



COMPARISON OF INTERPOLATION METHODS IN THE SPATIAL DISTRIBUTION OF MONTHLY PRECIPITATION DATA IN KONYA CLOSED BASIN

¹ Cansu Hacer KAPLAN , ^{2*} Meral BÜYÜKYILDIZ , ³ Cihangir KÖYCEĞİZ 

¹Konya Technical University, Institute of Graduate Studies, Civil Engineering Department, Konya, TÜRKİYE
^{2,3}Konya Technical University, Engineering and Natural Sciences Faculty, Civil Engineering Department, Konya, TÜRKİYE

¹ cansuhacerkaplan@gmail.com, ² mbuyukyildiz@ktun.edu.tr, ³ ckoycegiz@ktun.edu.tr

Highlights

- The performance of deterministic and geostatistical interpolation methods in the spatial distribution of monthly total precipitation in the Konya Closed Basin (KCB) was investigated.
- The effect of both the number of stations and the observation period on the prediction performance was evaluated.
- Inverse Distance Weighted Interpolation Method (IDW), Regularized Spline (Sp-R) and Tension Spline (Sp-T) were used as deterministic methods, while Ordinary Kriging (OK) and Universal Kriging (UK) were used as geostatistical methods.



COMPARISON OF INTERPOLATION METHODS IN THE SPATIAL DISTRIBUTION OF MONTHLY PRECIPITATION DATA IN KONYA CLOSED BASIN

¹ Cansu Hacer KAPLAN^{ID}, ^{2,*} Meral BÜYÜKYILDIZ^{ID}, ³ Cihangir KÖYCEĞİZ^{ID}

¹ Konya Technical University, Institute of Graduate Studies, Civil Engineering Department, Konya, TÜRKİYE
^{2,3} Konya Technical University, Engineering and Natural Sciences Faculty, Civil Engineering Department, Konya, TÜRKİYE

¹ cansuhacerkaplan@gmail.com, ² mbuyukyildiz@ktun.edu.tr, ³ ckoycegiz@ktun.edu.tr

(Received: 21.08.2024; Accepted in Revised Form: 14.10.2024)

ABSTRACT: Interpolation methods are used as an effective tool in determining the spatial distribution of precipitation. In this study, the performance of deterministic and geostatistical interpolation methods in estimating the spatial distribution of monthly total precipitation in the Konya Closed Basin (KCB) was investigated. In the study, the effect of both the number of stations and the observation period on the prediction performance was evaluated. While 11 stations were used in the long period (1971-2019), 34 stations were used in the short period (2014-2019). Spatial forecasts were performed by deterministic methods such as Inverse Distance Weighted Interpolation (IDW), Regularized Spline (Sp-R), and Tension Spline (Sp-T) and geostatistical methods such as Ordinary Kriging (OK) and Universal Kriging (UK). spherical (S), gaussian (G), circular (C), and exponential (E) were used as semivariogram methods in the OK method. According to Nash Sutcliffe efficiency coefficient (NSE), the most successful interpolation methods for the long period (1971-2019) were Sp-T (NSE=0.721) at Cihanbeyli station, Sp-R (NSE=0.561) at Seydişehir station, and OK-G (NSE=0.704) at Karapınar station. In the short period (2014-2019), the highest prediction success among the 10 test stations was obtained from Seydişehir station (IDW_{NSE}=0.843), and the lowest prediction success was obtained from Sultanhanı station (OK-G_{NSE}=0.533).

Keywords: Deterministic, Geostatistics, IDW, Interpolation, Kriging, Precipitation, Spline

1. INTRODUCTION

Climate parameters are used in many different fields such as hydrology, meteorology, geology, agriculture, forest management, and ecology. Precipitation is among the climate parameters that play a key role in modeling hydrological processes [1]. Analysis of spatial and temporal variability in precipitation data is quite important for the management of water resources systems, the management of floods and droughts, landslide management, and management of agricultural activities [2-3]. Precipitation, which is the main input data for modeling hydrological processes, is measured pointwise at meteorological stations or determined by satellites and weather radars, as with most climatological parameters, [4]. Satellite and radar data, which are often used in hydrological studies, need to be verified and corrected before use [2]. Therefore, the most reliable measurement method is a rain gauge. Since precipitation is the climate element with the most variation over time and location, denser network of measuring stations is needed to measure precipitation data compared to other climate elements [5]. Due to economic and geographical difficulties around the world, the land measurement network is insufficient to represent the spatial variability of precipitation. Therefore, spatial interpolation techniques based on point measurements are used as alternative tools for precipitation estimation [6]. Interpolation methods are generally categorized into two groups: deterministic and stochastic (geostatistical) methods. Geostatistical interpolation methods quantify point or spatial correlation based on the distance between sampling points, and take into account the spatial configuration of sampling points around the estimation points [7-8]. Deterministic interpolation methods create surfaces from sample points using mathematical functions [9-10]. The interpolation methods used have different advantages and disadvantages. For this reason, there is no valid and appropriate interpolation method that can be used in all conditions [11]. This

*Corresponding Author: Meral BÜYÜKYILDIZ, mbuyukyildiz@ktun.edu.tr

is mainly because the performance of interpolation techniques is controlled by many factors, such as data density, spatial distribution of data, data clustering, surface type, data variance, grid size or resolution, the quality of the supporting information to be used, and the interactions between these factors [12]. Therefore, it is important to make a comparative assessment of different interpolation methods for a specific study area.

The literature contains numerous studies that use interpolation methods to estimate precipitation parameter [2], [9], [13-24]. Katipoğlu [9] obtained maps showing the spatial distribution of seasonal precipitation in the Euphrates Basin by using several interpolation techniques. The most effective interpolation techniques were found to be ordinary Kriging for autumn precipitation, ordinary CoKriging for winter and spring precipitation, and local polynomial interpolation for summer precipitation in the study that used precipitation data from 21 stations for the period 1966-2017. Antal et al. [14] estimated the average annual precipitation using seven interpolation methods. For this purpose, data of 128 stations in Portugal for the period 1991-2000 were used, and it was determined that the empirical Bayesian kriging regression (EBKR) interpolation method showed the most successful spatial distribution. Liu et al. [20] found that hybrid methods such as Trend Surfaces and Regression-Ordinary Kriging (TSA-OK) and Bayesian Model Averaging (BMA) between sparse and relatively dense gauge stations for different time scales (daily, monthly, and yearly) performed best at all time scales for spatial precipitation estimation in the Changjiang River Basin. In another study, Fung et al. [22] investigated the temporal-spatial variation of rainfall patterns (number of wet days, monthly rainfall, and maximum daily rainfall) in Peninsular Malaysia using four interpolation methods. The performance of multivariate interpolation (geographical weighted regression—GWR, multiscale geographical weighted regression—MGWR) and univariate interpolation (Ordinary Kriging and IDW) methods were compared. The results show that MGWR has better prediction performance in general among the interpolation methods.

Interpolation techniques are also utilized in the spatial distribution of other meteorological data such as temperature [25], evapotranspiration [26-27], groundwater level [28-29], and drought [30-31].

In this study, the applicability of stochastic and deterministic interpolation methods in the spatial precipitation distribution of the Konya Closed Basin (KCB) was investigated. For this purpose, deterministic methods such as Inverse Distance Weighting (IDW), Regularized Spline (Sp-R), and Tension Spline (Sp-T), as well as geostatistical methods Ordinary Kriging (OK) and Universal Kriging (UK), were applied. For the OK method, spherical (S), gaussian (G), circular (C), and exponential (E) semivariogram models, which are the most used in the literature, were applied. In the UK method, predictions were made with the Stable semivariogram model. KCB has quite an important place in terms of agricultural production in our country. Most of the water potential in the basin is used in agriculture. It is of great importance to analyze the spatial variation of precipitation in KCB, which is the driest and water-limited basin of Turkey.

2. STUDY AREA and DATA

The Konya Closed Basin (KCB), which was used as the study area, is located between 36°51' - 39°29' north latitude and 31°36' - 34°52' east longitude. The basin covers an area of 49805.34 km², corresponding to 7% of Türkiye's surface area. The KCB is bordered by the Sakarya and Kızılırmak Basins to the north, the Kızılırmak and Seyhan Basins to the east, the Eastern Mediterranean Basin to the south, and the Akarçay and Antalya Basins to the west. KCB is among the basins with the lowest rainfall in Türkiye. The average annual precipitation is around 300-350 mm. While the least precipitation falls in the central parts of the basin, the most precipitation falls in the western part. Due to the irregularity of precipitation in the basin, river regimes are also irregular. KCB is among the most important regions of Türkiye in terms of agricultural production.

Two different periods were taken into consideration in the spatial distribution of precipitation data: long period (1971-2019) and short period (2014-2019). The data from 11 meteorological observation stations were used for the long period, and 34 meteorological observation stations were used for the short period. Information about the meteorological observation stations used in the study is given in Table 1.

Table 1. Meteorological observation stations used in the study

| Station Code | Station Name | Station Number | Latitude | Longitude |
|--------------|----------------------------------|----------------|---------------|---------------|
| S1 | Aksaray ^{xx} | 17192 | 38°22'13.80"N | 33°59'55.32"E |
| S2 | Niğde ^{xx} | 17250 | 37°57'30.60"N | 34°40'46.20"E |
| S3 | Çumra ^{xx} | 17900 | 37°33'56.88"N | 32°47'24.00"E |
| S4 | Beyşehir ^{xx} | 17242 | 37°40'39.72"N | 31°44'46.68"E |
| S5 | Kulu ^{xx} | 17754 | 39° 4'43.68"N | 33° 3'56.52"E |
| S6 | Konya Havalimanı ^{xx} | 17244 | 37°59'1.32"N | 32°34'26.40"E |
| S7 | Ereğli ^{xx} | 17248 | 37°31'31.80"N | 34° 2'54.60"E |
| S8 | Karaman ^{xx} | 17246 | 37°11'35.5"N | 33°13'12.7"E |
| S9 | Seydişehir/Alacabel ^x | 18212 | 37°14'03.1"N | 31°55'00.8"E |
| S10 | Akören ^x | 18487 | 37°27'06.1"N | 32°22'49.1"E |
| S11 | Ahırlı ^x | 18486 | 37°14'25.1"N | 32°06'52.9"E |
| S12 | Güneysinır ^x | 18495 | 37°16'04.8"N | 32°43'14.9"E |
| S13 | Altnekin ^x | 18488 | 38°17'56.0"N | 32°52'45.1"E |
| S14 | Hüyük ^x | 18497 | 37°57'55.1"N | 31°35'47.0"E |
| S15 | Yalıhüyük ^x | 18500 | 37°17'31.9"N | 32°06'43.9"E |
| S16 | Derebucak ^x | 18492 | 37°23'30.8"N | 31°30'51.8"E |
| S17 | Emirgazi ^x | 18494 | 37°53'33.0"N | 33°50'28.0"E |
| S18 | Bozkır/Sorkun ^x | 18591 | 37°09'06.1"N | 32°05'35.2"E |
| S19 | Derbent ^x | 18491 | 38°00'59.0"N | 32°01'01.9"E |
| S20 | Güzelyurt ^x | 18116 | 38°16'14.9"N | 34°22'19.9"E |
| S21 | Eskil ^x | 18481 | 38°18'31.0"N | 33°21'33.1"E |
| S22 | Altunhisar ^x | 18501 | 38°00'05.4"N | 34°21'31.7"E |
| S23 | Çiftlik ^x | 18503 | 38°08'35.2"N | 34°27'42.8"E |
| S24 | Ayrancı ^x | 18211 | 37°20'13.9"N | 33°43'16.0"E |
| S25 | Seydişehir ^{yy} | 17898 | 37°25'36.12"N | 31°50'56.40"E |
| S26 | Cihanbeyli ^{yy} | 17191 | 38°39'2.08"N | 32°55'18.70"E |
| S27 | Karapınar ^{yy} | 17902 | 37°42'58.72"N | 33°31'33.60"E |
| S28 | Karatay TAGEM ^y | 18213 | 37°51'38.2"N | 32°35'02.0"E |
| S29 | Bozkır ^y | 18489 | 37°10'59.9"N | 32°14'46.0"E |
| S30 | Halkapınar/İvriz ^y | 18496 | 37°26'29.0"N | 34°09'06.8"E |
| S31 | Sultanhanı ^y | 18117 | 38°11'58.9"N | 33°31'00.8"E |
| S32 | Gülağaç ^y | 18482 | 38°24'32.0"N | 34°20'37.0"E |
| S33 | Bor ^y | 18502 | 37°55'17.0"N | 34°33'10.1"E |
| S34 | Kazımkarabekir ^y | 18484 | 37°13'07.0"N | 32°57'23.0"E |

