Sakarya University Journal of Science

ISSN : 2147-835X Publisher : Sakarya University

Vol. 28, No. 3, 542-549, 2024 DOI: https://doi.org/10.16984/saufenbilder.1358209

Research Article

Anti-reflective coatings are effective in minimizing these losses. In our study, we used Fresnel equations to calculate reflectance values for single-layer SiO_2 , ZrO_2 , a $SiO₂$ -ZrO₂ mixture, and a double-layer $SiO₂/ZrO₂$ configuration. We then assessed their impact on crystalline silicon solar cells using the SCAPS program. The reflectance values of single-layer SiO_2 , ZrO_2 and $10\%SiO_2$ -90% ZrO_2 mixture were calculated as 19.17%, 13.09% and 13.01%, respectively. Notably, the double-layer $SiO₂/ZrO₂$ coating showed a low reflectance of 7.58%, a significant improvement compared to uncoated silicon at 37.45%. Efficiency values for crystalline silicon solar cells were calculated for single layer as 18,95% (SiO2), 20.39% (ZrO2), 20,40% (mixed coating) respectively and 21.68% for the double-layer SiO_2/ZrO_2

Theoretical Analysis and Simulation of SiO² and ZrO² Based Antireflective Coatings to Improve Crystalline Silicon Solar Cell Efficiency

İmran Kanma[z](https://orcid.org/0000-0001-8827-1590) D

Karadeniz Technical University, Faculty of Sciences, Department of Physics, Trabzon, Türkiye, imrankanmaz@ktu.edu.tr

 $ZrO₂$ $SiO₂$ SCAPS Article History: Received: 11.09.2023 Accepted: 08.05.2024

Online Available: 06.06.2024

Antireflection coating

1. Introduction

Zirconium dioxide $(ZrO₂)$ thin films are widely used in science, technology and industry, with various applications such as optical filters, photocatalysts, and transistors $[1-3]$. ZrO₂ is found in three different phases: monoclinic (1443K), tetragonal (1443-2643K) and cubic (2643-2953K) at different annealing temperatures and has a stable structure in these temperature ranges [4]. When the cubic phase of the $ZrO₂$ thin films is considered, it has a band gap of 6.1 eV and a refractive index of around 2 [5, 6]. Because of these properties of $ZrO₂$ thin films can be used as an anti-reflective coating for crystalline silicon solar cells. Anti-reflective coatings can be applied to the top surface of crystalline silicon solar cells as one or more layers of thin films. The minimum reflection condition of anti-reflective thin films is related to the thickness and refractive index of the thin films.

configuration.

These conditions can be expressed as [7],

$$
d_1 = \frac{\lambda_0}{4\eta_1} \tag{2}
$$

ZrO² thin films can be easily produced by methods such as vacuum evaporation, sputtering, pulsed laser deposition, ion-assisted deposition, ion beam sputtering, and Sol-gel [8-10]. However, it is important both in terms of time and cost to calculate the film thickness for the appropriate reflectance value of the film to be coated and to carry out the experiments in this direction. Therefore, the thickness value of the materials to be coated can be easily calculated with Fresnel equations to obtain the ideal reflectance value of the single-layer and doublelayer films. While some of the sun rays coming to the surface of the solar cell are reflected back from the surface, some of them may pass through the surface and cause current formation in the solar cell. By using anti-reflective coatings, light reflection can be reduced, and transmittance can be increased. In this way, higher efficiency solar cells can be produced. The Fresnel equations in which the reflection value is measured for anti-

 $n_1 = \sqrt{n_0 n_2}$ (1)

Cite as: İ. Kanmaz (2024). Theoretical Analysis and Simulation of SiO2 and ZrO2 Based Antireflective Coatings to Improve Crystalline Silicon Solar Cell Efficiency, *Sakarya University Journal of Science*, 28(3), 542-549. https://doi.org/10.16984/saufenbilder.1358209

reflective coatings are given in eq (3) and eq (4) for single layer and double layer, respectively.

