



## Hybrid Adaptive Neuro Fuzzy based speed Controller for Brushless DC Motor

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### Abstract

This paper presents a Hybrid Adaptive Neuro Fuzzy Control technique for speed control of BLDC motor drives. The proposed controller is an integration of adaptive neuro fuzzy, fuzzy PID and PD controllers. The objective is to utilize the best attribute of fuzzy PID and PD controllers, which exhibits a better response than the neuro fuzzy controllers. The error back propagation learning algorithm (EBPA) is used to train the data to minimize learning error. To validate the performance of proposed controller, simulations are done in MATLAB and comparison is made with PI, PD and fuzzy PID controllers. In addition, the performance of proposed controller is benchmarked with other controllers reported in the literature. The results of the proposed controller are promising in terms of quick settling time, zero peak overshoot and zero steady state error.

## 1. INTRODUCTION

The Brushless DC (BLDC) Motor is a permanent magnet synchronous motor (PMSM) with trapezoidal Back EMF, and requires no mechanical commutators. It would have certain advantages like high efficiency, high power density, required torque, speed characteristics, and easier control [1-3]. Speed control of BLDC motor drives is a key topic in the field of the control theory. Ziegler- Nichols [4] first implemented the PI/PID controller tuning. The conventional controllers like proportional Integral controller (PI), Proportional Derivative/Proportional Integral Derivative controller (PD/PID) are widely used in electrical applications, chemical processes and various industrial control applications, etc., over a few decades because of their simple design, acceptable control effect and robustness.

In [5-10], discussed the different types of PI controllers like anti-windup PI, self-tuned, offline, gain scheduled PI Controllers to control the speed in the Motors. But these controllers have a certain disadvantages like larger rise time, settling time and more oscillations in steady state. The optimal PI controller gains are obtained in [11-13] using neural networks, algorithms like Practical Swarm Optimization (PSO) and Bacterial Forging (BF) optimization to achieve the optimal performances. The drawbacks of these methods are larger steady state error under sudden load disturbances. The phase locked loop (PLL) assisted internal model (IM) controller to control the speed of BLDC motors is proposed in [14]. This controller has an adjustable speed module structure and integrated with IM control strategy. The conventional controllers are not quite suitable for the drives, which exhibit parameters uncertainty and unmodelled dynamics.

To improve the performance in industrial applications the researchers found out fuzzy logic controllers to be more suitable. In [15] a fuzzy logic controller for achieving improved speed performance of a BLDC servo motor drive is made. In this fuzzy logic controller is implemented in the digital form. The presented controller is effective in dealing with uncertainties and parameter variations when compared with normal PID controllers. In [16], to improve the fuzzy controller performance researches done the optimization of the fuzzy membership functions. The advantages of optimal FLC controller are that it avoids trial and error method for obtaining the membership function.

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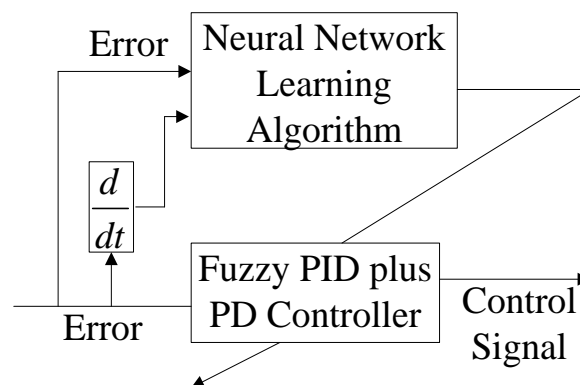
In [17] the extended kalman filter (EKF) filter to control the speed of BLDC motor. Here EKF is employed to find the state variables by using stator line voltages and currents. The EKF is used to estimate the speed of BLDC motor in both steady state and dynamic conditions. In [18-22] developed the different types of fuzzy PID controllers, in [23-26] describes the optimal Fuzzy PID controllers and in [26-28] developed the fractional order fuzzy PID controllers to achieve the optimal performances. The extension of the fuzzy PID controller are neural network is used to train the fuzzy outputs. In [29] dealt about the PI/PD fuzzy neural network controller based on EKF to control BLDC motor drives. In the controller, EKF is used to train the fuzzy neural network type PI/PD controller. The fuzzy neural network has two parallel PI/PD controllers with four internal layers.

A prominent technique called adaptive neuro fuzzy controller is used in various applications. Some of the important applications are maximum power extraction and inertia control of wind turbines [30] & [31], estimation of mechanical properties for conductive silicone rubber [32], control of robotic gripper [33], human musculoskeletal arm [34], antilock braking system [35], underwater vehicles [36], control of non linear industrial process and batch process [37] & [38], estimation of system forecasting [39], estimation of open lens system parameters [40]. For electrical applications, adaptive neuro fuzzy system is used to control the speed of electrical motors. In [41] the adaptive neuro fuzzy controller to control the speed in permanent magnet excitation transverse flux linear motor. This controller has two fuzzy inputs and one fuzzy output. The scaling factors of the fuzzy logic controller are trained by artificial neural network.

In [42], a technique for speed control of BLDC motor using the adaptive neuro fuzzy interface methodology. The error and change in error are inputs and controller output data is used to train the adaptive neuro fuzzy system. This adaptive neuro fuzzy controller gives better performance under different load conditions.

In [43] a fuzzy PID supervised ANFIS controller to control the speed of BLDC motor. The Recursive least square back propagation algorithm is used to train the neuro fuzzy system. As we observe the above literature the existing controllers having disadvantages like more settling time, steady state errors and undesired response under varying load conditions. So we proposed a controller to improve the further better settling time, desired response when load varying conditions and zero steady state errors.

In this article, a hybrid adaptive neuro fuzzy controller is proposed to control the speed of the brushless DC motor. The proposed controller is a combination of adaptive neuro fuzzy, fuzzy PID and PD controller. The training data of proposed controller is taken from the input, error and output data of fuzzy PID plus PD controller. The block diagrams of the existing adaptive neuro fuzzy controller are shown in Fig. 1. The organization of the paper is as follows. Section 1 deals the Introduction of the paper. Section 2 describes mathematical modeling and methodology for speed control of brushless DC motor. Section 3 explains the design of proposed controller. Section 4 gives the results and discussions. Finally, the conclusions of proposed controller are discussed in section 5.