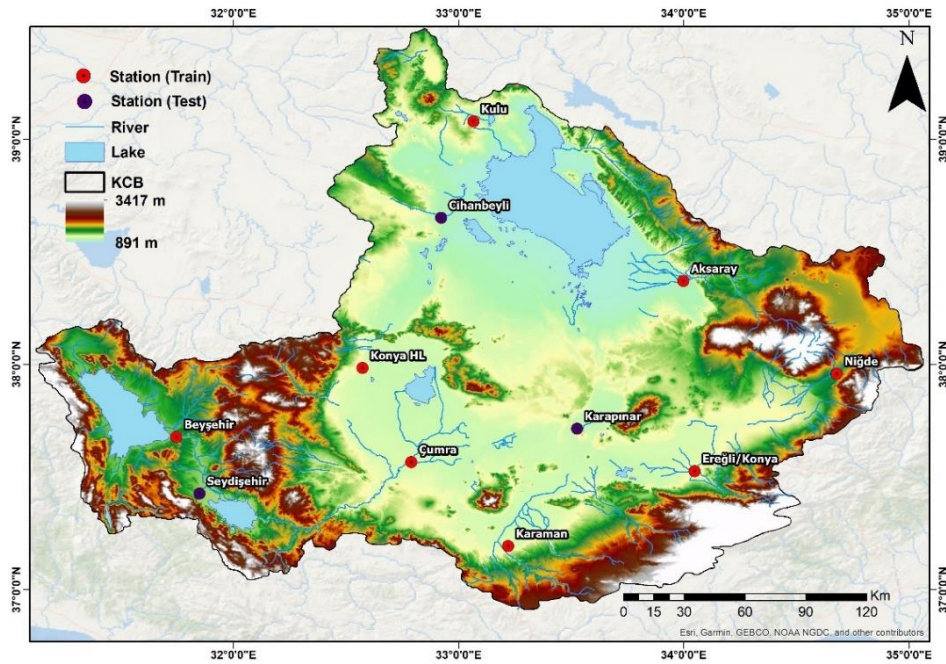
^{xx} : Meteorological stations used in spatial distribution in the long period (1971-2019)

^{yy} : Test stations used in the long period (1971-2019)

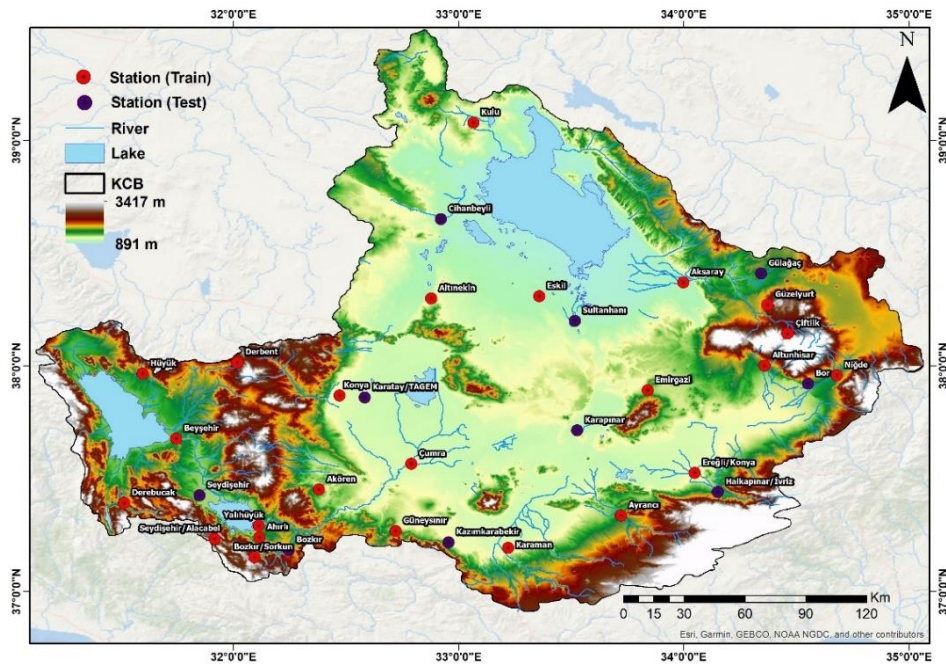
^{x ve xx} : Meteorological stations used in the spatial distribution in the short period (2014-2019)

^{y ve yy} : Test stations used in the short period (2014-2019)

The interpolation methods applied to the monthly total precipitation data were tested with 3 stations in the long period and 10 stations in the short period, and the methods were compared. The locations of the meteorological observation stations utilized for the long and short periods are presented in Figure 1a and Figure 1b, respectively.



(a)



(b)

Figure 1. Location of the meteorological observation stations used in the spatial distribution and for testing purposes in KCB **a)** Long period (1971-2019), **b)** Short period (2014-2019)

In the long period (1971-2019), Seydişehir, Cihanbeyli, and Karapınar stations were utilized for testing, whereas Aksaray, Niğde, Çumra, Beyşehir, Kulu, Konya, Ereğli, and Karaman stations were used for spatial distribution (Figure 1a). In the short period (2014-2019), 10 stations (Seydişehir, Cihanbeyli, Karapınar, Karatay-Tagem, Bozkır, Halkapınar/İvriz, Sultanhanı, Gülağaç, Bor and Kazımkarabekir) were used for testing, while the remaining 24 stations, which are shown in Table 1, were used for spatial distribution (Figure 1b).

For geostatistical analyses to yield useful findings, details about the statistical distribution, outliers, and kurtosis of the analyzed data set are crucial [32]. Statistical characteristics of annual total precipitation data from the stations for the long period (2014-2019) and short period (2014-2019) are given in Table 2 and Table 3, respectively.

Table 2. Annual total precipitation statistics for the period 1971-2019

| Station Name | Station Number | Avg. (mm) | Max (mm) | Min (mm) | Std Dev (mm) | Skewness | Kurtosis |
|--------------|----------------|-----------|----------|----------|--------------|----------|----------|
| Aksaray | 17192 | 346.77 | 506.20 | 228.80 | 70.51 | 0.30 | -0.53 |
| Beyşehir | 17242 | 490.45 | 656.90 | 317.10 | 90.12 | -0.45 | -0.72 |
| Çumra | 17900 | 322.19 | 502.10 | 176.50 | 70.31 | 0.16 | -0.43 |
| Ereğli | 17248 | 304.64 | 438.50 | 140.00 | 57.69 | -0.17 | 0.51 |
| Kulu | 17754 | 376.29 | 547.80 | 218.70 | 71.65 | -0.04 | -0.01 |
| Niğde | 17250 | 336.87 | 484.00 | 192.90 | 70.22 | 0.02 | -0.24 |
| Karaman | 17246 | 333.97 | 513.40 | 212.60 | 70.66 | 0.41 | -0.15 |
| Konya | 17244 | 326.53 | 523.90 | 176.10 | 73.80 | 0.14 | 0.18 |
| Seydişehir | 17898 | 752.65 | 1202.00 | 474.90 | 154.61 | 0.46 | 0.46 |
| Cihanbeyli | 17191 | 323.57 | 499.80 | 184.60 | 70.86 | 0.11 | -0.40 |
| Karapınar | 17902 | 291.05 | 412.90 | 171.60 | 57.72 | 0.22 | -0.43 |