$$
R_{SL} = |r^2| = \frac{r_1^2 + r_2^2 + 2r_1r_2\cos 2\theta}{1 + r_1^2r_2^2 + 2r_1r_2\cos 2\theta}
$$
 (3)

where;
$$
r_1 = \frac{n_0 - n_1}{n_0 + n_1}
$$
, $r_2 = \frac{n_1 - n_2}{n_1 + n_2}$, $\theta = \frac{2\pi n_1 d_1}{\lambda}$

$$
R_{DL} = \frac{A+B+C+D+E+F}{1+(r_1^2r_2^2)+(r_1^2r_3^2)+(r_2^2r_3^2)+C+D+E+F}
$$
 (4)

,

where;

$$
r_1 = \frac{n_0 - n_1}{n_0 + n_1}, r_2 = \frac{n_1 - n_2}{n_1 + n_2}, r_3 = \frac{n_2 - n_3}{n_2 + n_3}
$$

\n
$$
\theta_1 = \frac{2\pi n_1 t_1}{\lambda}, \ \theta_2 = \frac{2\pi n_2 t_2}{\lambda} \text{ and}
$$

\n
$$
A = r_1^2 + r_2^2 + r_3^2, B = r_1^2 r_2^2 r_3^2,
$$

\n
$$
C = 2r_1 r_2 (1 + r_3^2) \cos 2\theta_1,
$$

\n
$$
D = 2r_2 r_3 (1 + r_1^2) \cos 2\theta_2,
$$

\n
$$
E = 2r_1 r_3 \cos 2(\theta_1 + \theta_2),
$$

\n
$$
F = 2r_1 r_2^2 r_3 \cos 2(\theta_1 - \theta_2)
$$

In this study, reflectance calculations were made for the first layer of anti-reflective layer $ZrO₂$ thin film and for the second layer, $SiO₂$ thin films with good optical transmittance and passivation effect in solar cells [11], and average reflectance values were obtained. In order to investigate the antireflective effect of $SiO₂$ and $ZrO₂$ mixtures, the refractive index of the mixture at various ratios was calculated with the Arago-Biot (A-B) equation and the reflectance values were calculated. In addition, the different equations for calculating the refractive index of mixtures are expressed as;

$$
Argo-Biot (A-B): n=n_1\phi_1+n_2\phi_2 \qquad (5)
$$

n=Refractive index of mixture, n_1 =Refractive index of pure component-1, n_2 =Refractive index of pure component-2, ϕ_1 =Volume fraction of pure component-1 and ϕ_2 =Volume fraction of pure component-2 Where, also $\phi_1 = x_1 V_1 / \Sigma x_i V_i$ and $\phi_2 = x_2 V_2 / \Sigma x_i V_i$ here x is the mole fraction V_i is the molar volume of component i [12-14].

2. Methodology and Simulation

In our research, we conducted an analysis of the average reflectivity values for single-layer Zirconium Dioxide (ZrO2), Silicon Dioxide $(SiO₂)$, and double-layer $SiO₂/ZrO₂$ thin films, as well as the average reflectivity values of $SiO₂$ -ZrO² mixtures at varying ratios. These calculations were performed using eq (3) and eq (4). Furthermore, we determined the refractive indices of $SiO₂-ZrO₂$ mixtures with different composition ratios employing the Arago-Biot (A-B) formula presented in eq (5). Additionally, to explore the impact of average reflectivity values on crystalline silicon solar cell parameters, we employed the numerical simulation program SCAPS.

SCAPS is a versatile software tool capable of simulating various thin-film solar cell types, including solar cells, Copper Indium Gallium Selenide (CIGS) cells, Cadmium Telluride (CdTe) cells, Gallium Arsenide (GaAs) cells, crystalline silicon (c-Si) cells, and amorphous Silicon (a-Si:H) cells, as described in references [15, 16]. The SCAPS program performs calculations involving steady-state band diagrams, recombination profiles, and carrier transport in one dimension, based on Poisson's equation and the continuity equations for both holes and electrons [17].

