

## Elastic, Electronic, Dynamic and Thermodynamic Properties of YbPdH<sub>3</sub>

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### Keywords

first principles calculation,  
hardness, elastic properties,  
machinability, anisotropy.

**Abstract:** A comprehensive computational investigation has been carried out for YbPdH<sub>3</sub> via first principles calculations for the first time. Structural, electronic and thermodynamic properties are obtained. The obtained lattice constant of YbPdH<sub>3</sub> is in a good agreement with the existing literature. Subsequently, the elastic constants are obtained and used to compute several parameters such as anisotropy, hardness, Cauchy pressure, shear and Young modulus, machinability index and Poisson's ratio. According to Born stability criteria, YbPdH<sub>3</sub> is mechanically stable material. Cauchy pressure and Poisson's ratio indicates ductile nature. The anisotropy factor indicates anisotropic nature almost in every direction for Young modulus, shear modulus, linear compressibility and Poisson's ratio. The machinability index (B/C<sub>44</sub>) is found to be 2.88 whereas Vickers hardness of YbPdH<sub>3</sub> is computed via Chen's model as 2.965. The electronic band structure of YbPdH<sub>3</sub> demonstrates metallic characteristics since there is no band gap between valence and conduction band. The thermodynamic properties such as Debye temperature, Debye vibrational energy, vibrational free energy, entropy, heat capacity and melting temperature of YbPdH<sub>3</sub> are also obtained. The heat capacity seems to reach its Dulong-Petit limit at about 300 K.

## YbPdH<sub>3</sub>'ün Elastik, Elektronik, Dinamik ve Termodinamik Özellikleri

### Anahtar Kelimeler

İlk prensip hesaplamaları,  
sertlik, elastik özellikler,  
işlenebilirlik, anizotropi.

**Öz:** YbPdH<sub>3</sub> için ilk kez ilk prensip hesaplamaları yoluyla kapsamlı bir hesaplamalı araştırma yapıldı. Yapısal, elektronik ve termodinamik özellikler elde edildi. YbPdH<sub>3</sub>'ün elde edilen örgü sabiti mevcut literatürle iyi bir uyum içindedir. Daha sonra elastik sabitler elde edildi ve anizotropi, sertlik, Cauchy basıncı, kayma ve Young modülü, işlenebilirlik indeksi ve Poisson oranı gibi çeşitli parametreleri hesaplamak için kullanıldı. Born stabilite kriterlerine göre YbPdH<sub>3</sub> mekanik olarak stabil bir malzemedir. Cauchy basıncı ve Poisson oranı sünek yapıyı gösterir. Anizotropi faktörü Young modülü, kayma modülü, doğrusal sıkıştırılabilirlik ve Poisson oranı için neredeyse her yönde anizotropik doğayı göstermiştir. İşlenebilirlik indeksi (B/C<sub>44</sub>) 2.88 olarak bulunurken YbPdH<sub>3</sub>'ün Vickers sertliği Chen modeliyle 2.965 olarak hesaplandı. YbPdH<sub>3</sub>'ün elektronik bant yapısı, değerlik ve iletim bandı arasında bant aralığı olmadığından metalik özellikler göstermektedir. YbPdH<sub>3</sub>'ün Debye sıcaklığı, Debye titreşim enerjisi, titreşim serbest enerjisi, entropi, ısı kapasitesi ve erime sıcaklığı gibi termodinamik özellikleri de elde edilmiştir. Isı kapasitesi yaklaşık 300 K'da Dulong-Petit sınırına ulaşmış gibi görülmüştür.

### 1. Introduction

To date, several hydrides have been under investigation for several reasons such as superconductivity and hydrogen storage. YbPdH<sub>3</sub> is a perovskite type hydride which contains hydrogen in its structure. It might be a possible candidate for

hydrogen storage. Its application can be carried out both as conducting material or storage material. Hydrogen storage requires a couple of conditions such as cost, safety, high concentration storage capacity, kinetic etc. In general, there are two types of hydrogen storage methods, these are physisorption and chemisorption. While physisorption is based on weak

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interaction between the host material and hydrogen molecules, chemisorption is based on the chemical reaction of the host material and hydrogen and a new hybrid phase is formed. Recently, hydrogen storage in perovskite hydrides with high gravimetric density has been extensively investigated alongside metal hydrides. There are very few studies exist in literature on YbPdH<sub>3</sub> [1, 2], in which only electronic properties were investigated. In this study, a thorough investigation on YbPdH<sub>3</sub> has been done to reveal its extensive properties.