**Figure 1.** Block diagram of adaptive neuro fuzzy Controller

## 2. METHODOLOGY TO CONTROL THE SPEED OF BLDC MOTOR

The merits of the BLDC motor, when compared to the DC motor, have higher reliability, lower electromagnetic interference (EMI) and lower maintenance costs [1] & [2]. The various fields of applications of BLDC Motor are aerospace applications, domestic applications, industrial automation sector, medical, textile industry and digital control machine tools. Generally, the BLDC Motor consists of three stator windings and permanent magnets on the rotor. BLDC Motor is stated as the trapezoidal back EMF permanent magnet synchronous motor [3], [15] & [44]. The line to line voltage equations is expressed in Eq. (1).

$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} R & 0 & 0 \\ 0 & R & 0 \\ 0 & 0 & R \end{bmatrix} \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} + \begin{bmatrix} L-M & 0 & 0 \\ 0 & L-M & 0 \\ 0 & 0 & L-M \end{bmatrix} \begin{bmatrix} \frac{di_a}{dt} \\ \frac{di_b}{dt} \\ \frac{di_c}{dt} \end{bmatrix} + \begin{bmatrix} e_a \\ e_b \\ e_c \end{bmatrix} \quad (1)$$

Where,  $V_a, V_b, V_c$  represents the phase voltages of BLDC Motor in Volts,

$R$  represents the resistance of stator Windings in ohms,

$i_a, i_b, i_c$  represents phase currents of the motor in amperes,

$L$  represents the Self Inductance in Henry,

$M$  represents the mutual inductance.

$e_a, e_b, e_c$  denotes the trapezoidal back EMF of each phase in volts.

The electromechanical torque of the BLDC motor is given in Eq.(2)

$$T_a = \frac{(e_a i_a + e_b i_b + e_c i_c)}{\omega_1}, \omega_1 = \frac{d\theta_r}{dt} \quad (2)$$

The terms  $\omega_1, \theta_r$  represents the rotor position, angular velocity (rad/s). The electromagnetic torque is utilized to overcome the opposing torques of inertia and load, it can be expressed as Eq. (3).

$$T_a = T_L + J_n \frac{d\omega}{dt} + B_n \omega_1; \omega_e = \frac{p}{2} * \omega_1 \quad (3)$$

Then the terms  $T_L$  represents load torque (NM/A),  $J_n$  is Momentum of Inertia (J or kg/m<sup>2</sup>),  $B_n$  indicates Friction coefficient,  $\omega_e$  are rotor frequency and  $p$  represents the number of poles in the rotor. To analyze and verify the performance of the proposed controller architecture, simulations were performed in MATLAB/Simulink. The basic building blocks of closed loop control system for this article are BLDC motor, DC power supply, three-phase voltage inverter, three phase V-I Measurement block and switching logic circuits. The reference signal speed 1200 rpm is given as input signal and output speed signal of the BLDC Motor is given to the proposed controller as feedback. The switching logic is developed by using three hall signals  $H_1, H_2, H_3$ , and controller signal, switching logic is given as gating signal to three phase voltage inverter. The Fig.2 shows the Simulink diagram for speed control of BLDC Motor.

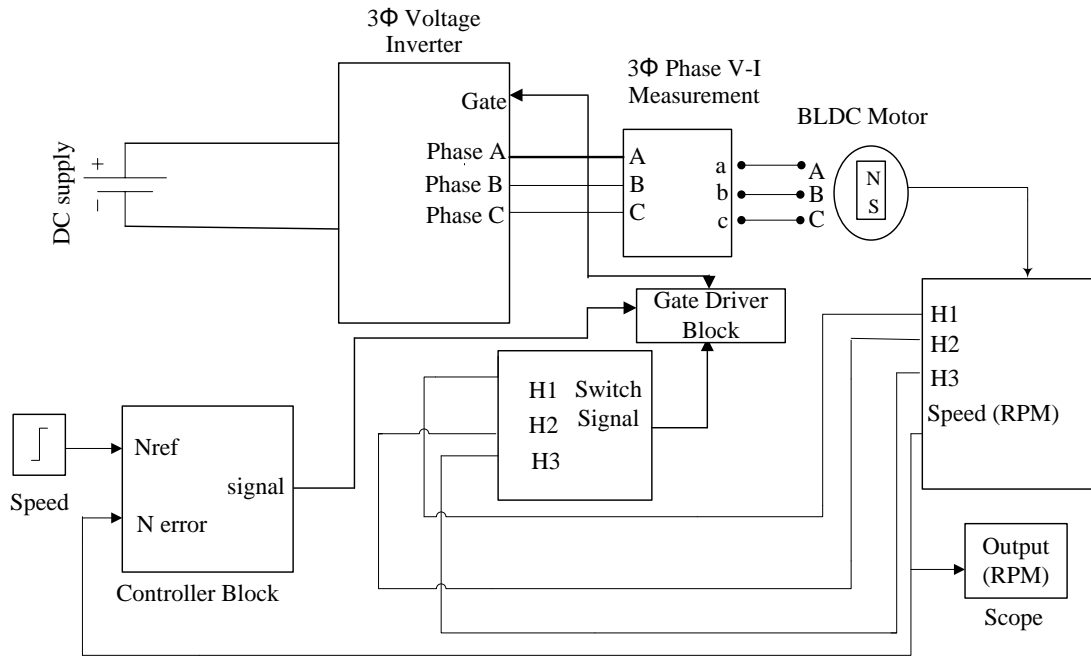


Figure 2. Simulink Model diagram of Speed Control of BLDC Motor

### 3. PROPOSED CONTROLLER FOR SPEED CONTROL OF BLDC MOTOR

The proposed controller for speed control of BLDC Motor is given by the integration of adaptive neuro fuzzy controller, fuzzy PID and PD controller. Initially, the fuzzy PID controller was tuned by using the error signal. The output and input data of fuzzy PID and PD is taken to train the adaptive neuro fuzzy interface system (ANFIS) to tune the adaptive neuro fuzzy controller. Finally, the outputs of the ANFIS, fuzzy PID controller, and PD controller are added parallel named as hybrid adaptive neuro fuzzy controller. The Fig.3 shows the block diagram of the proposed controller.