Table 3. Annual total precipitation statistics for the period 2014-2019

| Station Name | Station Number | Avg. (mm) | Max (mm) | Min (mm) | Std Dev (mm) | Skewness | Kurtosis |
|---------------------|----------------|-----------|----------|----------|--------------|----------|----------|
| Aksaray | 17192 | 358.72 | 434.60 | 298.90 | 46.89 | 0.27 | -0.76 |
| Beyşehir | 17242 | 526.68 | 593.40 | 463.50 | 47.01 | 0.08 | -2.08 |
| Çumra | 17900 | 355.40 | 443.60 | 245.20 | 68.51 | -0.54 | -0.99 |
| Ereğli | 17248 | 318.03 | 353.90 | 274.80 | 32.09 | -0.47 | -2.20 |
| Kulu | 17754 | 386.07 | 459.20 | 328.80 | 48.38 | 0.20 | -1.84 |
| Niğde | 17250 | 350.72 | 463.80 | 246.50 | 71.08 | 0.18 | -0.52 |
| Karaman | 17246 | 393.68 | 477.60 | 287.10 | 64.63 | -0.33 | -0.64 |
| Konya | 17244 | 371.52 | 523.90 | 283.70 | 75.96 | 1.38 | 2.68 |
| Seydişehir Alacabel | 18212 | 1152.35 | 1475.00 | 884.10 | 194.31 | 0.29 | -0.33 |
| Akören | 18487 | 465.48 | 566.60 | 376.00 | 62.54 | 0.09 | -0.34 |
| Ahırlı | 18486 | 543.42 | 641.00 | 428.30 | 90.01 | -0.30 | -2.55 |
| Güneysınır | 18495 | 503.75 | 553.40 | 408.70 | 60.71 | -0.98 | -1.65 |
| Hüyük | 18497 | 490.73 | 571.00 | 329.90 | 75.77 | -1.88 | 4.27 |
| Yalıhüyük | 18500 | 538.85 | 645.00 | 425.40 | 67.95 | -0.17 | 0.51 |
| Derebucak | 18492 | 854.67 | 1073.30 | 593.80 | 142.38 | -0.57 | 1.94 |
| Emirgazi | 18494 | 325.47 | 379.40 | 211.00 | 55.92 | -1.66 | 2.84 |
| Bozkır/Sorkun | 18591 | 699.52 | 928.70 | 331.90 | 211.91 | -1.08 | 0.60 |
| Derbent | 18491 | 553.82 | 633.30 | 474.20 | 64.39 | 0.00 | -2.93 |
| Altınekin | 18488 | 373.17 | 442.30 | 262.00 | 59.77 | -0.96 | 0.75 |
| Güzelyurt | 18116 | 435.97 | 487.40 | 351.20 | 48.47 | -0.88 | -0.45 |
| Eskil | 18481 | 287.93 | 347.70 | 250.90 | 38.57 | 0.88 | -1.67 |
| Altunhisar | 18501 | 328.40 | 390.90 | 299.70 | 31.40 | 1.51 | 1.97 |
| Çiftlik | 18503 | 557.25 | 670.80 | 440.40 | 69.75 | -0.11 | 1.05 |
| Ayrancı | 18211 | 308.68 | 374.80 | 253.00 | 41.54 | 0.37 | -0.93 |
| Seydişehir | 17898 | 772.23 | 935.80 | 696.40 | 85.60 | 1.35 | 0.88 |
| Cihanbeyli | 17191 | 347.83 | 446.50 | 270.20 | 76.25 | 0.25 | -2.72 |
| Karapınar | 17902 | 327.90 | 391.80 | 260.20 | 41.75 | -0.02 | 0.09 |
| Bozkır | 18489 | 553.10 | 630.00 | 443.60 | 68.77 | -0.57 | -1.42 |
| Kazımkarabekir | 18484 | 446.13 | 533.40 | 326.90 | 64.66 | -0.87 | 1.09 |
| Halkapınar/İvriz | 18496 | 362.52 | 476.40 | 293.00 | 67.08 | 0.82 | -0.82 |
| Karatay(TAGEM) | 18213 | 280.62 | 409.50 | 177.10 | 68.19 | 0.73 | 2.54 |
| Sultanhanı | 18117 | 298.72 | 340.90 | 255.40 | 32.47 | -0.16 | -1.81 |
| Bor | 18502 | 374.17 | 460.40 | 272.40 | 67.04 | 0.13 | -1.00 |
| Gülağaç | 18482 | 337.03 | 367.20 | 303.50 | 21.95 | -0.44 | -1.11 |

3. METHODOLOGY

3.1. Interpolation Methods

By utilizing measured point data, estimates can be made for unmeasured regions. To achieve spatial estimations, a variety of interpolation methods are employed. To perform spatial estimations and mapping of precipitation data in this study, interpolation methods were implemented in ArcGIS 10.7.1 software utilizing the Spatial Analyst Tools and Geostatistical Analyst module. As interpolations, IDW, Sp-R, and Sp-T from deterministic methods and OK and UK from geostatistical methods were applied. For OK methods, applications were performed with the most frequently used semivariogram models in the literature. These are spherical (S), gaussian (G), circular (C), and exponential (E) semivariogram models. In the UK interpolation method, the stable semivariogram model was used. The workflow diagram of the deterministic and geostatistical analysis applications in this study is given in Figure 2.

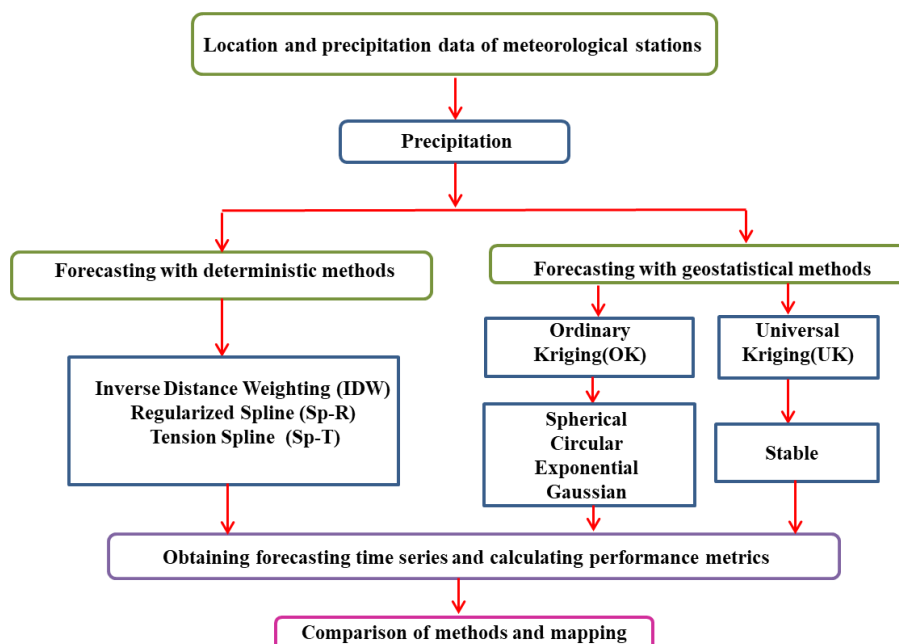


Figure 2. Workflow diagram of deterministic and geostatistical analysis applications

3.1.1. Inverse Distance Weighting (IDW)

IDW is one of the widely used deterministic interpolation methods. IDW is a local interpolation method since it produces estimates only from neighboring points [22], [25]. IDW is based on the principle that nearby points on the surface to be interpolated have more weight than distant points. As the distance from the point to be interpolated increases, the importance and influence on the cell to be estimated decreases [18], [22], [25], [33]. This technique uses the mathematical functions in Equations 1, 2, and 3 [34].

$$F(x, y) = \sum_{i=1}^n w_i f_i \quad (1)$$

$$w_i = \frac{h_i^{-p}}{\sum_{j=1}^n h_j^{-p}} \quad (2)$$

$$\sum_{i=1}^n w_i = 1 \quad (3)$$

In the above equations, p is the force parameter, h_i is the spatial distance between sample points and the interpolated points, and w_i is the weights [33]. In the weight function, the power parameter is expressed

as the exponent of the distance inversely proportional to the distance. If the power parameter p is 0, no weighting can be done in relation to the distance. p can be given ≥ 1 values [32].

3.1.2. Spline (Sp)

Spline is a deterministic interpolation method that interpolates by passing the minimum curvature surface through points of known value (input values). Spline interpolation is not suitable for data with large variations over short horizontal distances [35].

Two types of Spline versions are used in this study: Regularized Spline (Sp-R) and Tension Spline (Sp-T). Compared to the Sp-R method, the Sp-T method produces a more closed and uniform data set that is bounded by the sample data range [28], [36-37]. A general mathematical function is used for the Spline method (Equation 4). Equations 5-6 are the mathematical functions for the Sp-T method, and Equations 7-8 are the mathematical functions for the Sp-R method [28].

$$S(x, y) = T(x, y) + \sum_{j=1}^N \lambda_j R(r_j) \quad (4)$$

$$T(x, y) = a_1 \quad (5)$$

$$R(r) = \frac{1}{2\pi\varphi^2} \left[\ln\left(\frac{r\varphi}{2}\right) + c + K(r\varphi) \right] \quad (6)$$

$$T(x, y) = a_1 + a_2x + a_3y \quad (7)$$

$$R(r) = \frac{1}{2\pi} \left\{ \frac{r^2}{4} \left[\ln\left(\frac{r}{2\pi}\right) + c - 1 \right] + \tau^2 \left[K\left(\frac{r}{\tau}\right) + c + \ln\left(\frac{r}{2\pi}\right) \right] \right\} \quad (8)$$

In the above equations; N: Number of points, λ_j : Coefficients found by solving the system of linear equations, r_j : Distance between point (x, y) and point j. a_1 : Coefficients found by solving the system of linear equations, φ^2 and τ^2 : Weight parameters, $C = 0.0577215$, r: Distance between point and sample, K: modified Bessel function.

3.1.3. Kriging Interpolation

Kriging is a geostatistical estimation method developed for spatial estimation [38]. This method is defined as the best linear unbiased estimator or calculator known as collocation in mathematical geodesy [39]. The Kriging method does not only depend on the distance between the measurement points and the estimation points as in the IDW method. It also depends on the overall spatial regularization between the measurement points. In the Kriging method, weights are determined by the semivariogram model developed according to the spatial location of the data. Kriging is an interpolation method that has proven its popularity in geostatistics and many other fields [35].

The variogram, which measures the spatial correlation between two points, is the most crucial in this interpolation technique. The major advantage of the Kriging method is that, in addition to the estimated surface, it also provides a measure of the error or uncertainty of the estimated surface [32], [40]. Its disadvantage is that it requires more computational time and input compared to IDW and Spline methods [28].

To know the properties of the regional parameters and to estimate the values at points where the measured values are not known, it is necessary to know the semivariogram values of each point. This is achieved by fitting a mathematical function to the experimental semivariogram values. This model is called the theoretical semivariogram model or semivariogram model [41]. The mathematical functions of the semivariogram model are shown in Table 4.

Table 4. Semivariogram models

| Semivariogram Model | Mathematical Function |
|---------------------|----------------------------------------------------------------------------------------------------------------------------------------------|
| Spherical | $\gamma(h) = C_0 + C \left(\frac{3h}{2a} - \frac{h^3}{2a^3} \right), \quad 0 \leq h \leq a$ |
| Gaussian | $\gamma(h) = C_0 + C \left(1 - \exp\left(\frac{-h^2}{a^2}\right) \right), \quad h \geq 0$ |
| Circular | $\gamma(h) = C_0 + C \left(1 - \frac{2}{\pi} \cos^{-1}\left(\frac{h}{a}\right) + \sqrt{1 - \frac{h^2}{a^2}} \right), \quad 0 \leq h \leq a$ |
| Exponential | $\gamma(h) = C_0 + C \left(1 - \exp\left(\frac{-h}{a}\right) \right), \quad h \geq 0$ |

In the equations given in Table 4, *a* is the impact distance, *C* is the threshold value, and *C*₀ is the nugget effect.

The Stable model is a model that balances between Gaussian and Exponential semivariogram models. This model produces results by approximating Gaussian and Exponential semivariogram models [32], [42]. The general formulation of the kriging technique is known as the OK method [43]. OK is the most widely used type of kriging [44]. The analysis of the Kriging system by taking into account the presence of trends in the data is called the UK method [38]. In this study, OK (with 4 different semivariogram versions) and the UK method are Kriging methods used as geostatistical methods. More information about the Kriging method is available in Webster and Oliver [44].

3.2. Performance Metrics

The performance of the interpolation methods was evaluated using the metrics given in Table 5.