Hydrogen storage materials and technology are crucial to promoting hydrogen use and fuel cell energy in stationary and portable power sources and transportation. The bottleneck of using hydrogen as an energy carrier is storing hydrogen in an efficient way. A couple of hydrogen storage methods have been proposed and investigated last a few decades such as gaseous form in high pressure, liquid form in low temperature and solid-state storage. High pressure gaseous form is limited to heavy tanks, poor safety and possible leakage. High strength materials should be reinforced for pressure vessels which brings extra costs and limited gravimetric hydrogen density.

Moreover, compressing gases leads to release of heat including hydrogen, therefore a pre-cooling system of hydrogen is required when compressing. Liquid form requires low temperature which leads to addition of cooling system that decreases the efficiency of it. This procedure requires a good thermal insulation of the tank, otherwise the heat transfer between the tank and environment will lead to release of hydrogen (boil-off) from the valves. To sum up, both ways bring extra costs, strict regulations, and safety concerns, especially for mobile applications. Thus, explosion, flammability, toxicity etc. are not desired for hydrogen storage. Compared to these two methods, solid state hydrogen storage provides superior safety and allows to operate at appropriate pressure and temperature. The biggest obstacle to the use of hydrogen as a fuel is the lack of materials with suitable gravimetric density. To overcome this problem, an interactive approach is needed where materials can be synthesized with sufficient storage capacity at higher densities. Hence, it is crucial to carry out a theoretical computation for this capacity. Along with various parameters, gravimetric hydrogen density (GHD) is a significant parameter is computed for hydrides for hydrogen. The GHD of YbPdH<sub>3</sub> is obtained as follows [3]:

$$C_{wt\%} = \left( \frac{(H/M)^{M_H}}{M_{Host} + (H/M)^{M_H}} \times 100 \right) \% \quad (1)$$

In the equation H/M donates for hydrogen to metal ratio, M<sub>H</sub> donates for molar mass of hydrogen and M<sub>Host</sub> donates for molar weight of host material. The GHD value of YbPdH<sub>3</sub> is computed as 1.06 wt.%.

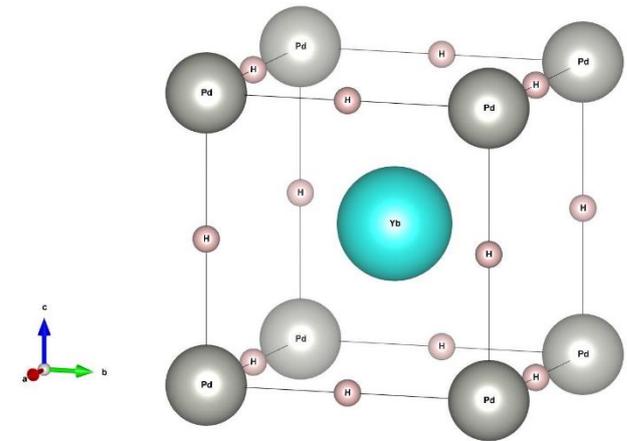
## 2. Materials and Methods

Quantum Espresso code was utilised to carry out calculations. The plane wave pseudopotential approach was adopted within the Quantum Espresso [4, 5]. The GGA (generalized gradient approximation) by Perdew, Burke, and Ernzerhof (PBE) was used to treat electronic exchange correlation potentials [6]. The cut-off energy for the maximum plane wave was adopted as 60 Ry while the basis cut-off was taken as 600 Ry for the electronic charge density. A 8×8×8 k point grid was used to integrate Brillouin-zone. The smearing parameter is taken as  $\sigma = 0.01$  Ry for integration up to Fermi level [7]. Stress-strain approach within thermo-pw program was adopted to compute elastic constants within Quantum Espresso. The thermodynamic properties under constant volume were obtained by using the Gibbs2 code with semi-harmonic approximation (QHA). The thermodynamic properties were obtained using the energy-strain method applied in the thermo-pw code.