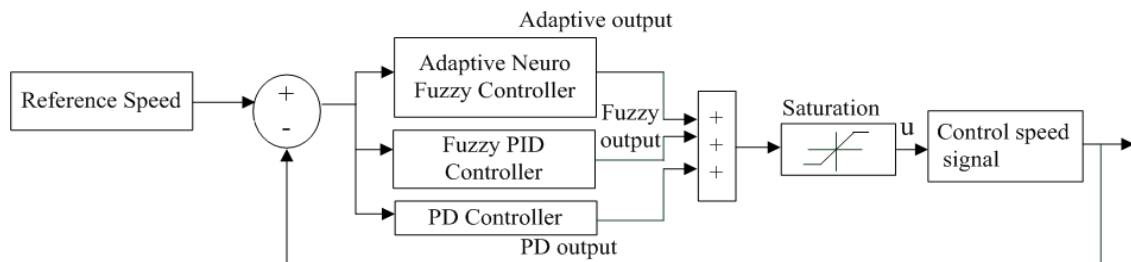


Figure 3. Block Diagram of the proposed hybrid adaptive neuro fuzzy controller

The main advantage of the fuzzy inference system is, it controls the complex systems, nonlinear systems, and the time varying dynamic processes systems in several industrial control loops. It can be used as the online gain tuner for developing the fuzzy PID controller. The fuzzy PI and fuzzy PD controller are combined to form fuzzy PID controller [20]. As shown in the Fig.3, a PD controller runs parallel to fuzzy PID controller and adaptive neuro fuzzy controller.

#### 3.1 Adaptive neuro fuzzy Controller

The adaptive neuro fuzzy controller is a combination of artificial neural network with fuzzy interface system. The Takagi- Sugeno model is used in this proposed work [45]. ANFIS is a very good learning technique to take over an issue on uncertainties in any system. This controller is based on constructing a set of fuzzy IF-Then rules with an appropriate membership function to generate the specify input- outputs.

The ANFIS is a taking a Fuzzy Inference System (FIS) and tuning with back propagation algorithm based on the collection of output and input data. The components of ANFIS are first is rule base, the second one is data base which is membership functions. The Third one is reasoning mechanism, which gives the reasonable output [30] & [32-33].

Consider the set of fuzzy rules

Let  $R_j = \text{If } x_1 \text{ is } A_1(x_1) \text{ and } x_2 \text{ is } A_2(x_2) \text{ and } \dots\dots\dots x_n \text{ is } A_{nj}(x_n) \text{ THEN } y \text{ is } c_j$

Where  $x_1 = \text{change in error given as } w_{ref} - w_r$ .

$x_2 = \text{derivative of change in error given as } d(w_{ref} - w_r)/dt$ .

$y = \text{output given as } P_i x_1 + R_i x_2 + S_i$

$A_1(x_1)$  and  $A_{nj}(x_n), \dots\dots\dots A_{nj}(x_n)$  are input linguistic labels and  $c_j$  is constant consequent labels.

In TS Fuzzy model, the inference procedure used to find the conclusion for input X consists of the two main steps.

The weight of  $w_j$  each rule is calculated as

$$w_j = \prod_{i=1}^n \mu_{ij}(x_i^0) \tag{4}$$

The output inference result  $y$  is obtained by means of the weighted average of the consequents

$$y = \frac{\sum_{j=1}^m w_j c_j}{\sum_{j=1}^m w_j} \tag{5}$$

Eq.(4) and (5) provides the complete representation of the inference model.

The Architecture of ANFIS network consists of different types of inference models as adaptive networks. The adaptive network consists of following layers as shown in Fig. 4.

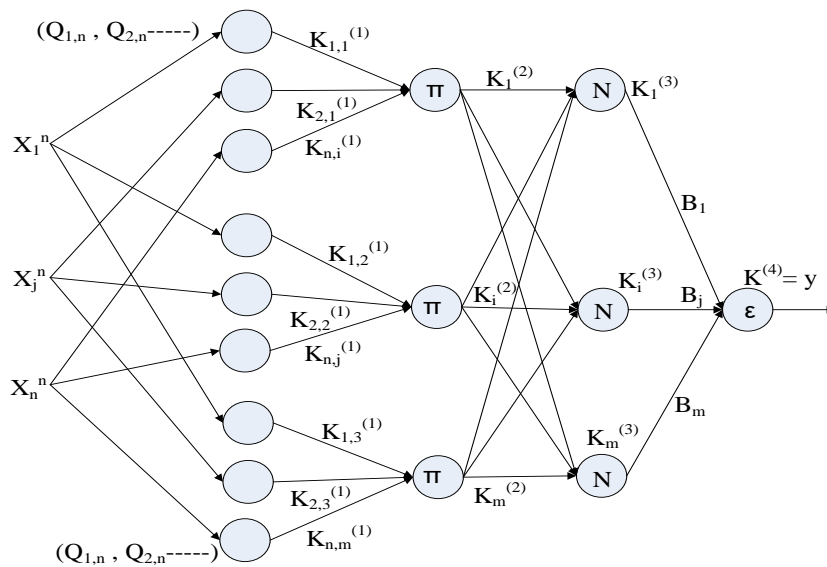


Figure 4. Architecture of an n – input adaptive neuro fuzzy controller

The layer 1 having m groups and having n nodes of each one. Every single node generates output  $k_{ij}^{(1)}$  by solving each membership function.

$$k_{ij}^{(1)} = \mu_{ij}(x_i^0) = f(x_i^0; p_{1ij}, p_{2j}, \dots) \quad (6)$$

The layer 2 having m nodes with outputs  $k_j^{(2)}$  node j in this layer generates the strength the  $j^{\text{th}}$  rule by solving the algebraic product of all inputs.

$$k_j^{(2)} = \prod_{i=1}^n k_{ij}^{(1)} = w_j \quad (7)$$

The layer 3 consists of an m – nodes normalization layer. The output of the  $j^{\text{th}}$  node  $k_j^{(3)}$  is the ratio of the  $j^{\text{th}}$  rules of weight to the sum of the all the rules.

$$k_j^{(3)} = \frac{w_j}{\sum_{j=1}^m w_j} \quad (8)$$

The layer 4 consists of only one node. The node output  $k_j^{(4)}$  is the sum of the weighted consequents. This node is an adaptive node whose parameters  $c_j$ , are the set of consequent parameters.

$$k_j^{(4)} = \sum_{j=1}^m k_j^{(3)} c_j = y \quad (9)$$

Adaptive neuro fuzzy constructs a fuzzy interface system FIS whose membership function values are tuned using EBPA.