Table 5. Performance metrics

| | |
|---------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Determination Coefficient (R ²) | $R^2 = \frac{\left[\sum_{i=1}^n (Z_{g_i} - \bar{Z}_g)(Z_{m_i} - \bar{Z}_m) \right]^2}{\sum_{i=1}^n (Z_{g_i} - \bar{Z}_g)^2 \sum_{i=1}^n (Z_{m_i} - \bar{Z}_m)^2}$ |
| Nash-Sutcliffe Efficiency Coefficient (NSE) | $NSE = 1 - \frac{\left[\sum_{i=1}^n (Z_{g_i} - Z_{m_i})^2 \right]}{\left[\sum_{i=1}^n (Z_{g_i} - \bar{Z}_g)^2 \right]}$ |
| Mean Absolute Error (MAE) | $MAE = \frac{1}{n} \sum_{i=1}^n Z_m - Z_g $ |
| Root Mean Squared Error (RMSE) | $RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (Z_m - Z_g)^2}$ |

In the equations given in Table 5, *Z_g* is the measurement data, *Z_m* is the data generated by the model, and *n* is the data number. In addition, \bar{Z}_g and \bar{Z}_m are the average of measurement data and model data, respectively. According to the NSE metric, model performance levels are evaluated as “very good” for 0.75 < NSE ≤ 1, “good” for 0.65 < NSE ≤ 0.75, “satisfactory” for 0.50 < NSE ≤ 0.65, and “unsatisfactory” for NSE ≤ 0.5 [45].

4. RESULTS and DISCUSSION

In this study, the usability of different interpolation techniques in the spatial distributions of monthly total precipitation data in KCB were investigated. Two different time periods, long (1971-2019) and short (2014-2019), were considered in the spatial distribution of precipitation. Precipitation data from 11 and 34 stations were used in the long and short periods, respectively. Thus, it was aimed to evaluate the effect of the number of stations, i.e., density, on the estimation success of interpolation methods by using fewer stations in the long period and more stations in the short period.

4.1. Spatial Interpolation Results of Monthly Total Precipitation for Long Period (1971-2019)

The results obtained by applying the interpolation methods for the KCB's monthly total precipitation data between 1971 and 2019 are given in Table 6. The maximum NSE value was considered in determining the most successful interpolation method and is shown in bold in Table 6.

Table 6. The long period (1971-2019) performance values of interpolation methods

| Station Name | Model Name | R ² | NSE | Performance | MAE (mm) | RMSE (mm) |
|---------------------|-------------|----------------|--------------|---------------------|--------------|--------------|
| 17898 Seydişehir | IDW | 0.781 | 0.503 | Satisfactory | 28.87 | 45.28 |
| | Sp-R | 0.762 | 0.561 | Satisfactory | 27.78 | 42.55 |
| | Sp-T | 0.783 | 0.556 | Satisfactory | 27.73 | 42.84 |
| | UK | 0.604 | 0.137 | Unsatisfactory | 36.77 | 59.66 |
| | OK-C | 0.761 | 0.409 | Unsatisfactory | 31.36 | 49.41 |
| | OK-E | 0.715 | 0.404 | Unsatisfactory | 31.63 | 49.61 |
| | OK-G | 0.734 | 0.370 | Unsatisfactory | 32.31 | 50.99 |
| | OK-S | 0.755 | 0.413 | Unsatisfactory | 31.34 | 49.25 |
| 17191 Cihanbeyli | IDW | 0.747 | 0.719 | Good | 9.23 | 12.45 |
| | Sp-R | 0.686 | 0.659 | Good | 10.09 | 13.73 |
| | Sp-T | 0.741 | 0.721 | Good | 9.11 | 12.42 |
| | UK | 0.654 | 0.644 | Satisfactory | 9.76 | 13.99 |
| | OK-C | 0.654 | 0.605 | Satisfactory | 9.80 | 14.74 |
| | OK-E | 0.494 | 0.294 | Unsatisfactory | 10.91 | 19.72 |
| | OK-G | 0.724 | 0.710 | Good | 9.08 | 12.65 |
| | OK-S | 0.627 | 0.566 | Satisfactory | 9.96 | 15.47 |
| 17902 Karapınar | IDW | 0.730 | 0.686 | Good | 8.89 | 11.94 |
| | Sp-R | 0.648 | 0.612 | Satisfactory | 9.37 | 13.25 |
| | Sp-T | 0.708 | 0.683 | Good | 8.73 | 11.98 |
| | UK | 0.577 | 0.513 | Satisfactory | 10.08 | 14.89 |
| | OK-C | 0.684 | 0.648 | Satisfactory | 8.81 | 12.88 |
| | OK-E | 0.499 | 0.319 | Unsatisfactory | 9.82 | 17.55 |
| | OK-G | 0.725 | 0.704 | Good | 8.24 | 11.55 |
| | OK-S | 0.652 | 0.601 | Satisfactory | 8.88 | 13.45 |

At Seydişehir station, the IDW, Sp-R, and Sp-T models showed “satisfactory” level prediction success with NSE values of 0.503, 0.561, and 0.556, respectively, while the other 5 models showed “unsatisfactory” level prediction success. At this station, the most successful interpolation method in monthly total precipitation prediction was obtained as the Sp-R method (NSE=0.561). Other metric values of the Sp-R model were R²=0.762, MAE=27.78 mm, and RMSE=42.55 mm. At Seydişehir station, the performance metric values of the Sp-R and IDW interpolation methods were also close to the Sp-T model's. The OK models using the four semivariograms performed close to each other, and the OK-S model with an NSE value of 0.413 was the most successful OK model. The interpolation method with the lowest prediction success was the UK method with NSE=0.137. According to the results obtained, it can be said that deterministic interpolation methods are generally more successful at Seydişehir station.

In precipitation estimation at Cihanbeyli station, NSE values for the IDW, Sp-R, Sp-T, and OK-G models were obtained as 0.719, 0.659, 0.721, and 0.710, respectively, and according to these NSE values there is a “good” level of prediction success. The OK-E model shows “unsatisfactory” prediction success

with $NSE=0.294$. The NSE values in other models vary between 0.50 and 0.65, and “satisfactory” prediction success was obtained. The most successful interpolation model at Cihanbeyli station was the Sp-T model with $NSE=0.721$. In this model, $R^2=0.741$, $MAE=9.11$ mm, and $RMSE=12.42$ mm were obtained.

The OK-G model, which had a maximum NSE value of 0.704, was the best-performing interpolation method for the Karapınar station. The OK-G model showed a “good” level of prediction success. Other metric values for this model were $R^2=0.725$, $MAE=8.24$ mm, and $RMSE=11.55$ mm. IDW and Sp-T models also showed “good” prediction performance with $NSE=0.686$ and $NSE=0.683$, respectively. Sp-R, UK, OK-C, and OK-S methods showed “adequate” prediction performance with NSE values of 0.612, 0.513, 0.648 and 0.601, respectively. The lowest prediction success in precipitation prediction at Karapınar station was obtained in the OK-E model with $NSE=0.319$, which is at the “unsatisfactory” level.

The time series and scatter diagrams of the interpolation techniques that had the best prediction success for the long period are presented in Figure 3.

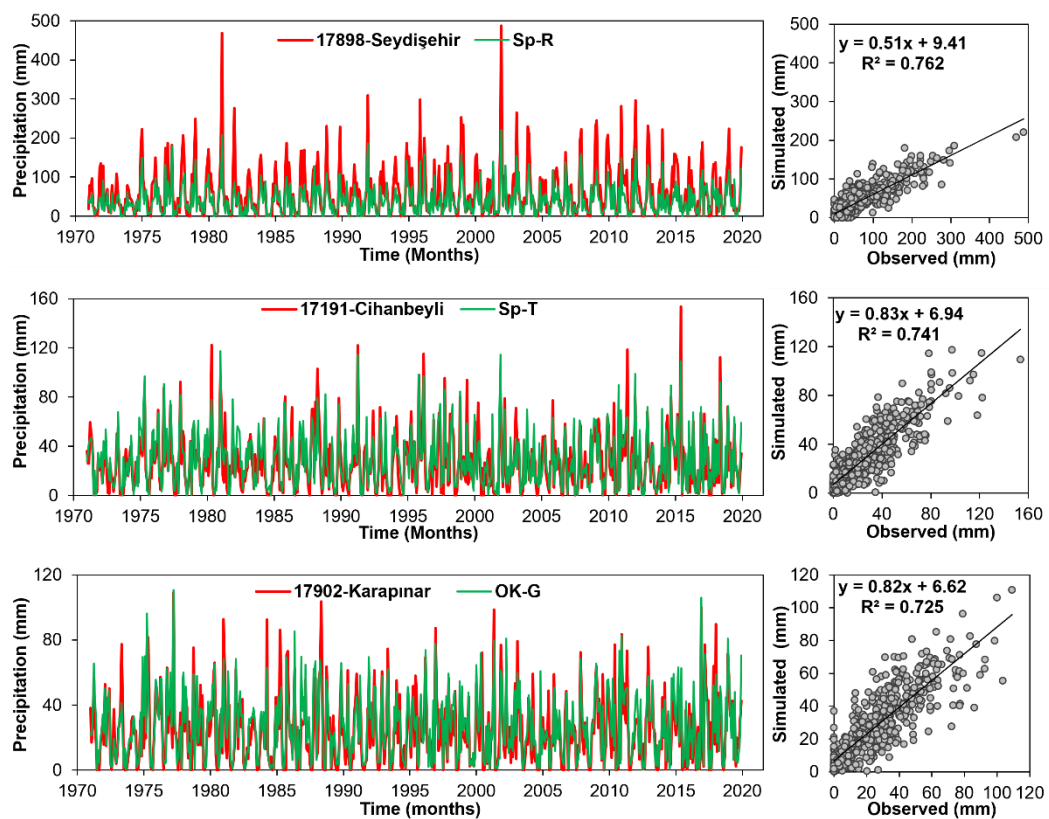


Figure 3. Monthly total precipitation time series and scatter diagrams for the period 1971-2019

As can be seen from the time series given in Figure 3 for the Seydişehir station, the monthly total precipitation data obtained by the Sp-R method generally successfully represent the behavior of the measured precipitation data. However, at this station, the Sp-R method underestimated the precipitation data compared to the observation data. When the time series of the Cihanbeyli station is examined, it is seen that Sp-T forecasts represent the behavior of the measured precipitation more successfully than other stations. The scatter diagram of the Cihanbeyli station also shows that the interpolation method has a higher prediction success at this station. The time series and scatter diagram given for Karapınar station in Figure 3 also show that the success of the OK-G method at this station is similar to Cihanbeyli station.

Monthly total precipitation maps of the interpolation methods applied in KCB for the period 1971-2019 are given in Figure 4. For this period, the locations of the stations used in the spatial distribution of monthly total precipitation are illustrated as red dots on the IDW map in Figure 4, and the locations of the stations used as test stations are shown as black dots.