## 3. Results

### 3.1 Physical Properties

YbPdH<sub>3</sub> crystalizes in cubic structure with the space group  $Pm\bar{3}m$  (No. 221), its crystal structure representative is given in Figure 1. The computed lattice constant for YbPdH<sub>3</sub> is found as 3.696 Å which is the similar value given in Materials Project (3.66 Å). The mechanical properties of materials are generally evaluated by stiffness (elastic) constants  $C_{ij}$ . The stiffness constants help to understand the material's behavior such as hardness, ductility, bonding, machinability, brittleness, anisotropy and mechanical stability. In general, mechanical stability evaluation of materials are carried out by examining the material's respond in any application under static stress via elastic stiffness.



**Figure 1.** The crystal structure representative of YbPdH<sub>3</sub>.

The computation of elastic stiffness is explained in refs [8, 9]. The computed various parameters by using elastic stiffness are presented in Tables 1, 2 and 3.

There are three elastic stiffness are given for a cubic structure known as  $C_{11}$ ,  $C_{12}$ ,  $C_{44}$ . Max Born suggested a stability criteria for mechanical stability as [10]:

$$(C_{11} - C_{12}) > 0, C_{11} > 0, C_{44} > 0, (C_{11} + 2C_{12}) > 0 \quad (2)$$

Equation 2 can lead to;

$$C_{12} < B < C_{11} \quad (3)$$

The computed elastic stiffness of YbPdH<sub>3</sub> satisfy the conditions given in Equation 2 and 3. Therefore, it can be concluded that YbPdH<sub>3</sub> is mechanically stable material. Elastic stiffness of materials can also provide information about material's resistance along difference directions. The value of  $C_{11}$  is an indication of material's response towards linear compression along [100]. Since  $C_{11}$  value is greater than that of  $C_{12}$  and  $C_{44}$ , resistance to linear compression is greater for YbPdH<sub>3</sub>.

B of the materials indicate resistance of them towards fracture whereas G shows resistance towards plastic deformation. Higher  $C_{44}$  value also implies higher G which increases plasticity [11]. From Table 2, it can be predicted that YbPdH<sub>3</sub> has some plasticity and stiffness. Cauchy pressure ( $C_p$ ) provides information about angular characteristics of materials. More positive  $C_p$  implies predominance of ionic bonding whereas more negative  $C_p$  indicates covalent bonding predominance. It is stated by Pettifor [12] that Cauchy pressure ( $C_p = C_{12} - C_{44}$ ) can tell about bonding characteristics of the materials along with the fracture. In the case of negative Cauchy pressure, the material tends to show directional bonding characteristics with angular or covalent bonding and brittle nature. In the case of more positive Cauchy pressure, the material tends to exhibit metallic and ductile nature. The  $C_p$  of YbPdH<sub>3</sub> is computed as 58.23 GPa which suggests predominance of ionic bonding within YbPdH<sub>3</sub>. In addition,  $C_p$  can give an idea about brittleness and ductility of given material. Positive  $C_p$  indicates ductility [13].

The ductility and brittleness of the materials can be analyzed by using Pugh's criteria [14] and Frantsevich's rule [15]. Pugh's criteria distinguish materials based on the B/G ratio. Higher B/G ratio displays ductility and lower B/G ratio implies brittleness; the borderline is specified as 1.75. According to Frantsevich, materials with  $\sigma$ , lower than  $\sigma \sim 0.26$  are brittle and higher than 0.26 are ductile. As can be seen from Table 2 that, the computed B/G ratio is 5.51 and  $\sigma$  is 0.41 which suggests the ductile nature of YbPdH<sub>3</sub>.

B/ $C_{44}$  ratio is defined as machinability index [17], if  $C_{44}$  is low, machinability index is high which is the case for softer materials. If the hardness of the material is high, machinability index is lower. Hardness of the material

is computed using the Chen's model [18] and presented in Table 3.