### 3.1.1 Learning Algorithm: Error Back Propagation Algorithm (EBPA)

In this proposed controller, the neuro fuzzy interface system was trained by using the error backpropagation learning algorithm. In this method weight updating is mostly performed based on gradient descent method [46] & [47]. The standard back propagation learning algorithm is given by

$$\Delta W_{p,ij}^{i,(i+1)} = \alpha \frac{\partial E_p}{\partial W_{p,ij}^{i,(i+1)}} \quad (10)$$

$$\Delta b_{p,i}^1 = -\alpha \frac{\partial E_p}{\partial b_{p,i}^1} \quad (11)$$

Where  $W_{ij}$  is the weights between  $i^{\text{th}}$  and  $j^{\text{th}}$  neuron of two connected neurons of two connected layers. The  $b_i$  and  $\alpha$  represents the bias of neuron and learning rate. The notation p is the weight and biases of each input learning pattern.

Training of weights ( $E_p$ ) is given by the following eq. (12)

$$E_p = \sum_{k=1}^{nl} (t_{p,k} - o_{p,k})^2 \quad (12)$$

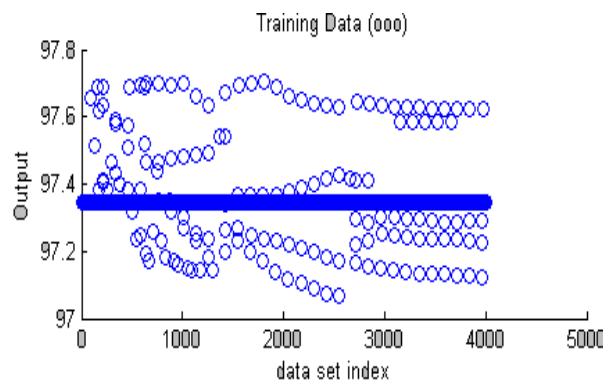
The training is continued up to the sum of squares for all the input pattern (E), reached to the minimum value given in eq. (13)

$$E = \sum_{p=1}^P \sum_{k=1}^{N_L} (t_{p,k} - o_{p,k})^2 \tag{13}$$

Where  $t_{p,k}$  is defined as desired target.  $o_{p,k}$  defined as network output of  $K^{th}$  neuron for input pattern respectively. The  $N_L$  is the number of neurons in layer  $L$ . Adaptive neuro fuzzy constructs a fuzzy interface system FIS whose membership function values are tuned using EBPA. For the proposed controller the data of error and change error of fuzzy PID plus PD controller data set is used it having the 4000 sets are present. The linear equation of the data sets to train the adaptive neuro fuzzy is given in eq. (14).

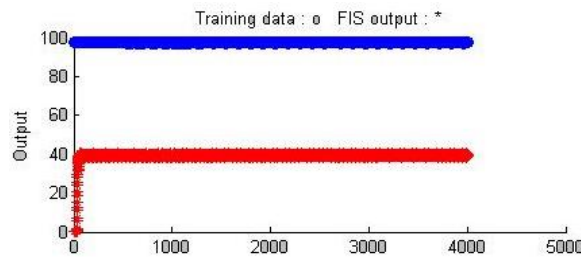
$$y = 2E + 0.7x - 5E + 09 \tag{14}$$

The grid partition method is used to generate the adaptive fuzzy controller. The 3 input and 3 output member functions are taken to generate the controller. The Fig.5 and Fig.6 show the input and train data for adaptive neuro fuzzy controller.



**Figure 5.** Training Dataset of adaptive neuro fuzzy controller

The Structure of adaptive fuzzy controller, generated by the MATLAB code is a five layer network as shown in Fig. 7. It has two inputs given as error and change in error, one output, three membership functions for each. The training error of the proposed controller is shown in Fig 8.



**Figure 6.** Adaptive neuro fuzzy output data

The membership functions for each input, which is trained by the grid partition method as shown in Fig.9. The Fig.10 shows the output of fuzzy rule for a specific value of error and change in error. The adaptive neuro fuzzy controller generated for Fuzzy PID plus PD Controller surface, 3–dimensional plot between two inputs error and change in error and output is shown in Fig.11

