \left( \frac{f_w - f_B}{2 \cos \theta_w} \right) \quad (5.2)$$

$$g_{HZ\gamma}^2 = \left( \frac{g m_w}{\Lambda^2} \right) \frac{\sin \theta_w}{2 \cos \theta_w} [2 \sin^2 \theta_w f_{BB} - 2 \cos^2 \theta_w f_{ww} + (\cos^2 \theta_w - \sin^2 \theta_w) f_{BW}] \quad (5.3)$$

Here,  $\theta_w$  and  $m_w$  indicates Weinberg angle and  $W$  boson's mass respectively. Also in the calculations taken into account the energy scale of new physics as  $\Lambda=1$  TeV. For the aim of the easiness six scenarios of new physics have been considered as follows:

- Senaryo I ;  $f_B = f_w = 0$ ,  $f_{ww} = f_{BB}$
- Senaryo II ;  $f_{ww} = f_{BB} = 0$ ,  $f_B = -f_w$
- Senaryo III ;  $f_B = f_w = 0$ ,  $f_{ww} = -f_{BB}$
- Senaryo IV ;  $f_B = f_w = 0$ ,  $f_{ww} = \tan^2 \theta_w f_{BB}$
- Senaryo V ;  $f_{ww} = f_w = 0$
- Senaryo VI ;  $f_{BB} = f_B = 0$

For ignoring the contributions of  $HZZ$  and  $HWW$  couplings in the calculations  $f_{BW}$  is taken to be zero ( $f_{BW} = 0$ ). Taking into account one-loop level contribution of SM for the anomalous  $H\gamma\gamma$  ve  $HZ\gamma$  couplings, the effective Lagrangian can be written as follows [34,35] ;

$$\mathcal{L}_{eff}^{(SM)} = g_{H\gamma\gamma}^{(SM)} HA_{\mu\nu} A^{\mu\nu} + g_{HZ\gamma}^{(SM)} HA_{\mu\nu} Z^{\mu\nu} \quad (6)$$

Here,  $g_{HZ\gamma}^{(SM)} = \frac{\alpha}{4\pi v \sin\theta_W} (5.508 - 0.004i)$  and

$$g_{H\gamma\gamma}^{SM} = \frac{2\alpha}{9\pi v}.$$

The cross section of the main process is given as;

$$\frac{\sigma(pp \rightarrow p\gamma p \rightarrow pHqX)}{\sigma(\gamma q \rightarrow Hq)} = \int_{x_{1min}}^{x_{1max}} dx_1 \int_0^1 dx_2 \int_{Q_{min}^2}^{Q_{max}^2} dQ^2 \left( \frac{dN_\gamma}{dx_1 dQ^2} \right) \left( \frac{dN_q}{dx_2} \right) \times \quad (7)$$

where  $\left( \frac{dN_q}{dx_2} \right)$  and  $\left( \frac{dN_\gamma}{dx_1 dQ^2} \right)$  are quark distribution and equivalent photon functions, respectively.

Detailed information and the integral bounds for equivalent photon distribution function can be found in the literature [36,37]. Also, using the MSTW2008 programme (38), the quark distribution functions can be calculated numerically. At the high energies ( $E \gg m_p$ ),  $x_1$  can be taken as  $x_1 = \frac{E-E'}{E} = \frac{E_\gamma}{E} \approx \xi$ .  $\xi$  is called forward detector acceptance. Here,  $E$  is energy of the initial proton and  $E'$  is energy of final (scattered) proton. Also  $E_\gamma$  indicates the equivalent photon energy.  $\xi$  is called forward detector acceptance. Therefore during the calculations  $x_{1min}$  and  $x_{1max}$  are taken as  $x_{1min} = \xi_{min} = 0.015$  ve  $x_{1max} = \xi_{max} = 0.15$ .