3. Result and Discussion

This study was conducted in three sequential stages. In the initial stage, we computed the reflectance values of single-layer ZrO_2 , SiO_2 , and double-layer SiO_2/ZrO_2 thin films using Fresnel equations. Subsequently, in the second stage, we determined the refractive indices of $SiO₂$, $ZrO₂$, mixtures across various ratios and calculated reflectance values dependent on fim thickness.

Finally, in the third stage, we applied the average reflectance values of single-layer $SiO₂$, $ZrO₂$, $SiO₂-ZrO₂$ mixtures, and double-layer $SiO₂/ZrO₂$ thin films as anti-reflective coatings to crystalline silicon (c-Si) solar cells using the SCAPS solar cell program. To calculate the reflectance values of $SiO₂$ and $ZrO₂$ thin films at different thicknesses, we systematically varied the thicknesses from 30nm to 100nm and summarized the obtained reflectance values in Figure 1.

Figure 1. Reflective values of single-layer $ZrO_2(a)$ single-layer SiO₂ (b), double layer SiO₂/ $ZrO_2(c)$ and average reflectance values (d) average reflectance values (d)

As depicted in Figure 1(a), for $ZrO₂$ thin films with low thicknesses, high reflectance values were observed. With increasing thickness, both the reflectance values significantly decreased, and the minimum reflectance point shifted towards longer wavelengths. Figure 1(d) illustrates that the lowest average reflectance value for $ZrO₂$ thin films, 13.09%, was achieved at a thickness of 70nm. Additionally, as the thickness of the single-layer $SiO₂$ thin film increased, the average reflectance values decreased, reaching a minimum of 19.17% for a thickness of 90nm.

By employing multiple anti-reflective layers in solar cells, the reflective properties can be further reduced, thereby enhancing solar cell efficiency [18]. The reflectance values of double-layer antireflective coatings can be readily calculated

using Eq (4). The thickness of the $ZrO₂$ thin film, previously determined as the optimal thickness, was held constant at 70nm, while the thickness of the SiO² thin film was varied between 30nm and 100nm. in order to achieve the lowest reflectance value. The reflectivity of the SiO_2/ZrO_2 doublelayer thin film decreased from 12.01% to its lowest point of 7.58% when the $SiO₂$ thin film reached a thickness of 80nm. When the thickness of the $SiO₂$ thin film was increased from 80nm to 100nm, the average reflectivity value increased from 7.58% to 8.05%. In the literature, it is commonly observed that double-layer thin films offer advantages in terms of anti-reflective properties, leading to lower levels of reflection compared to single-layer thin films [19, 20]. When two materials with different refractive indices are mixed at different rates, the refractive

index of the mixture is expected to be a value between the refractive indices of both materials included in the mixture $(n_{Low} < n_{Mix} < n_{High})$.

Based on the refractive indices of $SiO₂$ and $ZrO₂$ materials, the refractive indices of $SiO₂-ZrO₂$ mixtures at different ratios were calculated using eq (5) at nine different ratios

Figure 2. Graph of the reflectance of three different ratios of $SiO₂$ - $ZrO₂$ mixed

Considering the refractive index of $SiO₂$ as 1.44 [21] and of $ZrO₂$ as 2.05 [22], it is clearly seen from table 1 that the refractive index of $SiO₂$ -ZrO² mixture varies between 1.49 and 1.93. Eq (5) was used for the refractive index of each $SiO₂-ZrO₂$ ratios, and the reflectance values were calculated with the eq (3) by changing the thin film thicknesses from 30nm to 100nm. Calculations were made by taking molarity of $SiO₂$ and $ZrO₂$ as equal. It was seen that the mole fractions of $SiO₂$ and $ZrO₂$ changed in direct proportion to $V_{SiO2}/(V_{SiO2}+V_{ZrO2})$ and $V_{ZrO2}/(V_{SiO2}+V_{ZrO2})$, respectively.