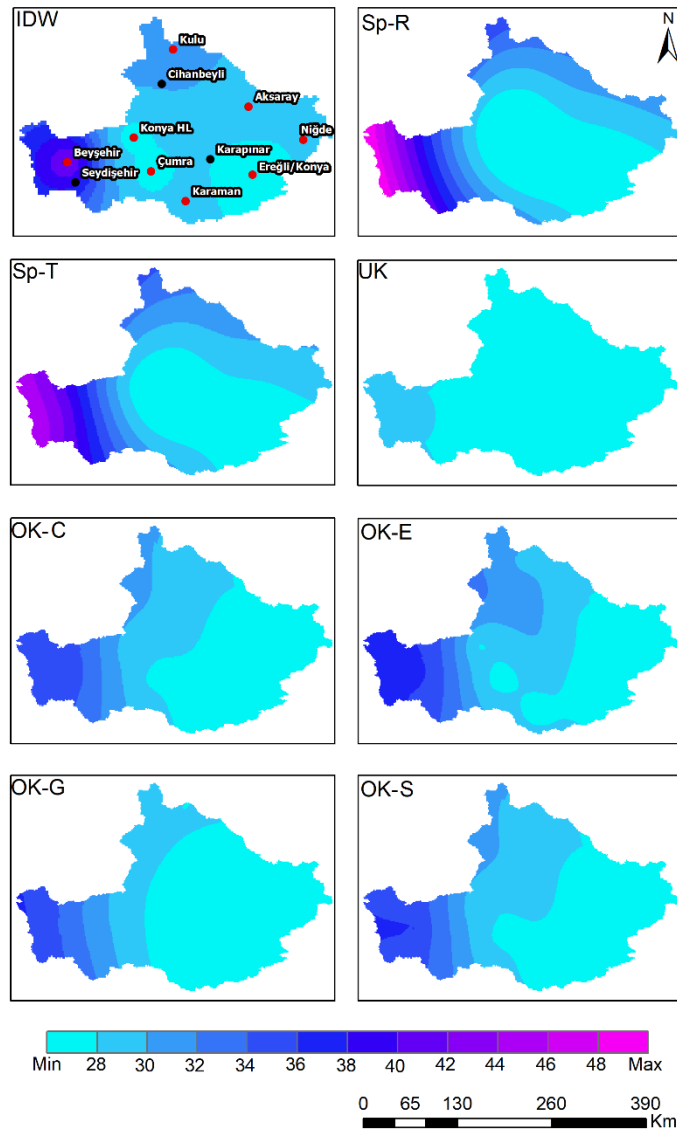


Figure 4. Spatial distribution of monthly total precipitation in KCB for the period 1971-2019

When the precipitation distribution maps are analyzed, it is seen that the monthly total precipitation amount varies between 26 and 41 mm in the IDW method. In the IDW method, it is seen that the maximum precipitation is around Beyşehir and Seydişehir, and the minimum precipitation is around Konya, Çumra, and Ereğli. In the Sp-R method, total monthly precipitation varies between 25 and 51 mm. In the Sp-T method, it varies between 26 and 46 mm. In the Sp-R and Sp-T methods, the maximum precipitation falls around Beyşehir and Seydişehir, while the minimum precipitation falls around Konya, Çumra, Karapınar, and Ereğli. In the UK method, total monthly precipitation is distributed between 25 and 36 mm. While the maximum precipitation falls around Beyşehir and Seydişehir, the rest of the basin is dominated by minimum precipitation. There is not a clear pattern in the UK method. In the OK methods, total monthly precipitation varies between 25 and 37 mm. It is observed that the maximum precipitation in OK methods is around Beyşehir and Seydişehir. Minimum precipitation falls around Çumra, Karapınar, Karaman, Ereğli, Niğde, and Aksaray.

4.2. Spatial Interpolation Results of Monthly Total Precipitation for Short Period (2014-2019)

The performance of the interpolation methods applied to monthly total precipitation data for the short period (multi-station) between 2014 and 2019 is given in Table 7.

Table 7. The short period (2014-2019) performance values of interpolation methods

| Station Name | Model Name | R ² | NSE | Performance | MAE (mm) | RMSE (mm) |
|---------------------------|-------------|----------------|--------------|------------------|--------------|--------------|
| 17898 Seydişehir | IDW | 0.848 | 0.843 | Very Good | 15.29 | 22.52 |
| | Sp-R | 0.610 | 0.397 | Unsatisfactory | 28.66 | 44.15 |
| | Sp-T | 0.681 | 0.557 | Satisfactory | 25.14 | 37.94 |
| | UK | 0.782 | 0.627 | Satisfactory | 23.19 | 34.61 |
| | OK-C | 0.695 | 0.665 | Good | 22.47 | 32.91 |
| | OK-E | 0.553 | 0.536 | Satisfactory | 24.93 | 38.69 |
| | OK-G | 0.764 | 0.701 | Good | 21.10 | 31.02 |
| | OK-S | 0.643 | 0.622 | Satisfactory | 23.20 | 34.92 |
| 17191 Cihanbeyli | IDW | 0.733 | 0.722 | Good | 10.34 | 14.43 |
| | Sp-R | 0.725 | 0.676 | Good | 11.86 | 15.69 |
| | Sp-T | 0.760 | 0.739 | Good | 10.52 | 14.00 |
| | UK | 0.673 | 0.666 | Good | 11.07 | 15.86 |
| | OK-C | 0.001 | -20.252 | Unsatisfactory | 26.01 | 126.31 |
| | OK-E | 0.094 | -1.762 | Unsatisfactory | 16.46 | 45.18 |
| | OK-G | 0.000 | -31.908 | Unsatisfactory | 29.19 | 155.65 |
| | OK-S | 0.002 | -15.837 | Unsatisfactory | 24.16 | 111.33 |
| 17902 Karapınar | IDW | 0.746 | 0.720 | Good | 8.48 | 11.71 |
| | Sp-R | 0.589 | 0.203 | Unsatisfactory | 13.49 | 19.74 |
| | Sp-T | 0.714 | 0.685 | Good | 8.30 | 12.44 |
| | UK | 0.705 | 0.681 | Good | 8.32 | 12.45 |
| | OK-C | 0.698 | 0.672 | Good | 8.38 | 12.76 |
| | OK-E | 0.696 | 0.662 | Good | 8.71 | 13.54 |
| | OK-G | 0.705 | 0.678 | Good | 8.39 | 12.60 |
| | OK-S | 0.683 | 0.647 | Satisfactory | 8.71 | 13.22 |
| 18489 Bozkr | IDW | 0.849 | 0.822 | Very Good | 11.88 | 17.14 |
| | Sp-R | 0.546 | 0.286 | Unsatisfactory | 24.33 | 34.50 |
| | Sp-T | 0.605 | 0.387 | Unsatisfactory | 21.71 | 31.88 |
| | UK | 0.814 | 0.778 | Very Good | 12.18 | 19.13 |
| | OK-C | 0.271 | -0.689 | Unsatisfactory | 18.80 | 52.98 |
| | OK-E | 0.587 | 0.490 | Unsatisfactory | 15.78 | 29.16 |
| | OK-G | 0.811 | 0.795 | Very Good | 11.96 | 18.48 |
| | OK-S | 0.411 | 0.018 | Unsatisfactory | 17.22 | 40.46 |
| 18484 Kazımkarabekir | IDW | 0.837 | 0.836 | Very Good | 8.39 | 13.09 |
| | Sp-R | 0.784 | 0.757 | Very Good | 10.63 | 15.89 |
| | Sp-T | 0.800 | 0.786 | Very Good | 9.60 | 14.92 |
| | UK | 0.784 | 0.709 | Good | 11.16 | 17.30 |
| | OK-C | 0.779 | 0.757 | Very Good | 10.23 | 15.82 |
| | OK-E | 0.781 | 0.765 | Very Good | 10.10 | 15.65 |
| | OK-G | 0.801 | 0.776 | Very Good | 9.62 | 15.20 |
| | OK-S | 0.778 | 0.759 | Very Good | 10.10 | 15.79 |
| 18496 Halkapınar/İvriz | IDW | 0.725 | 0.710 | Good | 9.19 | 14.42 |
| | Sp-R | 0.505 | 0.378 | Unsatisfactory | 14.32 | 21.16 |
| | Sp-T | 0.613 | 0.558 | Satisfactory | 11.64 | 17.79 |
| | UK | 0.751 | 0.712 | Good | 9.17 | 14.39 |
| | OK-C | 0.742 | 0.716 | Good | 9.46 | 14.28 |
| | OK-E | 0.730 | 0.708 | Good | 9.40 | 14.47 |
| | OK-G | 0.744 | 0.714 | Good | 9.37 | 14.31 |
| | OK-S | 0.727 | 0.705 | Good | 9.51 | 14.54 |
| 18213 Karatay(TAGEM) | IDW | 0.777 | 0.530 | Satisfactory | 10.69 | 14.72 |
| | Sp-R | 0.777 | 0.663 | Good | 8.10 | 12.43 |
| | Sp-T | 0.785 | 0.646 | Satisfactory | 8.42 | 12.75 |
| | UK | 0.662 | 0.453 | Unsatisfactory | 12.01 | 15.89 |
| | OK-C | 0.719 | 0.521 | Satisfactory | 11.25 | 14.89 |
| | OK-E | 0.727 | 0.521 | Satisfactory | 11.29 | 14.89 |
| | OK-G | 0.707 | 0.485 | Unsatisfactory | 11.75 | 15.46 |
| | OK-S | 0.716 | 0.517 | Satisfactory | 11.26 | 14.91 |

Table 7. The short period (2014-2019) performance values of interpolation methods (continued)

| Station Name | Model Name | R ² | NSE | Performance | MAE (mm) | RMSE (mm) |
|---------------------|-------------|----------------|--------------|---------------------|-------------|--------------|
| 18117 Sultanhanı | IDW | 0.569 | 0.528 | Satisfactory | 10.26 | 15.64 |
| | Sp-R | 0.478 | 0.371 | Unsatisfactory | 11.75 | 18.14 |
| | Sp-T | 0.508 | 0.458 | Unsatisfactory | 10.33 | 16.80 |
| | UK | 0.569 | 0.527 | Satisfactory | 9.59 | 15.71 |
| | OK-C | 0.574 | 0.528 | Satisfactory | 9.50 | 15.70 |
| | OK-E | 0.552 | 0.496 | Unsatisfactory | 10.12 | 16.25 |
| | OK-G | 0.576 | 0.533 | Satisfactory | 9.30 | 15.61 |
| | OK-S | 0.564 | 0.515 | Satisfactory | 9.70 | 15.93 |
| 18502 Bor | IDW | 0.764 | 0.721 | Good | 8.26 | 11.70 |
| | Sp-R | 0.729 | 0.681 | Good | 8.58 | 12.52 |
| | Sp-T | 0.750 | 0.714 | Good | 7.99 | 11.83 |
| | UK | 0.762 | 0.718 | Good | 8.63 | 11.84 |
| | OK-C | 0.754 | 0.726 | Good | 8.39 | 11.63 |
| | OK-E | 0.754 | 0.731 | Good | 8.32 | 11.56 |
| | OK-G | 0.761 | 0.728 | Good | 8.36 | 11.59 |
| | OK-S | 0.749 | 0.721 | Good | 8.46 | 11.68 |
| 18482 Gülağaç | IDW | 0.721 | 0.441 | Unsatisfactory | 10.92 | 16.03 |
| | Sp-R | 0.293 | -1.044 | Unsatisfactory | 19.51 | 30.62 |
| | Sp-T | 0.486 | -0.247 | Unsatisfactory | 14.56 | 23.87 |
| | UK | 0.777 | 0.740 | Good | 7.37 | 10.82 |
| | OK-C | 0.714 | 0.632 | Satisfactory | 8.38 | 12.94 |
| | OK-E | 0.665 | 0.562 | Satisfactory | 9.41 | 14.17 |
| | OK-G | 0.724 | 0.636 | Satisfactory | 8.28 | 12.93 |
| | OK-S | 0.702 | 0.614 | Satisfactory | 8.68 | 13.32 |

In Table 7, IDW models showed the highest prediction success with NSE= 0.843 (very good), NSE= 0.720 (good), NSE= 0.822 (very good), and NSE= 0.836 (very good) for Seydişehir, Karapınar, Bozkır, and Kazımkarabekir stations, respectively. For the Karatay (TAGEM) station, the Sp-R model showed the best performance with NSE=0.663 and achieved “good” prediction success. The best-performing interpolation method for Cihanbeyli was Sp-T, which showed a “good” prediction success with NSE=0.739. For Sultanhanı station, the highest NSE value was obtained for the OK-G model, and “satisfactory” prediction success was obtained with NSE=0.533. At Gülağaç station, the UK method showed the highest prediction success with NSE= 0.740 (good). For Halkapınar/İvriz, the OK-C model showed the best performance with a value of NSE=0.716 (good). At this station, the OK-G method also performed very close to the OK-C method. The model with the best performance for Bor station was the OK-E model with NSE=0.731, which is at a “good” level.