**Table 1.** The calculated lattice constants ( $a$ , Å), Bulk modulus ( $B$ , GPa), elastic constants ( $C_{11}$ ,  $C_{12}$ ,  $C_{44}$ , GPa) and Cauchy Pressure ( $C_p$ ) of YbPdH<sub>3</sub>.

Material	a	B	C <sub>11</sub>	C <sub>12</sub>	C <sub>44</sub>	C <sub>12</sub> -C <sub>44</sub> (C <sub>p</sub> )
YbPdH <sub>3</sub>	3.696	95.57	103.95	91.39	33.16	58.23
		3.710				
YbPdH <sub>3</sub> [1, 16]						

**Table 2.** The calculated Bulk modulus (B,GPa), Shear modulus (G, GPa), B/G ratios, Poisson's ratios ( $\sigma$ ) and Young's modulus (E, GPa) of YbPdH<sub>3</sub>.

Material	B	G	B/G	$\sigma$	E
YbPdH <sub>3</sub>	95.57	17.32	5.51	0.41	48.77

**Table 3.** The computed anisotropy factor (A), melting temperature (T<sub>m</sub>, K), Vickers hardness ( $H_v^G$ ,  $H_v^E$ , GPa) and machinability index (B/ $C_{44}$ ) of YbPdH<sub>3</sub>.

Material	A	$\theta$	T <sub>m</sub>	$H_v^G$	$H_v^E$	B/ $C_{44}$
YbPdH <sub>3</sub>	5.28	206.34	1167.3	0.164	2.965	2.88

By adopting elastic stiffness B, G, E,  $H_v^G$ ,  $H_v^E$  and B/ $C_{44}$  are obtained. The calculated hardness values for YbPdH<sub>3</sub> are;  $H_v^G = 0.164$  and  $H_v^E = 2.965$  thus, it can be predicted that YbPdH<sub>3</sub> is not a hard material. In general, materials with Vickers hardness value above 10 GPa is defined as hard material and materials with a hardness value greater than 40 GPa are defined as super hard materials [19].

As well as elastic properties, melting temperatures (T<sub>m</sub>) can also be obtained by using elastic constants. T<sub>m</sub> provides an idea about practicability and reliability of the materials. For a cubic structure, T<sub>m</sub> can be computed by using  $T_m = 553 + 5.91 C_{11}$  relation [18]. The computed T<sub>m</sub> for YbPdH<sub>3</sub> is 1167.3 K which suggests that this material can be used for high temperature applications.

Debye temperature ( $\theta$ ) is also a significant value which describes the temperature at which the vibration wavelengths of atoms are equal to the unit cell length [20].  $\theta$  is a parameter that can be used with the inherent properties of the elastic lattice vibrations and can be computed through the average elastic wave velocity (V<sub>m</sub>). Several thermodynamic properties can be obtained using  $\theta$  such as specific heat capacity, thermal expansion and thermal conductivity.  $\theta$  of YbPdH<sub>3</sub> is obtained as 206.34 K.

Deformation do not occur for brittle materials; however, it is expected for ductile materials before fracture. The crystal anisotropy can have an effect on plastic deformation and fracture. Anisotropy of the