The reflection-wavelength graph for three different ratios $(10\%SiO₂-90\%ZrO₂, 50\%SiO₂-$

 50% ZrO₂, 90% SiO₂-10%ZrO₂) is given in figure 2. It can be clearly seen from table 1 that the lowest average reflectance value of 10% SiO₂-90%ZrO² mixture was calculated as 13.01% for the 70nm thickness. It was also noted that as the $SiO₂$ ratio in the mixture increased, the refractive index of the mixture decreased and therefore the average reflectance values decreased. In addition, as the $SiO₂$ ratio increases, the thin film thickness required to be coated in order to obtain low reflectance values also increases.

Figure 3. Reflection-wavelength graphs of different thin films

When the refractive indices of $SiO₂-ZrO₂$ mixtures at different ratios were examined, it was seen that the average reflectance value decreased as the refractive index approached 2. Unfortunately, the desired reflection values cannot be achieved even if ideal refractive index materials are produced for anti-reflective coatings with the mixture of two different materials in different ratios. From the reflectance wavelength graphs given in figure 3, it is clearly seen that the reflectance values of double layer $SiO₂/ZrO₂$ thin films give better results compared to the single layer reflectance values. While the best reflectance value in single layer layers was 13.01% for 10% SiO₂-90%ZrO₂ thin film, this value decreased to 7.58% for double layer $SiO₂/ZrO₂$ thin film. Therefore, multi-layer antireflective coatings are highly preferred for highefficiency solar cells due to their low reflectance values [23].

The average reflectance values of single layer $SiO₂$, single layer $ZrO₂$, single layer %10SiO₂-

%90ZrO₂ mixed and double layer $SiO₂(80nm)/ZrO₂(70nm)$ thin films and the initial parameters of the crystalline silicon solar cell given in table 2 were used together in the SCAPS program to investigate the effect of antireflective coatings on the crystalline silicon solar cell. Figure 4 shows a schematic representation of conventional crystalline silicon solar cells.

Figure 4. Schematic representation of Crystalline silicon solar cell

The current-voltage graph of this solar cell is given in figure 5 and the parameters of the solar cell are summarized in table 3. As can be seen from table 3, anti-reflective coatings have a great effect on solar cell parameters. For the uncoated c-Si solar cell, the V_{oc} , J_{cs} , FF and efficiency values were calculated as 752.20V, 25.48mA/cm^2 , , 82.80% and 14.63%, respectively, and serious improvements were achieved on the solar cell parameters by applying anti-reflective coating to the solar cells. For example, the efficiency values for single layer SiO₂ increased from 14.63% to 18.95% compared to the uncoated solar cell. In addition, the efficiency values for single layer $ZrO₂$, single layer 10% SiO₂-90%ZrO₂ mixed and double layer SiO2-ZrO² were recorded as 20.39%, 20.40% and 21.68%, respectively

Table 2. Some initially parameters of c-Si solar cell for SCAPS [24]

	n^*	$p-Si$	p^* -Si-Bsf
Thickness (μm)	0.3	200	7
Bandgap (eV)	1.12	1.12	1.12
Electron affinity (eV)	4.05	4.05	4.05
Dielectric permittivity	11.90	11.90	11.90
CB effective density of states cm^{-3})	$4.79x10^{18}$	2.80×10^{19}	$2.80x10^{19}$
VB effective density of states cm^{-3})	4.52×10^{18}	$1.04x10^{19}$	$1.04x10^{19}$
Electron mobility (cm^2/Vs)	73.36	1041	202
Hole mobility cm^2/Vs)	155.6	412	77
Shallow uniform donor density N_D (cm ⁻³)	$1x10^{20}$	$1x10^{16}$	
Shallow uniform acceptor density N_A (cm ⁻³)		$1x10^{16}$	$1x10^{19}$

Figure 5. I-V graphics of crystalline silicon solar cell of uncoated and different anti-reflective coating

4. Conclusions

This study investigated the potential of antireflective coatings, specifically single-layer $SiO₂$, $ZrO₂$, $SiO₂-ZrO₂$ mixtures, and doublelayer SiO_2/ZrO_2 thin films, to enhance the performance of crystalline silicon solar cells. Reflectance calculations and refractive index assessments were conducted for various coating configurations, and their impact on solar cell efficiency was investigated using the SCAPS program. The results demonstrated significant improvements in solar cell parameters with the application of anti-reflective coatings. Singlelayer $SiO₂$, $ZrO₂$, and $SiO₂-ZrO₂$ mixtures all showed enhanced efficiency compared to uncoated solar cells. Furthermore, the doublelayer SiO_2/ZrO_2 configuration exhibited the highest efficiency among the coatings studied.