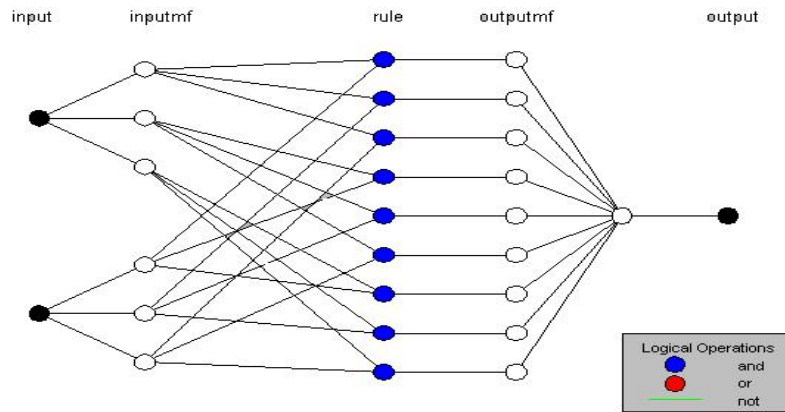


Figure 7. Structure for adaptive neuro fuzzy controller

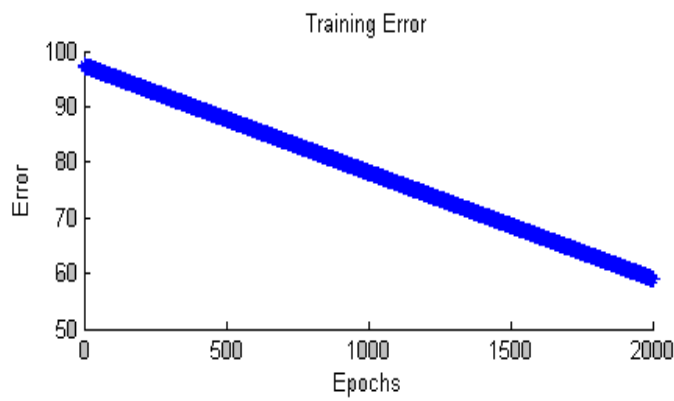


Figure 8. Training error Plot

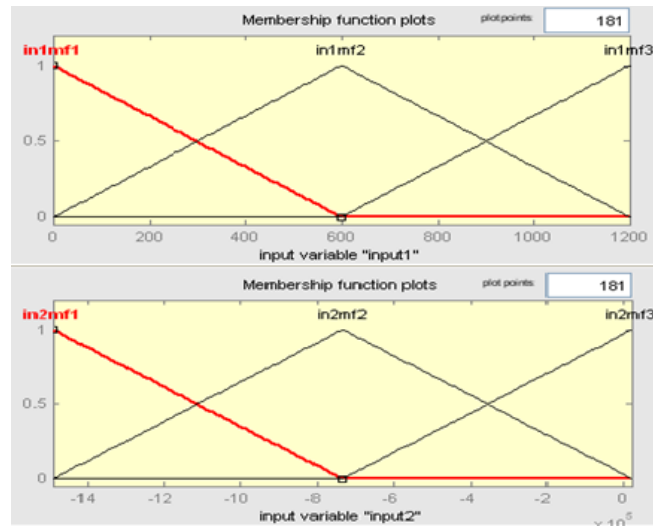


Figure 9. Input Membership Functions



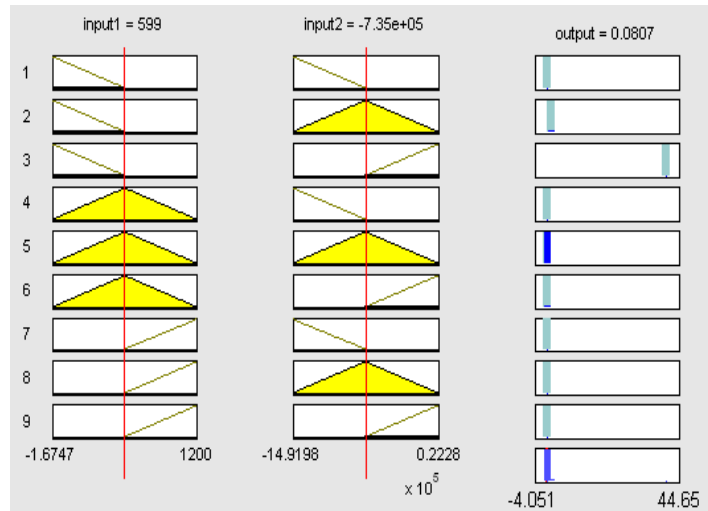


Figure 10. Adaptive neuro fuzzy controller rules

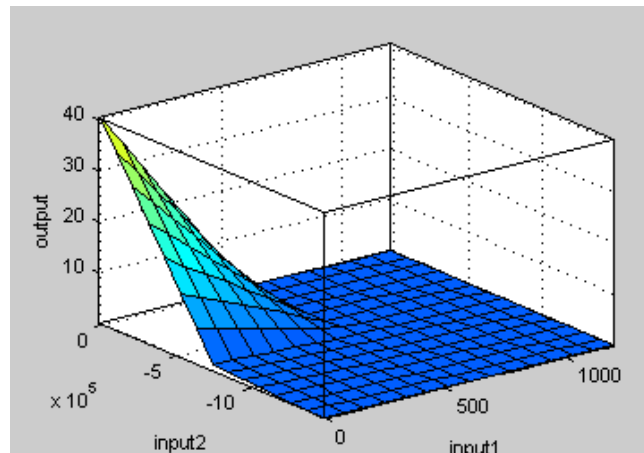
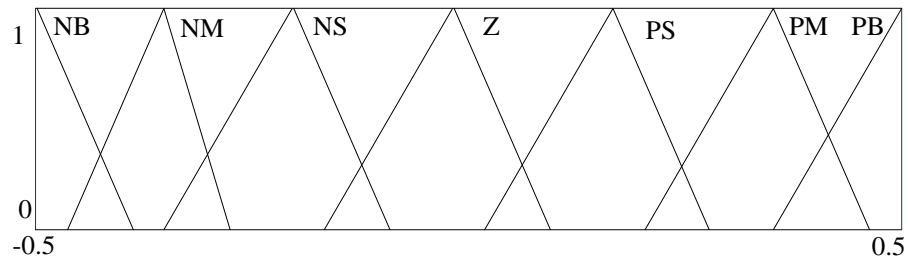


Figure 11. Surface plot between two inputs and one output.

### 3.2 Fuzzy PID Controller

The fuzzy systems are universal approximators. Fuzzy systems are used in situations involving highly complex systems, and for the system, whose behaviour is not clean [18] &, [21]. Both inputs and outputs have 7 triangular membership functions. The input range for both inputs and outputs is between [0.5 to 0.5]. The distribution of the membership functions has even functions, negative big, negative medium, negative small, zero, positive small, positive medium and positive big. The distribution of the membership functions as shown in the Fig. 12. The defuzzification of these fuzzy sets is given by the centroid method. The centroid method is also called as the centre of area or the centre of gravity. The formula governing the defuzzification is represented in Eq.(11).

$$z = \frac{\int V_c(z) dz}{\int V_c(z) dz} \tag{11}$$



**Figure 12.** Membership functions of inputs and outputs for Fuzzy PID Controller

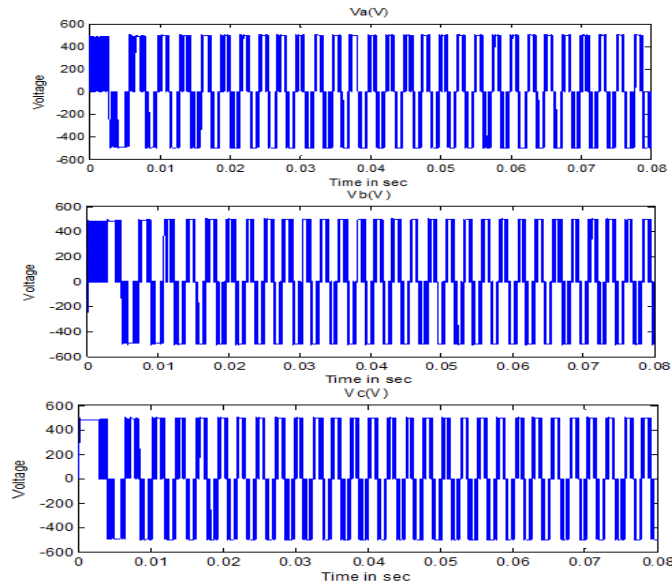
#### 4. RESULTS AND DISCUSSIONS

Speed response of the BLDC motor is analyzed under the constant speed, varying speed, set point tracking. The control system parameters such as rise time, peak time, settling time, steady state error, peak overshoot, integral absolute error, are used to compare the speed response of a proposed controller with fuzzy PID controller and PI controller. The specifications of the BLDC motor are shown in Table.1