Figure 5 shows the time series and scatter diagrams of the methods with the highest success in the test stations for the period 2014-2019. The IDW model was the most successful interpolation model at Seydişehir and Kazımkarabekir stations. It is seen that the precipitation estimates obtained with IDW represent the behavior of the observed precipitation at these stations quite consistently. Sultanhanı was the station with the least agreement between the observation and simulation (model) data. However, this station achieved a “satisfactory” success level in the OK-G model with the value of NSE = 0.533.

Monthly total precipitation maps of the interpolation methods applied for the short period between 2014 and 2019 are given in Figure 6. In this period, the stations used in the spatial distribution are shown on the IDW map using the station codes specified in Table 1, and the test stations are shown on the IDW map using their names. When the precipitation distribution maps are examined, it is seen that the monthly average precipitation in the IDW method varies between 25 and 96 mm. In the IDW method, it is seen that the maximum precipitation is around Seydişehir/Alacabel (S9) and Derebucak (S16), and the minimum precipitation is around Eskil (S21). In the Sp-R method, the monthly average precipitation varies between 0 and 107 mm, and in the Sp-T method, it varies between 17 and 101 mm. According to the Sp-R and Sp-T methods, maximum precipitation falls around Seydişehir/Alacabel (S9), Derebucak (S16), and Seydişehir. In the Sp-R method, minimum precipitation is seen in an area starting from Eskil (S21) and

Halkapınar/İvriz (S30) station to the borders of the Eastern Mediterranean and Seyhan Basins. In the Sp-T method, the minimum area in the Sp-R method narrowed, and Halkapınar/İvriz station remained outside the minimum area.

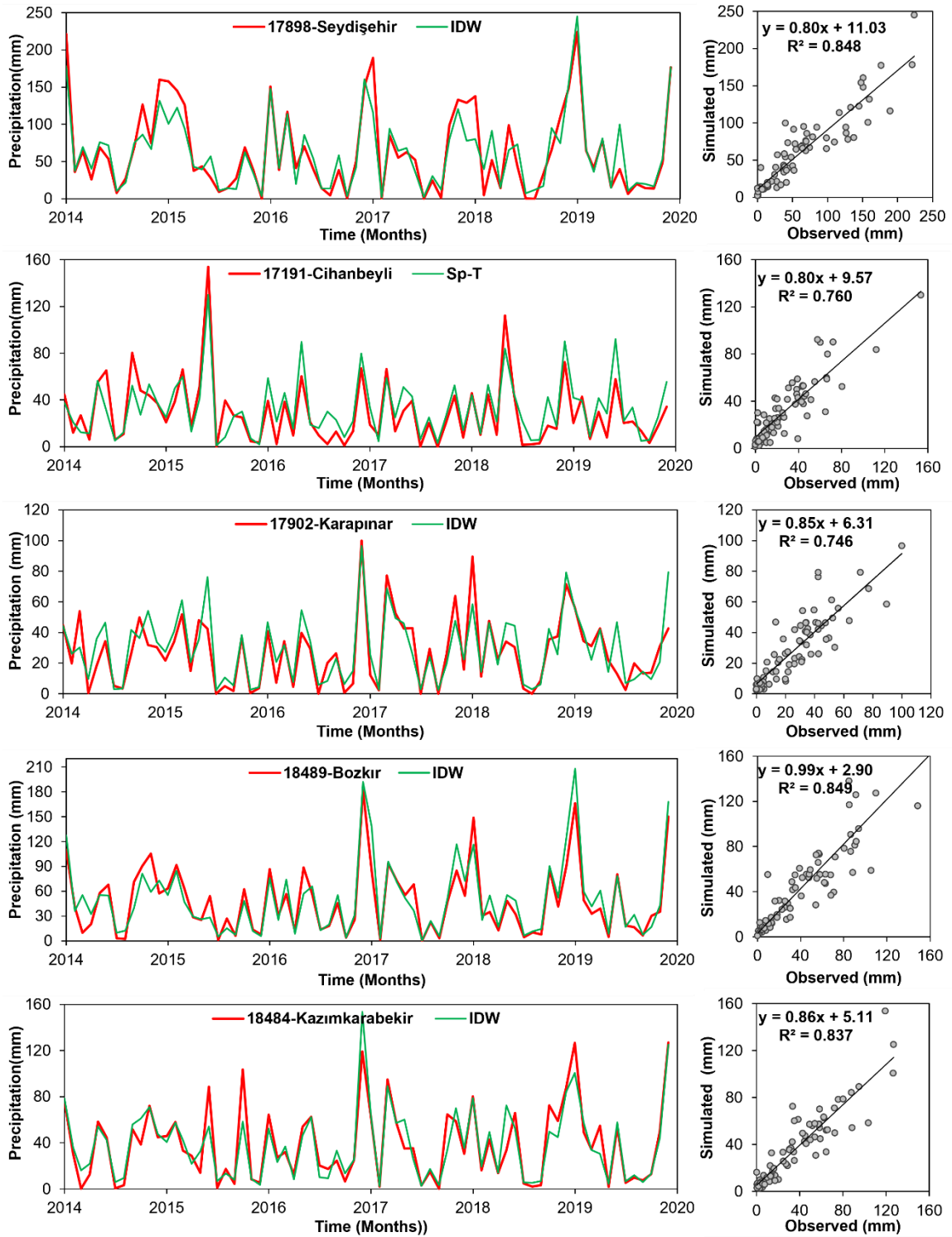


Figure 5. Time series and scatter diagrams for the period 2014-2019

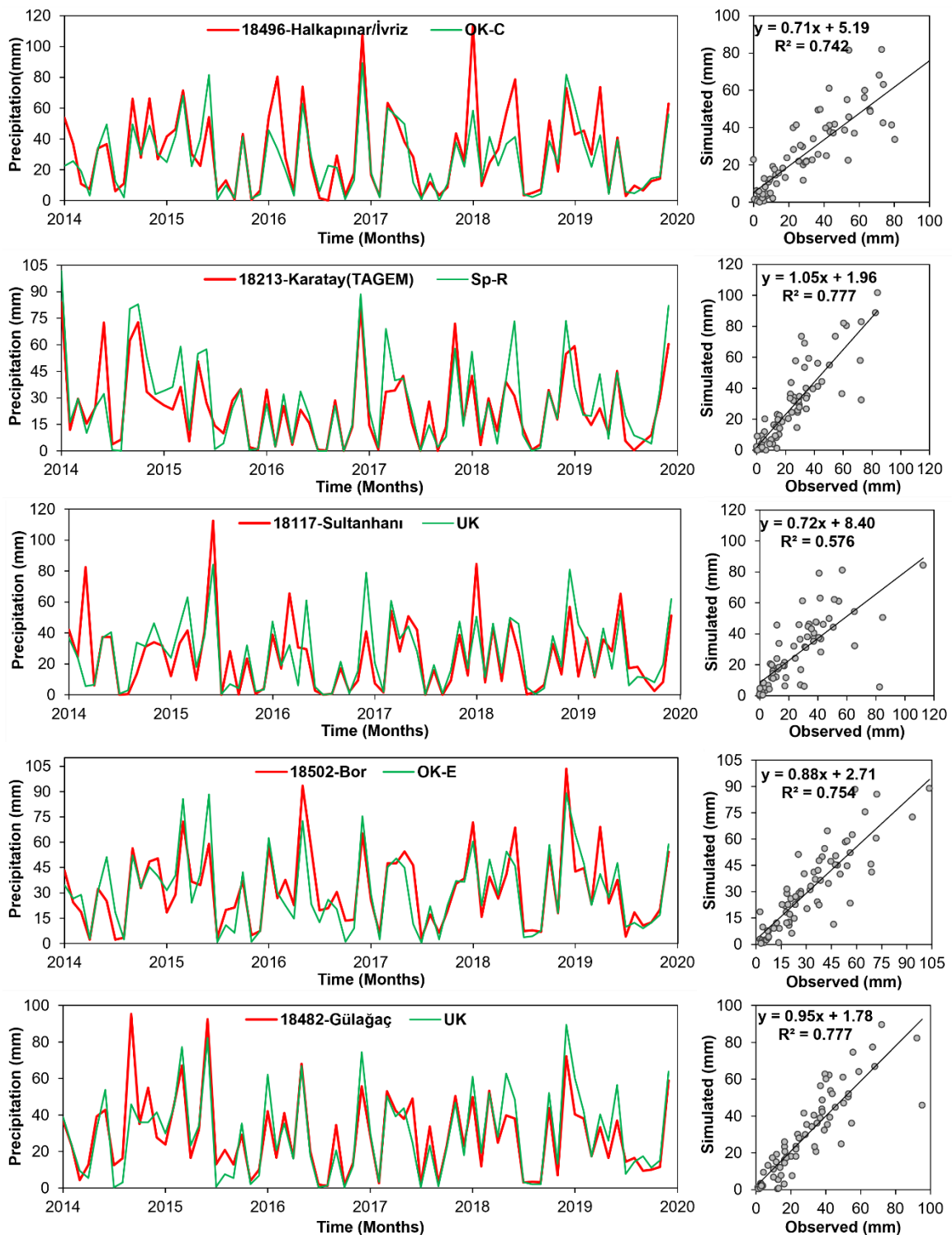


Figure 5. Time series and scatter diagrams for the period 2014-2019 (continued)

In the UK method, the monthly average precipitation is distributed between 26 and 57 mm. The amount of precipitation increases as it approaches the Antalya Basin. It is observed that the color and pattern distribution is less in the UK method compared to the other methods. In the OK methods, the monthly average precipitation amounts start from 25 mm and reach up to 82 mm. The most distinct pattern type is seen in the OK-C method, while the value ranges narrow and the patterns decrease in the OK-S, OK-G, and OK-E methods, respectively. It is seen that the maximum precipitation in the OK

methods is around Seydişehir/Alacabel (S9), Derebucak (S16), and Seydişehir. Unlike these, the maximum precipitation is seen around Bozkır station and Cihanbeyli station in the OK-E method.