These findings emphasize the critical role of antireflective coatings in increasing the efficiency of crystalline silicon solar cells, paving the way for more efficient and sustainable solar energy conversion technologies. The utilization of multi-layer anti-reflective coatings, such as double-layer SiO_2/ZrO_2 , is particularly

promising for achieving low reflectance values and maximizing solar cell performance.

Article Information Form

Funding

The author (s) has no received any financial support for the research, authorship or publication of this study.

The Declaration of Conflict of Interest/ Common Interest

No conflict of interest or common interest has been declared by the authors.

The Declaration of Ethics Committee Approval This study does not require ethics committee permission or any special permission.

The Declaration of Research and Publication Ethics

The authors of the paper declare that they comply with the scientific, ethical and quotation rules of SAUJS in all processes of the paper and that they do not make any falsification on the data collected. In addition, they declare that Sakarya University Journal of Science and its editorial board have no responsibility for any ethical

violations that may be encountered, and that this study has not been evaluated in any academic publication environment other than Sakarya University Journal of Science.

Copyright Statement

Authors own the copyright of their work published in the journal and their work is published under the CC BY-NC 4.0 license.

References

- [1] T. Yamaguchi, "Application of $ZrO₂$ as a catalyst and a catalyst support", Catalysis today, vol. 20, pp. 199-217, 1994.
- [2] Q. Zhang, X. Li, J. Shen, G. Wu, J. Wang, L. Chen, "ZrO₂ thin films and ZrO₂/SiO₂ optical reflection filters deposited by sol– gel method", Materials Letters, vol. 45 pp. 311-314, 2000.
- [3] J. H. Park, Y. B. Yoo, K. H. Lee, W. S. Jang, J. Y. Oh, S. S. Chae, H. W. Lee, S. W. Han, H. K. Baik, "Boron-doped peroxozirconium oxide dielectric for highperformance, low-temperature, solutionprocessed indium oxide thin-film transistor", ACS applied materials & interfaces, vol. 5 pp. 8067-8075, 2013.
- [4] G. Balakrishnan, P. Kuppusami, S. Murugesan, C. Ghosh, R. Divakar, E. Mohandas, D. Sastikumar, "Characterization of Al_2O_3/ZrO_2 nano multilayer thin films prepared by pulsed laser deposition", Materials Chemistry and Physics, vol. 133 pp. 299-303, 2012
- [5] W. J. Shin, W.-H. Huang, M. Tao, "Lowcost spray-deposited $ZrO₂$ for antireflection in Si solar cells", Materials Chemistry and Physics, vol. 230, pp. 37- 43, 2019.
- [6] U. Sikder, M. A. Zaman, "Optimization of multilayer antireflection coating for photovoltaic applications", Optics & Laser Technology, vol.79, pp. 88-94, 2016.
- [7] A. J. Thosar, M. Thosar, R. Khanna, "Optimization of anti-reflection coating for

improving the performance of GaAs solar cell", Indian Journal of Science and Technology, vol. 7 pp. 637-641, 2014.