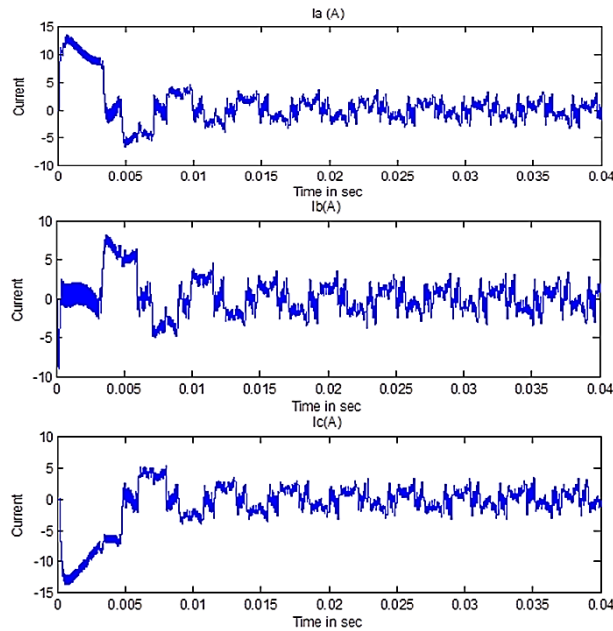
**Table.1.** Specifications of BLDC Motor

Specifications	Value
Rated Voltage (V)	500
Rated Current (A)	8
Rated Speed (rpm)	1200
Stator phase Resistance, R ( $\Omega$ )	14.56
Stator phase Inductance, I (H)	0.0025
Flux Linkage Established in Magnets (V.s)	0.106
Voltage Constant (V/rpm)	146.6
Torque Constant (N.M/A)	0.74
Back EMF flat Area (Degrees)	120
Moment of Inertia (J(kg/m <sup>2</sup> ))	0.0008
Friction factor (N m/(rad/s))	0.001
Pole Pairs	4

The Fig.13(a) and Fig.13(b) shows simulation results of the phase voltages with phase different of  $120^\circ$  and phase currents having 3.7 Amp of BLDC motor.



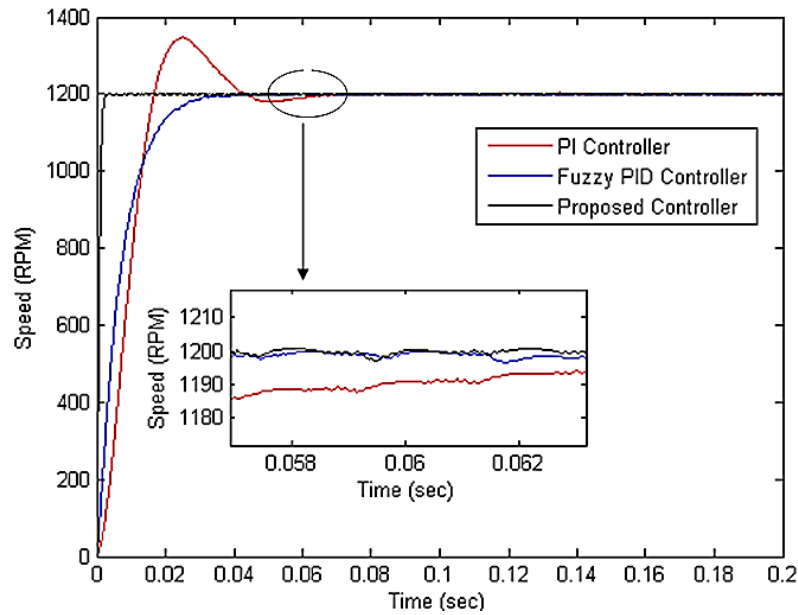
**Figure 13 (a).** Phase voltage waveforms



**Figure13 (b).** Phase current waveforms

**4.1 Result for Constant speed condition at 1200 RPM under constant load condition 20 Nm**

The simulation results for speed control of Brushless DC motor at constant speed condition with constant load condition 20 Nm are shown in Fig .14. The set point of the speed is 1200 RPM. The time domain specifications of the output response are shown in Table 2 as Case .A. The steady state error of PI, Fuzzy PID is 0 and 0.2. The steady state error of proposed Hybrid adaptive neuro fuzzy controller is zero. The settling time for PI and fuzzy PID are 0.07sec, 0.052 sec.The settling time for proposed controller is 0.0045sec. The Integral absolute error (IAE) for PI, Fuzzy PID and proposed adaptive neuro fuzzy controller is 8.127, 5.8521 and 0.70 respectively. The peak over shoot of the PI controller is 1345 rpm, but the fuzzy PID and the proposed hybrid adaptive neuro fuzzy controller exhibits zero overshoot. As in Fig.14, the PI controller fluctuates more while compared with proposed controller The time specifications of the system is better for the proposed hybrid adaptive neuro fuzzy controller.



**Figure 14.** Performance of Controllers at constant load condition, 20Nm

#### 4.2 Result for Speed at 1200 RPM under varying load condition 1Nm to 20Nm

The simulation results for speed control of BLDC motor at constant speed condition with varying load condition 1Nm to 20Nm are shown in Fig.15. The set point of the speed is 1200 RPM. The time domain specifications of the output response are shown in Table 2 as Case B. The steady state error of PI and Fuzzy PID are 0, 0.2.