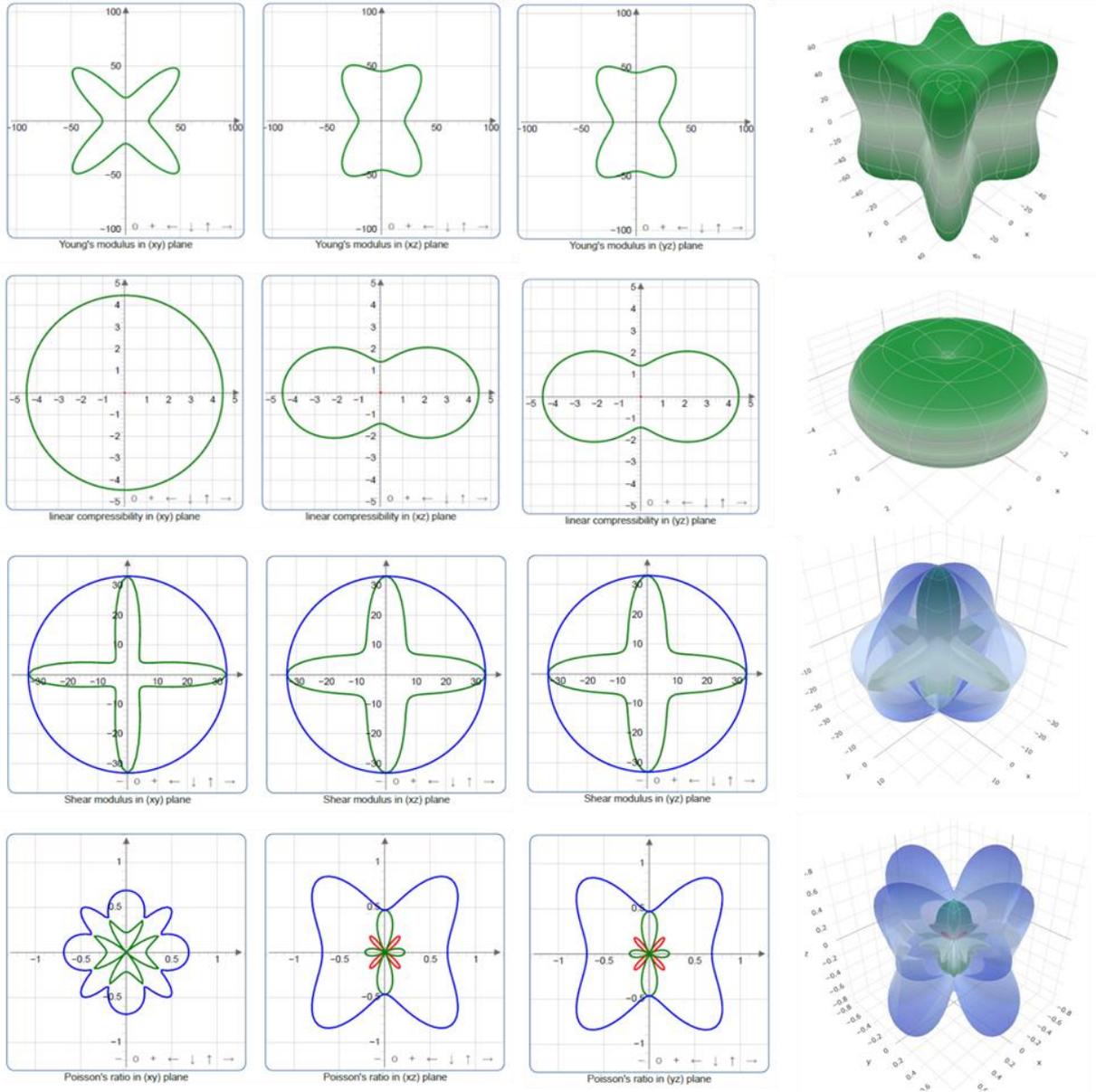
materials affect the physical properties in different directions. Thus, the anisotropy factor of YbPdH<sub>3</sub> has been computed by using  $A = 2C_{44} / C_{11} - C_{12}$  relation [21]. The calculated anisotropy factor is given as 5.28 in Table 3 which indicates anisotropic characteristics of YbPdH<sub>3</sub>. The 2D and 3D dimensional change of E, linear compressibility, G and  $\sigma$  is computed using the ELATE program and given in Figure 2. YbPdH<sub>3</sub> exhibits anisotropic behaviour almost in every direction.

Linear compressibility in xy plane seems to be isotropic, and other properties are anisotropic in all directions.

Similar anisotropic behaviours were observed for LiCaH<sub>3</sub> and NaCaH<sub>3</sub> previously [22].

### 3.2 Electronic Properties

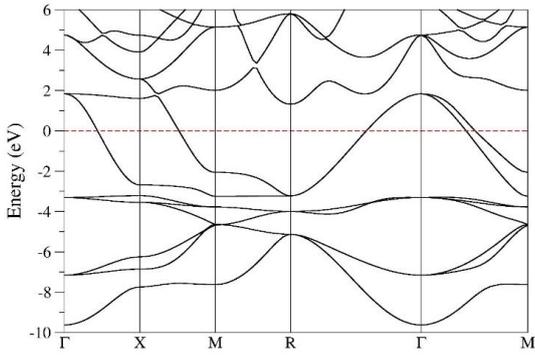
The electronic properties of YbPdH<sub>3</sub> have also been investigated. The electronic band structure and total (TDOS) and partial densities of states (PDOS) are given in Figure 3 and Figure 4.