- [8] M. Epifani, C. Giannini, L. Tapfer, L. Vasanelli, "Sol–gel synthesis and characterization of Ag and Au nanoparticles in $SiO₂$, TiO₂, and ZrO₂ thin films", Journal of the American Ceramic Society, vol. 83 pp. 2385-2393, 2000.
- [9] J. Čyvienė, M. Laurikaitis, J. Dudonis, "Deposition of nanocomposite Zr–ZrO2 films by reactive cathodic vacuum arc evaporation", Materials Science and Engineering: B, vol. 118, pp. 238-241, 2005.
- [10] D. Panda, T.-Y. Tseng, "Growth, dielectric properties, and memory device applications of ZrO₂ thin films", Thin Solid Films, vol. 531 pp. 1-20, 2013.
- [11] A. Uzum, I. Kanmaz, "Passivation properties of $HfO₂-SiO₂ mixed metal oxide$ thin films with low reflectivity on silicon substrates for semiconductor devices", Thin Solid Films, vol. 738 pp. 138965, 2021.
- [12] M. A. Khan, M. Sohel, M.A. Islam, F. I. Chowdhury, S. Akhtar, "Refractive Indices of Aqueous Solutions of Isomeric Butylamines at 303.15 K: Experimental and Correlative Approach", Journal of Applied Science & Process Engineering, vol. 8 pp. 1020-1030, 2021.
- [13] S. Sharma, P. B. Patel, R. S. Patel, J. Vora, "Density and comparative refractive index study on mixing properties of binary liquid mixtures of eucalyptol with hydrocarbons at 303.15, 308.15 and 313.15 K", E-Journal of Chemistry, vol. 4 pp. 343-349, 2007.
- [14] F. Pretorius, W. W. Focke, R. Androsch, E. du Toit, "Estimating binary liquid composition from density and refractive index measurements: A comprehensive review of mixing rules", Journal of Molecular Liquids, vol. 332 pp. 115893, 2021.
- [15] A. Kowsar, M. Billah, S. Dey, S. C. Debnath, S. Yeakin, S. F. U. Farhad, "Comparative Study on Solar Cell Simulators, in: 2019" 2nd International Conference on Innovation in Engineering and Technology (ICIET), IEEE, 2019, pp. 1-6.
- [16] S. M. Seck, E. N. Ndiaye, M. Fall, S. p. Charvet, "Study of efficiencies CdTe/CdS photovoltaic solar cell according to electrical properties by scaps simulation", Natural Resources, vol. 11 pp. 147-155, 2020.
- [17] A. Teyou Ngoupo, S. Ouédraogo, J. Ndjaka, "Numerical analysis of interface properties effects in CdTe/CdS: O thin film solar cell by SCAPS-1D", Indian Journal of Physics, vol. 93 pp. 869-881, 2019.
- [18] W. Zhang, K. Hu, J. Tu, A. Aierken, D. Xu, G. Song, X. Sun, L. Li, K. Chen, D. Zhang, "Broadband graded refractive index $TiO₂/Al₂O₃/MgF₂$ multilayer antireflection coating for high efficiency multi-junction solar cell", Solar Energy, vol. 217 pp. 271- 279, 2021.
- [19] K. Ali, S. A. Khan, M. M. Jafri, "Effect of double layer (SiO2/TiO2) anti-reflective coating on silicon solar cells", Int. J. Electrochem. Sci, vol. 9 pp. 7865-7874, 2014
- [20] M. A. Zahid, M. Q. Khokhar, S. Park, S. Q. Hussain, Y. Kim, J. Yi, "Influence of Al2O3/IZO double-layer antireflective coating on the front side of rear emitter silicon heterojunction solar cell", Vacuum, vol. 200, pp. 110967, 2022.
- [21] S.-Y. Lien, D.-S. Wuu, W.-C. Yeh, J.-C. Liu, "Tri-layer antireflection coatings $(SiO₂/SiO₂–TiO₂/TiO₂)$ for silicon solar cells using a sol–gel technique", Solar Energy Materials and Solar Cells, vol. 90, pp. 2710-2719, 2006.
- [22] F. Karaömerlioğlu, E. Mehmetov, "Optical Properties and Technological Applications

of Multilayer Antireflection Coatings", vol. 19 pp. 1-6, 2008.

- [23] X. Xiao, H. Z. Liu, J. Tu, "Multilayer antireflection coatings design for SiO2‐ passivated silicon solar cells", Materialwissenschaft und Werkstofftechnik, vol. 53 pp. 80-88, 2022.
- [24] İ. Kanmaz, "Simulation of CdS/p-Si/p+-Si and ZnO/CdS/p-Si/p+-Si Heterojunction Solar Cells", Results in Optics, pp. 100353, 2023.