**Table 2.** Comparisons of controllers under constant load condition 20 Nm and varying load 1Nm to 20 Nm Condition

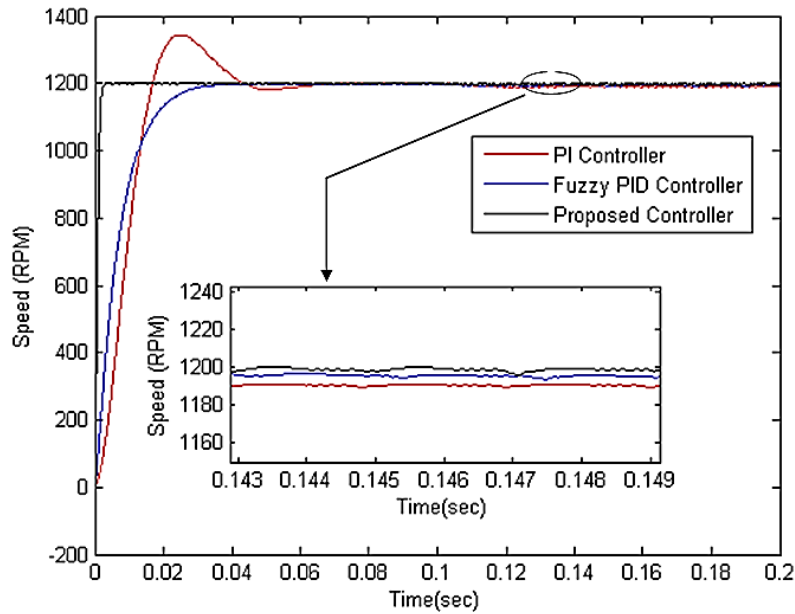
Type of Controller		Control system Parameters						
		Rise Time( $t_r$ ) Sec	Peak Time( $t_p$ ) Sec	Peak Value (RPM)	Peak Overshoot (%)	Settling Time ( $t_s$ ) Sec	SteadyState Error (RPM)	IAE
PI	Case A (constant load)	0.015	0.025	1345	12	0.07	0	8.127
	Case B (Varying load)	0.165	0.025	1345	12	0.075	0	8.61
Fuzzy PID	Case A	0.016	-	-	-	0.052	0.2	5.852
	Case B	0.016	-	-	-	0.06	0.2	6.23
Proposed Controller	Case A	0.0015	-	-	-	0.0045	-	0.70
	Case B	0.0018	-	-	-	0.0045	-	1.126

The steady state error of proposed adaptive neuro fuzzy controller is zero. The settling time for PI, fuzzy PID controllers are 0.075sec and 0.06sec respectively. The settling time for proposed controller is 0.0045sec. The Integral absolute error (IAE) for PI, Fuzzy PID and proposed adaptive neuro fuzzy controller is 8.61, 5.862 and 1.126 respectively. By observing the time domain specifications the proposed

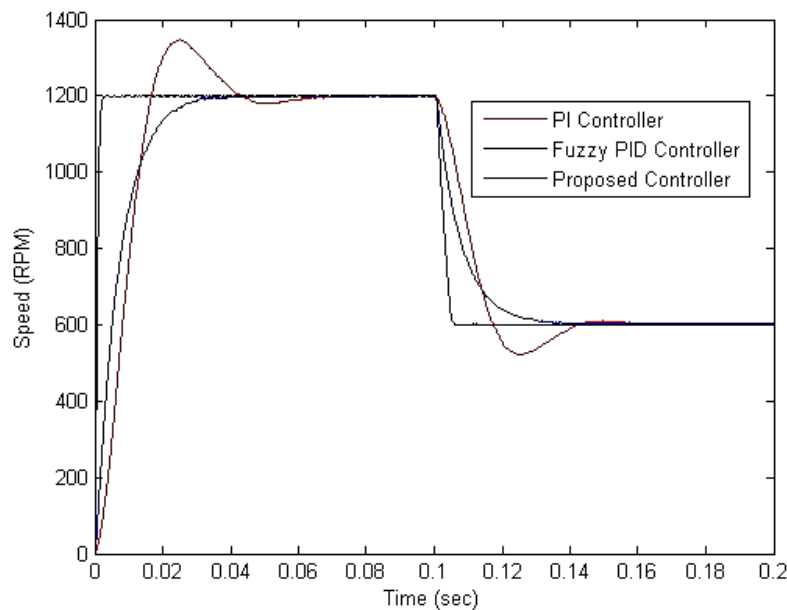
controller gives the better response for speed control of BLDC motor. As found in the Fig. 15, the proposed controller has little fluctuations when compared to the other controllers. The steady state error is zero.

**4.3 Result for setpoint speed at 1200 RPM to 600 RPM under constant load condition 20 Nm**

The simulation results for speed control of BLDC motor under varying speed condition under load condition are shown in Fig.16. The set point tracking of the speed is varied between 1200 RPM to 600 RPM at 20 Nm. The time domain specifications of the output response are shown in Table 3. The steady state error of PI, Fuzzy PID controllers is 0 and 0.7 respectively. The steady state error of proposed adaptive neuro fuzzy controller is 0. The recovery time for PI and Fuzzy PID are 0.22sec and 0.2sec. The recovery time for proposed controller is 0.145sec. The Integral absolute error (IAE) for PI, fuzzy PID and adaptive neuro fuzzy controller is 18.94, 13.35 and 2.211 respectively. The peak overshoot for PI, fuzzy PID and proposed adaptive neuro fuzzy controller is 16.6, 0 and 0 respectively. By observing the time domain specifications, the proposed controller tackles the setpoint better while compared with other controllers.



**Figure 15.** Speed Response for different conditions under varying load conditions



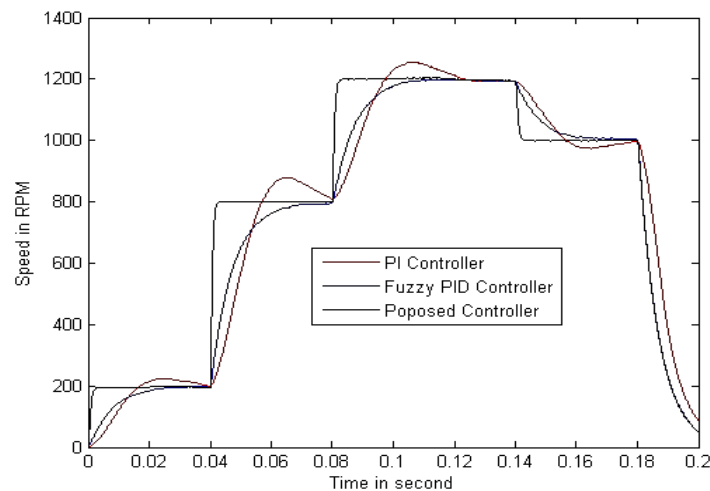
**Figure 16.** Speed Response varying speed condition under load condition 20 Nm

As seen in the Fig. 16, the proposed controller gives the very less oscillations under varying speed conditions. The proposed hybrid adaptive neuro fuzzy controller has zero steady state error.