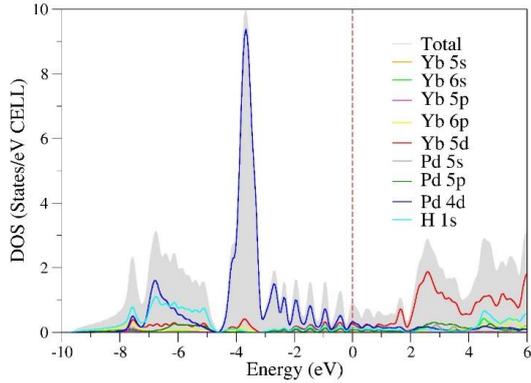
**Figure 2:** The 2D and 3D directional change of Young Modulus, linear compressibility, Shear modulus and Poisson's ratio of YbPdH<sub>3</sub>.

The band gap describes the region between valence and conduction band where electrons cannot occupy. Figure 3 demonstrates no band gap around Fermi energy level (set to 0 eV) since valence and conduction band overlaps, thus it can be easily predicted that

YbPdH<sub>3</sub> shows metallic behaviour. Figure 4 displays detailed contributions to the conductivity of YbPdH<sub>3</sub>. The contribution of d states of Pd is dominated in the valence band along with s states of H, whereas d states of Yb dominate to the conduction band.



**Figure 3.** Electronic band structure of YbPdH<sub>3</sub>.



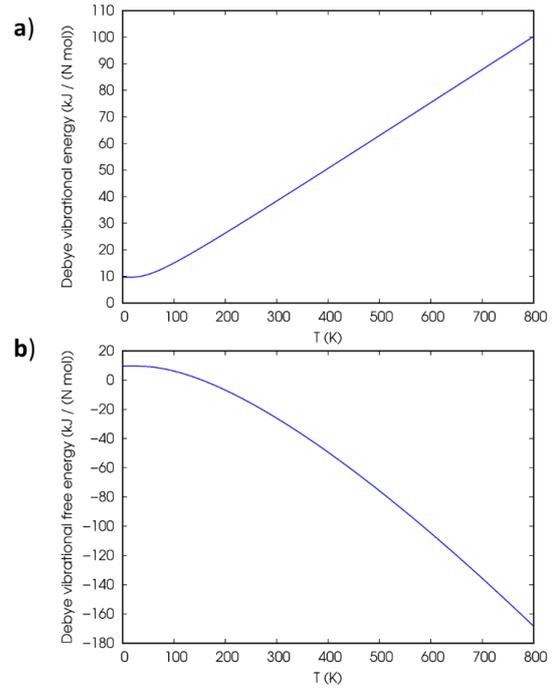
**Figure 4.** The TDOS and PDOS of YbPdH<sub>3</sub>.

### 3.3 Thermodynamic Properties

The thermodynamic properties are computed for YbPdH<sub>3</sub>. The internal energies of YbPdH<sub>3</sub> are shown in Figure 5. Debye vibrational energy seems to increase linearly with the increasing temperature. Debye vibrational free energy in Figure 5b seems to be more negative as the temperature increases. Materials with more negative Debye vibrational free energy seem to have better thermal response since they will have better thermodynamic stability at high temperatures.

Entropy of YbPdH<sub>3</sub> rises with the temperature as shown in Figure 6a. This is expected since as the temperature increases the kinetic energy and motion of atoms increase. Also, the entropy is zero at zero temperature which obeys the third law of thermodynamics. In addition, entropy can be related to vibrational free energy since vibrational free energy is obtained entropy. The more negative vibrational free energy, the higher entropy [23].