In the analysis  $\chi^2$  criterion has been used and bounds on anomalous Higgs couplings have been determined at 95% (C.L.).  $\chi^2$  criterion is taken as follows:

$$\chi^2 = \left( \frac{N_{AN} - N_{SM}}{N_{SM} \delta_{err}} \right)^2 \quad (8)$$

Here,  $N_{AN}$  is number of events which contains SM and new physics contributions,  $N_{SM}$  is number of events in the SM and  $\delta_{err}$  is the statistical error.  $N_{AN(SM)}$  is calculated from the formula:

$N_{(AN)SM} = E \times S \times L_{int} \times Br \times \sigma_{(AN)SM}$ , where  $S$  represents the survival probability factor ( $S=0.7$ ),  $E$  represents the b-tagging efficiency ( $E = 0.6$ ),  $L_{int}$  represents the integrated luminosity and BR is the branching ratio for  $H \rightarrow b\bar{b}$  ( $Br = 0.6$ ). Also,  $\sigma_{SM}$  and  $\sigma_{AN}$  are SM and anomalous cross sections respectively.

The background subprocesses  $\gamma q \rightarrow k, b, b$  ( $q = u, d, s, c, b, u, d, s, c, b$ ;  $k = u, d, s, c, b, t, u, d, s, c, b, t$ ) which contribute to main process  $pp \rightarrow p\gamma p \rightarrow pbbqX$ , are calculated by using CalcHEP 3.6.20. [39]

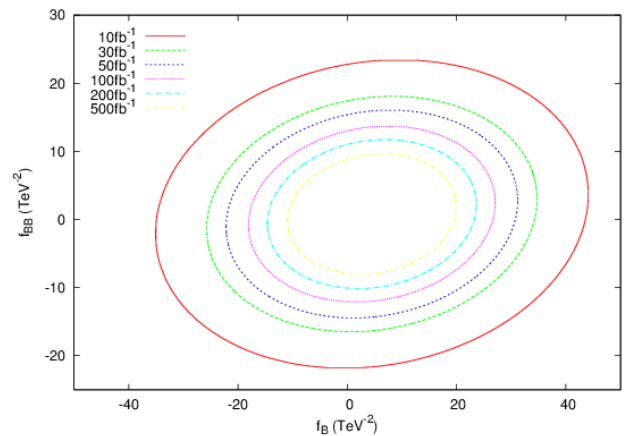
At the background calculations,  $H \rightarrow b\bar{b}$  decay channel of Higgs boson has been considered and  $b\bar{b}$  final state with invariant mass in the interval  $120 \text{ GeV} < M(b, \bar{b}) < 130 \text{ GeV}$  is identified as the signal. When these cuts are applied to the signal, the cross section of the background decline dramatically.

For LHC, taking into account scenarios I-IV, the bounds on anomalous  $f_w, f_{wW}$  and  $f_{BB}$  couplings are obtained in the Table -I at 95% C.L.

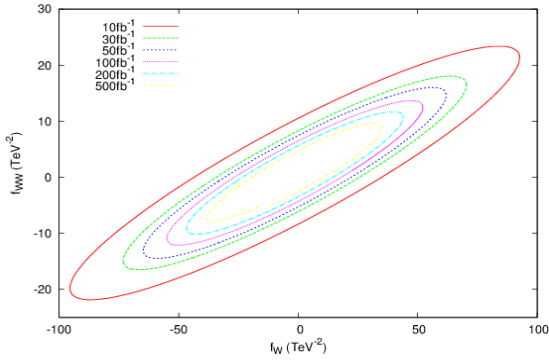
**Table I.** For various scenarios and luminosities the anomalous bounds are given at 95% C.L for LHC ( $\sqrt{s}=14 \text{ TeV}$ )

Luminosite	(Senaryo-I) $f_{ww}$	(Senaryo-II) $f_w$	(Senaryo-III) $f_{bb}$	(Senaryo-IV) $f_{bb}$
10 $fb^{-1}$	(-6.3,7.9)	(-19.8,15.4)	(-9.9,7.7)	(-13.2,15.6)
30 $fb^{-1}$	(-4.6,6.2)	(-15.6,11.3)	(-7.8,5.6)	(-9.8,12.2)
50 $fb^{-1}$	(-3.9,5.6)	(-14.1,9.7)	(-7.0,4.9)	(-8.5,10.8)
100 $fb^{-1}$	(-3.2,4.8)	(-12.2,7.9)	(-6.1,3.9)	(-7.0,9.3)
200 $fb^{-1}$	(-2.6,4.2)	(-10.7,6.4)	(-5.3,3.2)	(-5.7,8.1)
500 $fb^{-1}$	(-1.9,3.6)	(-9.0,4.7)	(-4.5,2.4)	(-4.3,6.7)

For scenarios V and VI, at LHC, with 95% C.L. restricted regions in two-dimensional  $f_B - f_{BB}$  and  $f_w - f_{wW}$  parameter spaces are given in Figure 3-4.