**Table 3.** Comparisons of controllers under constant load condition 20 Nm with Speed Variation 1200 RPM to 600 RPM

Type of Controller	Control system Parameters			
	Peak Overshoot	Recovery time (sec)	Steady state Error	IAE
PI Controller	16.6	0.22	-	18.9
Fuzzy PID Controller	-	0.2	0.7	13.35
Proposed Controller	-	0.145	-	2.211

Fig.17. Shows set point response for the proposed controller under no load condition. It shows the proposed controller settles in a very low time than the other existing controllers. Also it is observed that, the proposed hybrid adaptive neuro fuzzy controller takes less control energy than PI and Fuzzy PID controllers for all cases.

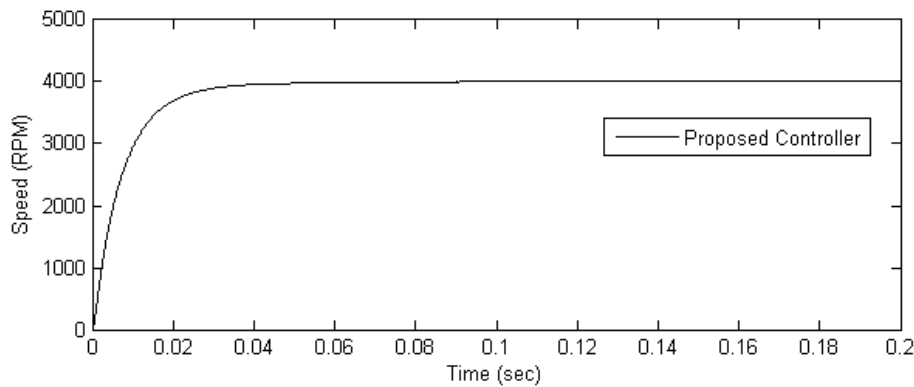


**Figure 17.** Comparison of controllers performance at no load condition

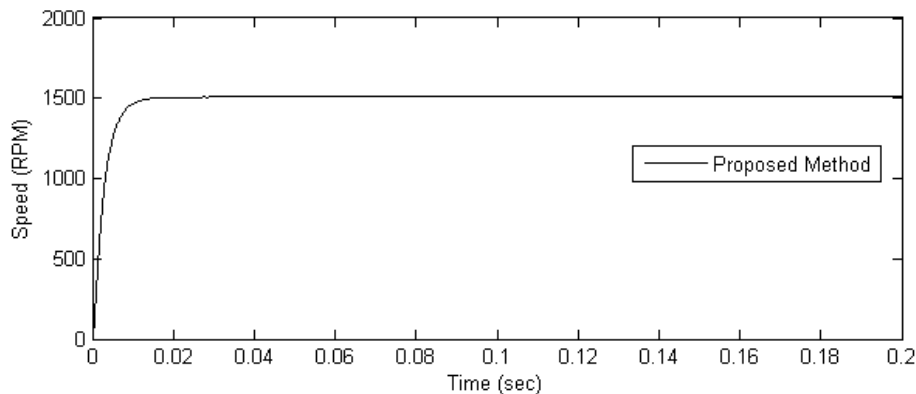
**Table 4.** BLDC Motor specifications of Ref-[26], [42] & [43]

Sl. No	Motor Parameters	Ref-[26]	Ref-[42]&[43]
1.	Rated Voltage (V)	24	470
2.	Rated Current (A)	7	50
3.	Rated Speed (rpm)	4000	1500
4.	Stator phase Resistance, R ( $\Omega$ )	1.4	3
5.	Stator phase Inductance, I (H)	0.0066	0.001
6.	Flux Linkage Established in Magnets (V.s)	-	0.175
7.	Voltage Constant (V/rpm)	0.1546	0.1466
8.	Torque Constant (N.M/A)	0.02	0.74
9.	Moment of Inertia (J/kg/m <sup>2</sup> )	0.00176	0.0008
10.	Friction factor (N m/(rad/s))	0.0003816	0.001
11.	Pole Pairs	4	4

To validate the proposed controller method, we compared with the other existing controllers presented in the literature. The motor specifications of ref [26], [42] and [43], were tabulated in Table.4. In [26], the motor specifications are vector control on a 24 V, 100 W, 7 A, rated speed is 4000 rpm and torque load is 0.02 Nm. Using these motor specifications the proposed controller is simulated and plotted the output shown in Fig 18. Table. 5 shows a comparison of settling time with other techniques available in the literature. The motor parameters specified in the cited literature were used in the proposed controller. In [26] results, hybrid fuzzy PI controller settling time is 0.19 sec. The proposed controller settles at 0.06 sec. Using these motor specifications the proposed controller is simulated and output is shown in Fig 19. From the Table.5, in [42] ANFIS controller settles at 0.0611sec. In [43] ANFIS supervised controller settles a 0.036 sec. The proposed hybrid neuro fuzzy controller gives better settling time i.e 0.02 sec than above existing controllers.



**Figure 18.** Output of proposed controller for motor specifications in [26]



**Figure 19.** Output of proposed controller for motor specifications in [42, 43]

**Table 5.** Comparison of settling time between proposed Controller with other existing speed Controllers.

S.No.	Type of Controller	Reference Article	Settling Time (sec)	
			Reference Article	Proposed Method
1.	Hybrid Fuzzy-PI Controller	[26]	0.19	0.06
2.	ANFIS Controller	[42]	0.0611	0.02
3.	Fuzzy PID Supervised online ANFIS Controller	[43]	0.036	0.02

## 5. CONCLUSIONS

The adaptive neuro fuzzy controller is trained and tuned in such a way that it suits for the speed control of the BLDC motor drives. It exposes prominent and satisfactory responses under various operating conditions. Simulation results are shown to demonstrate the performance of BLDC motor drive. The

proposed controller gives good performance in comparison with classical controllers under different operating conditions like set point speed tracking, change in phase resistance, full load, no load, and varying load conditions. Further, it can be noticed that the proposed controller settles very faster, at 0.0045 secs with negligible steady state error, better rise time and very low integral absolute error compared to the traditional controllers.

### CONFLICT OF INTEREST

No conflict of interest was declared by the authors

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