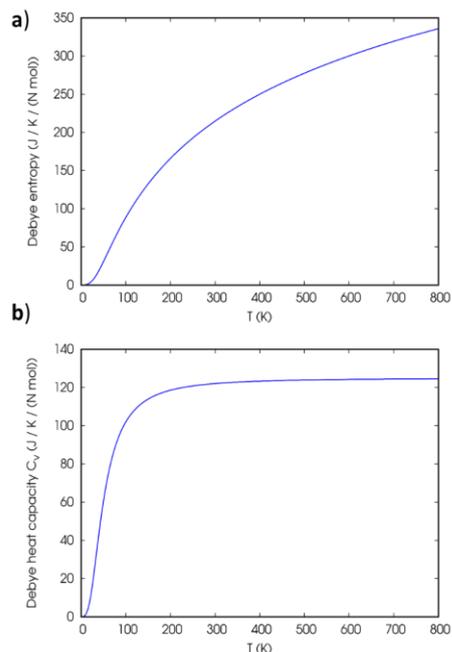
The heat capacity of YbPdH<sub>3</sub> is given in Figure 6b. As can be seen from the figure that there is a sharp increase in heat capacity with the temperature between 0-150 K. After that, a slight increase can be observed up until 250 K. Around 300 K, the heat capacity reaches its Dulong-Petit limit about 120 JNm<sup>-1</sup>K<sup>-1</sup>.



**Figure 5.** Debye vibrational energy (a) and free energy (b) of YbPdH<sub>3</sub>.

## 4. Discussion and Conclusion

The development of viable solid-state hydrogen storage materials primarily relies on the theoretical study of new materials and their properties. In this context, first principles calculations form the basis and allow discovery of new materials. In this sense, the structural, elastic, mechanical, anisotropic behavior and thermodynamic properties of YbPdH<sub>3</sub> has been investigated by means of first principles calculations. The mechanical stability is evaluated by using elastic constants and Born stability criteria, the result indicates mechanical stability for YbPdH<sub>3</sub>.



**Figure 6.** Debye entropy (a) and heat capacity (b) of YbPdH<sub>3</sub>.

Along with elastic constants several parameters such as  $C_p$ ,  $G$ ,  $E$ ,  $\sigma$ ,  $\theta$ , machinability index, hardness and  $T_m$  of YbPdH<sub>3</sub> are obtained. According to obtained values, YbPdH<sub>3</sub> is a ductile and anisotropic material. The electronic band structures show a metallic character with the highest contribution to the conduction band Pd 4d states. In addition, Debye vibrational energy, vibrational free energy, entropy and heat capacity of YbPdH<sub>3</sub> are obtained. As far as the author's knowledge these properties have been studied for the first time for YbPdH<sub>3</sub>.

### Declaration of Ethical Code

*In this study, we undertake that all the rules required to be followed within the scope of the "Higher Education Institutions Scientific Research and Publication Ethics Directive" are complied with, and that none of the actions stated under the heading "Actions Against Scientific Research and Publication Ethics" are not carried out.*