**Figure 3.** At 95% C.L. the restricted areas on  $f_B - f_{BB}$  parameter spaces are shown for LHC. ( $\sqrt{s}=14 \text{ TeV}$ )



**Figure 4.** At 95% C.L. the restricted areas on  $f_w - f_{ww}$  parameter spaces are shown for LHC. ( $\sqrt{s}=14$  TeV) Similarly, for 100 TeV proton-proton collider, taking into account scenarios I-IV, the bounds on anomalous  $f_w$ ,  $f_{ww}$  and  $f_{BB}$  couplings are obtained in the Table –II at 95% C.L.

**Table II.** For various scenarios and luminosities the anomalous bounds are given at 95% C.L. for future 100 TeV proton-proton collider .

Luminosity	(Scenario-I) $f_{ww}$	(Scenario-II) $f_w$	(Scenario-III) $f_{bb}$	(Scenario-IV) $f_{bb}$
$100fb^{-1}$	(-1.9,4.2)	(-8.2,4.0)	(-4.1,2.0)	(-4.9,9.0)
$500fb^{-1}$	(-1.1,3.3)	(-6.4,2.2)	(-3.2,1.1)	(-2.8,6.9)
$3000fb^{-1}$	(-0.5,2.8)	(-5.3,1.1)	(-2.7,0.6)	(-1.4,5.6)

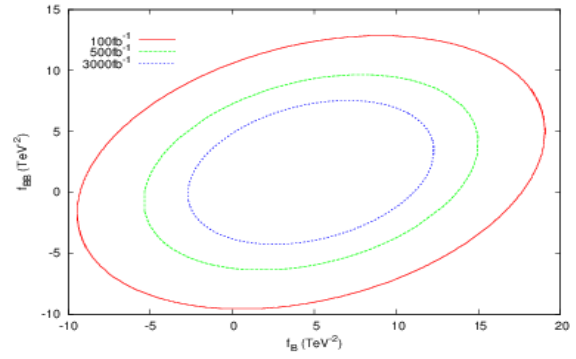
For scenarios V and VI, at 100 TeV proton-proton collider, with 95% C.L. restricted regions in two-dimensional  $f_B - f_{BB}$  and  $f_w - f_{ww}$  parameter spaces are given in Figure 5-6.

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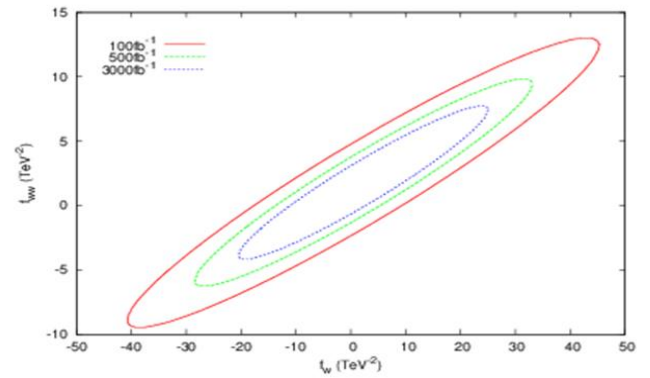
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**Figure 5.** At 95% C.L. the restricted areas on  $f_B - f_{BB}$  parameter spaces are shown for 100 TeV proton-proton collider.



**Figure 6.** At 95% C.L. the restricted areas on  $f_w - f_{ww}$  parameter spaces are shown for 100 TeV proton-proton collider.

**3. Conclusion and Suggestions**

As expected,  $\gamma p$  collision at 100 TeV proton-proton collider with a higher energy and a higher luminosity relatively, probes the anomalous  $H\gamma\gamma$  and  $HZ\gamma$  couplings with better sensitivity than  $\gamma p$  collision at the LHC. Consequently, we can say that, the sensitivity bounds on anomalous Higgs couplings are refined by an improvement factor of 2.

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