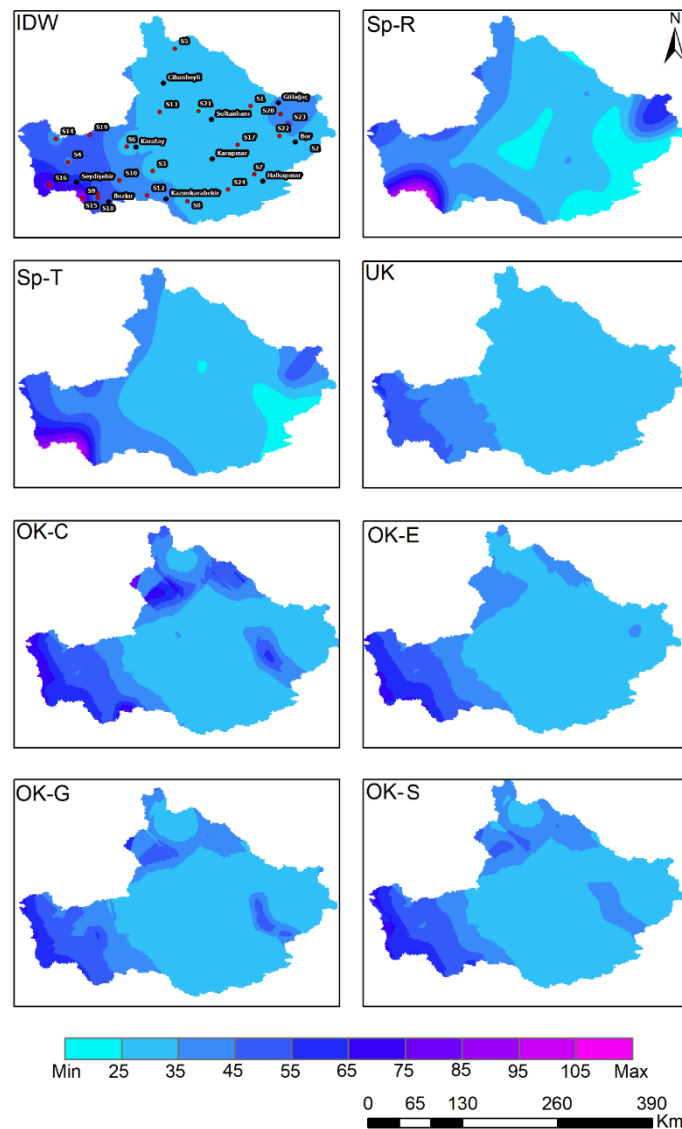


Figure 6. Spatial distribution of monthly total precipitation in KCB (2014-2019)

The model performance of the common test stations, Seydişehir, Cihanbeyli, and Karapınar stations, in the long and short periods was compared according to the NSE metric (Table 8). The most successful interpolation methods obtained in both periods are shown in bold in Table 8.

For monthly total precipitation estimation, the most successful model obtained in the long period at Seydişehir station was Sp-R with a value of $NSE=0.561$ (satisfactory), while the most successful model in the short period was the IDW method with a value of $NSE=0.843$ (very good). At Seydişehir station, NSE values always increased in all interpolation methods except Sp-R in the short period compared to the long period, and they exhibited higher success in estimating monthly total precipitation. The only method whose NSE value decreased in the short period compared to the long period was the Sp-R method. While the Sp-R method was the interpolation method that most successfully estimated the monthly total precipitation in Seydişehir in the long period, it was the method with the lowest estimation success in the short period. The NSE value obtained with Sp-R was at the “satisfactory” level with 0.561 in the long period, while it was at the “unsatisfactory” level with 0.397 in the short period.

Table 8. Performance values of interpolation models for long and short period

| Station Name | Model Name | 1971-2019 | | 2014-2019 | | Change |
|---------------------|------------|--------------|---------------------|--------------|------------------|--------|
| | | NSE | Performance | NSE | Performance | |
| 17898 Seydişehir | IDW | 0.503 | Satisfactory | 0.843 | Very Good | ↑ |
| | Sp-R | 0.561 | Satisfactory | 0.397 | Unsatisfactory | ↓ |
| | Sp-T | 0.556 | Satisfactory | 0.557 | Satisfactory | ↑ |
| | UK | 0.137 | Unsatisfactory | 0.627 | Satisfactory | ↑ |
| | OK-C | 0.409 | Unsatisfactory | 0.665 | Good | ↑ |
| | OK-E | 0.404 | Unsatisfactory | 0.536 | Satisfactory | ↑ |
| | OK-G | 0.370 | Unsatisfactory | 0.701 | Good | ↑ |
| | OK-S | 0.413 | Unsatisfactory | 0.622 | Satisfactory | ↑ |
| 17191 Cihanbeyli | IDW | 0.719 | Good | 0.722 | Good | ↑ |
| | Sp-R | 0.659 | Good | 0.676 | Good | ↑ |
| | Sp-T | 0.721 | Good | 0.739 | Good | ↑ |
| | UK | 0.644 | Satisfactory | 0.666 | Good | ↑ |
| | OK-C | 0.605 | Satisfactory | -20.252 | Unsatisfactory | ↓ |
| | OK-E | 0.294 | Unsatisfactory | -1.762 | Unsatisfactory | ↓ |
| | OK-G | 0.710 | Good | -31.908 | Unsatisfactory | ↓ |
| | OK-S | 0.566 | Satisfactory | -15.837 | Unsatisfactory | ↓ |
| 17902 Karapınar | IDW | 0.686 | Good | 0.720 | Good | ↑ |
| | Sp-R | 0.612 | Satisfactory | 0.203 | Unsatisfactory | ↓ |
| | Sp-T | 0.683 | Good | 0.685 | Good | ↑ |
| | UK | 0.513 | Satisfactory | 0.681 | Good | ↑ |
| | OK-C | 0.648 | Satisfactory | 0.672 | Good | ↑ |
| | OK-E | 0.319 | Unsatisfactory | 0.662 | Good | ↑ |
| | OK-G | 0.704 | Good | 0.678 | Good | ↓ |
| | OK-S | 0.601 | Satisfactory | 0.647 | Satisfactory | ↑ |

At Cihanbeyli station, the method with the highest prediction success was the Sp-T method with NSE values of 0.721 and 0.739 in the long and short periods, respectively. In addition, the Sp-T method showed a “good” level of performance. However, the IDW method showed a quite close prediction success to the Sp-T method, with NSE values of 0.719 and 0.733 in both periods. The performance of deterministic methods has increased slightly in the short term compared to the long term. Among the Kriging methods, there was an increase only in the UK in the short period. The performance of OK methods has decreased considerably in the short period and has always at an “unsatisfactory” level.

For Karapınar station, the most successful model in the long period was OK-G with a value of NSE=0.704, while the most successful model in the short period was IDW with a value of NSE=0.720. While NSE values decreased in the short period compared to the long period in OK-G and Sp-R models, higher NSE values were obtained in the remaining methods. The method that obtained the highest increase (decrease) in the NSE value in the short period compared to the long period was the OK-E (Sp-R) method. In 6 of the 8 interpolation methods applied in the short period at Karapınar station, a “good” level of prediction success was achieved with NSE>0.65. In the OK-S method, a “satisfactory” level of prediction success was achieved with NSE=0.647, and success very close to the “good” level was achieved. Only in the Sp-R method, an “unsatisfactory” level of success was achieved with NSE=0.203.

5. CONCLUSION

Interpolation methods are used in hydrological studies to estimate missing data, estimate the data needed at points where observation data is not available, and obtain spatial distribution. In this study, the usability of interpolation methods in estimating monthly total precipitation in KCB was investigated. For this purpose, 8 different interpolation methods were used. While the IDW and Spline methods [Regularized Spline (Sp-R) and Tension Spline (Sp-T)] were used as deterministic methods, OK and UK were used as geostatistical methods, and the estimation performance of all methods was compared. As semivariogram methods, circular (OK-C), exponential (OK-E), gaussian (OK-G), spherical (OK-S) were used for OK, while a Stable semivariogram model was used for the UK. In the study, applications were

carried out with few stations in the 1971-2019 period and with many stations in the 2014-2019 period for monthly total precipitation.

In the period 1971-2019, 8 out of 11 stations were used in spatial distribution with interpolation methods, and the monthly total precipitation data for the remaining 3 stations (Seydişehir, Cihanbeyli, and Karapınar) were estimated. When the performance of the 8 different interpolation methods applied was evaluated, the values of 0.561 (satisfactory), 0.721 (good), and 0.704 (good) were obtained in precipitation estimation at Seydişehir, Cihanbeyli, and Karapınar stations according to the NSE metric, respectively. The most successful interpolation methods at Seydişehir, Cihanbeyli, and Karapınar stations were Sp-R, Sp-T, and OK-G, respectively.

In the period 2014-2019, the spatial distribution of monthly total precipitation was carried out using more stations. In this period, 24 of the 34 stations in the basin were used in the spatial distribution, and the monthly total precipitation values of the remaining 10 stations were estimated. In the most successful interpolation methods obtained at 10 test stations with 8 different methods used, NSE values ranging from 0.533 to 0.843 were obtained. While the lowest success with the value of $NSE=0.533$ was obtained at the "satisfactory" level in the OK-G method at Sultanhanı station, the highest success was obtained with the value of $NSE=0.843$ and at the "very good" level with the IDW method at Seydişehir station.

When the success of estimating monthly total precipitation values of Seydişehir, Cihanbeyli, and Karapınar stations, which are common test stations used in long and short periods, in both periods was evaluated, it was seen that the success of estimating monthly total precipitation increased in the short period where more stations were used in spatial distribution compared to the long period where fewer stations were used in spatial distribution. Importance should be given to the use of water resources and sustainable basin management policies throughout the country, and action plans that are in practice or will be implemented should be accelerated and finalized. Appropriate databases that are easy to access should be created for use in research.

ACKNOWLEDGEMENTS

This study is based on Cansu Hacer KAPLAN's M. Sc. thesis [46]. The authors would like to thank the State Meteorological Service (Türkiye) for providing the precipitation data.

DECLARATION OF ETHICAL STANDARDS

Not applicable.

CREDIT AUTHORSHIP CONTRIBUTION STATEMENT

The authors contributed equally to the study's conception and design.

DECLARATION OF COMPETING INTEREST

The authors declare that they have no known competing interests.

FUNDING

The authors declare that they have no fund, or research grant (and their source) received in the course of study, research, or assembly of the manuscript.

DATA AVAILABILITY

Not applicable.