### References

- [1] Orgaz E. , Mazel V., Gupta M. 1996. Electronic structure and electron-phonon coupling in stoichiometric and defective hydrides MPdH<sub>3</sub> (M= Ca, Sr, Eu, Yb). Journal of Physical Review B, 54(22), 16124.
- [2] Orgaz E., Mazel V., Gupta M. 1997. Internal pressure effect in the series of perovskite structure hydrides: APdH<sub>3</sub> (A=Sr, Eu, Yb). Journal of Alloys Compounds, 253-254, 330-332.
- [3] Al S., Kurkcu C., Yamcicier C. 2020. Structural evolution, mechanical, electronic and vibrational properties of high capacity hydrogen storage TiH<sub>4</sub>. International Journal of Hydrogen Energy, 45(55), 30783-91.
- [4] Giannozzi P., Baroni S., Bonini N., Calandra M., Car R., Cavazzoni C., et al. 2009. QUANTUM ESPRESSO: a modular and open-source software project for quantum simulations of materials. Journal of physics: Condensed matter, 21(39), 395502.
- [5] Giannozzi P., Andreussi O., Brumme T., Bunau O., Nardelli M. B., Calandra M., et al. 2017. Advanced capabilities for materials modelling with Quantum ESPRESSO. Journal of physics: Condensed matter, 29(46), 465901.
- [6] Perdew J. P., Burke K., Ernzerhof M. Generalized gradient approximation made simple. 1996. Journal Physical review letters, 77(18), 3865.
- [7] Methfessel M., Paxton A. 1989. High-precision sampling for Brillouin-zone integration in metals. Journal of Physical Review B, 40(6), 3616.
- [8] Yıldız G. D., Yıldız Y. G., AL S., İyigör A., Arıkan N. 2018. Computational investigations of mechanic, electronic and lattice dynamic properties of yttrium based compounds. International Journal of Modern Physics B, 32(20), 1850214.
- [9] Al S., Arıkan N., Demir S., İyigör A. 2018. Lattice dynamic properties of Rh<sub>2</sub> XAl (X= Fe and Y) alloys. Physica B: Condensed Matter, 531, 16-20.
- [10] Al S., İyigör A. 2020. Structural, electronic, elastic and thermodynamic properties of hydrogen storage magnesium-based ternary hydrides. Chemical Physics Letters, 743, 137184.
- [11] Chen S., Sun Y., Duan Y-H., Huang B., Peng M-J. 2015. Phase stability, structural and elastic properties of C15-type Laves transition-metal compounds MCo<sub>2</sub> from first-principles calculations. Journal of Alloys and Compounds, 630, 202-208.
- [12] D. G. 1992. Theoretical predictions of structure and related properties of intermetallics. Materials Science and Technology, 8(4), 345-349.
- [13] Kurkcu C., Al S., Yamcicier C. 2020. Ab-initio study of structural, electronic, elastic, phonon properties, and phase transition path of sodium selenite. Chemical Physics, 539, 110934.
- [14] Al S. 2021. Elastic and thermodynamic properties of cubic perovskite type NdXO<sub>3</sub> (X=Ga, In). The European Physical Journal B, 94(5), 108.
- [15] Arar R., Ouahrani T., Varshney D., Khenata R., Murtaza G., Rached D., et al. 2015. Structural, mechanical and electronic properties of sodium based fluoroperovskites NaXF<sub>3</sub> (X=Mg, Zn) from first-principle calculations. Materials Science Semiconducting Process, 33, 127-135.
- [16] Bronger W., Ridder G. 1994. Synthese und Struktur von SrPdH<sub>2.7</sub>. Journal of Alloys Compounds, 210(1-2), 53-55.
- [17] Ali M. A., Hossain M. M., Islam A. Naqib S. H. 2021. Ternary boride Hf<sub>3</sub>PB<sub>4</sub>: Insights into the physical properties of the hardest possible boride MAX phase. Journal of Alloys Compounds, 857, 158264.
- [18] Chen H., Yang L., Long J. 2015. First-principles investigation of the elastic, Vickers hardness and thermodynamic properties of Al-Cu intermetallic compounds. Superlattices Microstructure, 79, 156-165.
- [19] Hossain M. M., Ali M. A., Uddin M. M., Islam A., Naqib S.H. 2021. Origin of high hardness and optoelectronic and thermo-physical properties of boron-rich compounds B<sub>6</sub>X (X=S, Se): A comprehensive study via DFT approach. Journal of Applied Physics, 129(17), 175109.
- [20] Mubarak A. A., Al-Omari S. 2015. First-principles calculations of two cubic fluoroperovskite compounds: RbFeF<sub>3</sub> and RbNiF<sub>3</sub>. Journal of Magnetism and Magnetic Materials, 382, 211-218.

- [21] Awais M., Zeba I., Gillani S. S. A., Shakil M., Rizwan M. 2022. First-principles calculations to investigate band gap of cubic BaThO<sub>3</sub> with systematic isotropic external static pressure and its impact on structural, elastic, mechanical, anisotropic, electronic and optical properties. *Journal of Physical Chemistry Solids*, 169, 110878.
- [22] Al S. 2021. Mechanical and electronic properties of perovskite hydrides LiCaH<sub>3</sub> and NaCaH<sub>3</sub> for hydrogen storage applications. *The European Physical Journal B*, 94(9), 182.
- [23] Musari A. A. 2021. Electronic, mechanical, vibrational and thermodynamic properties of FeXSb (X = Hf and Nb) Half-Heusler alloys from first-principles approach. *Solid State Sciences*, 122, 106755.