6. REFERENCES

- [1] C. Berndt, and U. Haberlandt, "Spatial Interpolation of Climate Variables In Northern Germany— Influence of Temporal Resolution and Network Density", *Journal of Hydrology: Regional Studies*, vol. 15, pp. 184-202, 2018.
- [2] P. d. A. Borges, J. Franke, Y. M. T. d. Anunciação, H. Weiss, and C. Bernhofer, "Comparison of Spatial Interpolation Methods for The Estimation of Precipitation Distribution in Distrito Federal, Brazil", *Theoretical and applied climatology*, vol. 123, no.1-2, pp. 335-348, 2015.
- [3] H. Li, D. Wang, V. P. Singh, Y. Wang, and J. Wu, "Developing an entropy and copula-based approach for precipitation monitoring network expansion", *Journal of Hydrology*, vol. 598, no. 126366, 2021.
- [4] K. Price, S. T. Purucker, S. R. Kraemer, J. E. Babendreier, and C. D. Knightes, "Comparison of radar and gauge precipitation data in watershed models across varying spatial and temporal scales", *Hydrological Processes*, vol. 28, no. 9, pp. 3505-3520, 2014.
- [5] H. H. Aksu, "Türkiye'de Yağış Ölçer Ağı Yoğunluğunun Yağış Dağılımı Modellemesine Etkisinin Değerlendirilmesi: Antalya Havzası Örneği", *Turkish Journal of Agriculture-Food Science and Technology*, vol. 12, no. 5, pp. 814-820, 2024.
- [6] E. Taş, "Akarçay Havzasında TRMM ve Co-Kriging Yağış Verilerinin Karşılaştırılması", Uluslararası Su ve Çevre Kongresi (SUÇEV), 22-24 Mart 2018, Bursa, Türkiye, 2018.
- [7] S. A. Matthews, "ArcGIS geostatistical analyst", GIS Resource Document, 02-19, 2002.
- [8] M. I. Kamali, R. Nazari, A. Faridhosseini, H. Ansari, and S. Eslamian, "The determination of reference evapotranspiration for spatial distribution mapping using geostatistics", *Water Resources Management*, vol. 29, pp. 3929-3940, 2015.
- [9] O. M. Katipoğlu, "Spatial analysis of seasonal precipitation using various interpolation methods in the Euphrates basin, Turkey", *Acta Geophysica*, vol. 70, pp. 859-878, 2022.
- [10] C. Childs, "Interpolating surfaces in ArcGIS spatial analyst", *ArcUser*, July-September, 3235 (569), pp. 32-35, 2004.
- [11] A. Kamińska, and A. Grzywna, "Comparison of deterministic interpolation methods for the estimation of groundwater level", *Journal of Ecological Engineering*, vol. 15, no. 4, pp. 55-60, 2014.
- [12] S. K. Adhikary, N. Muttill, and A. G. Yilmaz, "Genetic programming-based ordinary kriging for spatial interpolation of rainfall", *Journal of Hydrologic Engineering*, vol. 21, no. 2, 04015062, 2016.
- [13] S. K. Adhikary, N. Muttill, and A. G. Yilmaz, "Cokriging for enhanced spatial interpolation of rainfall in two Australian catchments", *Hydrological Processes*, vol. 31, no. 12, pp. 2143-2161, 2017.
- [14] A. Antal, P. M. Guerreiro, and S. Cheval, "Comparison of spatial interpolation methods for estimating the precipitation distribution in Portugal", *Theoretical and Applied Climatology*, vol. 145, no. 3, pp. 1193-1206, 2021.
- [15] M. Arganis, M. Preciado, J. J. Baños, and A. Mendoza, "Comparison of Rainfall Interpolation Methods for Obtaining Mean Annual Maximum Precipitation Isohyets in a High Elevation Zone in Mexico", *Magazine of Hydraulics, Pneumatics, Tribology, Ecology, Sensorics, Mechatronics*, vol. 2, pp. 76-89, 2021.
- [16] N. Chutsagulprom, K. Chaisee, B. Wongsaijai, P. Inkeaw, and C. Oonariya, "Spatial interpolation methods for estimating monthly rainfall distribution in Thailand", *Theoretical and Applied Climatology*, vol. 148, no. 1, pp. 317-328, 2022.
- [17] K. F. Fung, K. S. Chew, Y. F. Huang, A. N. Ahmed, F. Y. Teo, J. L. Ng, and A. Elshafie, "Evaluation of spatial interpolation methods and spatiotemporal modeling of rainfall distribution in Peninsular Malaysia", *Ain Shams Engineering Journal*, vol. 13, no. 2, 101571, 2022.
- [18] A. İlker, Ö. Terzi, and E. Şener, "Yağışın Alansal Dağılımının Haritalandırılmasında Enterpolasyon Yöntemlerinin Karşılaştırılması: Akdeniz Bölgesi Örneği", *Teknik Dergi*, vol. 30, no. 3, pp. 9213-9219, 2019.
- [19] M. Javari, "Comparison of interpolation methods for modeling spatial variations of Precipitation in Iran", *International Journal of Environmental & Science Education*, vol. 12, no. 5, pp. 1037-1054, 2017.

- [20] D. Liu, Q. Zhao, D. Fu, S. Guo, P. Liu, and Y. Zeng, "Comparison of spatial interpolation methods for the estimation of precipitation patterns at different time scales to improve the accuracy of discharge simulations," *Hydrology Research*, vol. 51, no. 4, pp. 583–60, 2020.
- [21] A. S. A. Silva, B. Stosic, R. S. C. Menezes, and V. P. Singh, "Comparison of Interpolation Methods for Spatial Distribution of Monthly Precipitation in the State of Pernambuco, Brazil", *Journal of Hydrologic Engineering*, vol. 24, no. 3: 04018068 1 -11, 2019.
- [22] E. D. Taylan, and D. Damçayırı, "Isparta Bölgesi Yağış Değerlerinin IDW ve Kriging Enterpolasyon Yöntemleri ile Tahmini", *Teknik Dergi*, vol. 27, no. 3, pp. 7551-7559, 2016.
- [23] B. Usowicz, J. Lipiec, M. Lukowski, and J. Slominski, "Improvement of Spatial Interpolation of Precipitation Distribution Using Cokriging Incorporating Rain-Gauge and Satellite (SMOS) Soil Moisture Data", *Remote Sensing*, vol. 13, no. 5, 1039, 2021.
- [24] Y. Zhang, Y. Li, X. Ji, X. Luo, and X. Li, "Fine-resolution precipitation mapping in a mountainous watershed: geostatistical downscaling of TRMM products based on environmental variables", *Remote Sensing*, vol. 10, no. 1, 119, 2018.
- [25] S. Zengin Kazancı, and E. Tanır Kayıkçı, "Konumsal Enterpolasyon Yöntemleri Uygulamalarında Optimum Parametre Seçimi: Doğu Karadeniz Bölgesi Günlük Ortalama Sıcaklık Verileri Örneği", 5. Türkiye Harita Bilimsel ve Teknik Kurultayı, Ankara, Türkiye, 25 - 28 Mart 2015, 2015
- [26] S. Hodam, S. Sarkar, A. G. R. Marak, A. Bandyopadhyay, and A. Bhadra, "Spatial Interpolation of Reference Evapotranspiration in India: Comparison of IDW and Kriging Methods", *Journal of The Institution of Engineers (India): Series A*, vol. 98, no. 4, pp. 511–524, 2017.
- [27] N. Malamos, I. L. Tsirogiannis, A. Tegos, A. Efstratiadis, and D. Koutsoyiannis, "Spatial Interpolation of Potential Evapotranspiration for Precision Irrigation Purposes", *European Water*, vol. 59, pp. 303-309, 2017.
- [28] Y. Wu, and M. Hung, "Comparison of spatial interpolation techniques using visualization and quantitative assessment", *Applications of Spatial Statistics*, pp. 17-34, 2016.
- [29] L. Yao, Z. Huo, S. Feng, X. Mao, S. Kang, J. Chen, J. Xu, and T. S. Steenhuis, "Evaluation of spatial interpolation methods for groundwater level in an arid inland oasis, northwest China", *Environmental Earth Sciences*, vol. 71, no. 4, pp. 1911–1924, 2014.
- [30] H. Chen, L. Fan, W. Wu, and H. Liu, "Comparison of spatial interpolation methods for soil moisture and its application for monitoring drought", *Environ Monit Assess*, vol. 189, no. 525, 2017.
- [31] M. Dikici, C. İpek, and İ. Topcu, "Seyhan Havzasında Palmer İndeksleri İle Kuraklık Analizi", International Symposium on Innovative Technologies in Engineering and Science 09-11 November 2018 (ISITES2018 Alanya – Antalya - Turkey), pp. 273-282, 2018.
- [32] M. Hüsrevoğlu, "Jeoistatistik analiz ile yağış haritalarının görselleştirilmesi", Yüksek Lisans Tezi, Selçuk Üniversitesi, Konya, 2018.
- [33] H. M. Doğan, D. S. Yılmaz, and O. M. Kılıç, "Orta Kelkit Havzası'nın Bazı Toprak Özelliklerinin Ters Mesafe Ağırlık Yöntemi (IDW) ile Haritalanması ve Yorumlanması", *Gaziosmanpaşa Bilimsel Araştırma Dergisi*, vol. 6, pp. 46-54, 2013.
- [34] D. Shepard, "A Two-Dimensional Interpolation Function For Irregularly-Spaced Data", Proceedings of the 1968 23rd ACM National Conference, New York, pp. 517–524, 1968.
- [35] A. Şen, "Elektrik Alan Şiddetlerinin Ölçümü ve Coğrafi Bilgi Sistemi Ortamında Yapay Sinir Ağları ile Analizi", Yüksek Lisans Tezi, Yıldız Teknik Üniversitesi, İstanbul, 2007.
- [36] S. A. Kamaruddin, S. N. Zainolabdin, M. A. Roslani, N. S. A. M. Zohir, and N. Y. M. Al-Bakri, "A Comparative Study of the Accuracy of Regularized and Tension Spline Interpolation Methods to Map the Surface Water Temperature of Pulau Tuba, Langkawi, Kedah", In Charting the Sustainable Future of ASEAN in Science and Technology, Proceedings from the 3rd International Conference on the Future of ASEAN (ICoFA) 2019- 2 , 285, Springer Nature, 2020.
- [37] A. Tait, R. Henderson, R. Turner, and X. Zheng, "Thin plate smoothing spline interpolation of Daily rainfall for New Zealand using a climatological rainfall Surface", *International Journal of Climatology*, vol. 26, no. 14, pp. 2097–2115, 2006.

- [38] S. Köroğlu, "Farklı Enterpolasyon Yöntemlerinin Hacim Hesabına Etkisinin Araştırılması", Yüksek Lisans Tezi, İstanbul Teknik Üniversitesi, İstanbul, 2006.
- [39] K. G. van den. Boogaart, and H. Schaeben, "Kriging of Regionalized Directions, Axes, and Orientations I, Directions and Axes", *Mathematical Geology*, vol. 34, no. 5, pp. 479-503, 2002.
- [40] Z. Şen, "Spatial Modeling Principles in Earth Sciences", Berlin/Heidelberg, Germany: Springer International Publishing, 2016.
- [41] O. Aydın, "Türkiye'de Yıllık Ortalama Toplam Yağışın Kriging Yöntemiyle Belirlenmesi", Doktora Tezi, Ankara Üniversitesi, Ankara, 2014.
- [42] K. Johnston, J. M. V. Hoef, K. Krivoruchko, and N. Lucas, "Using ArcGIS Geostatistical Analyst", Esri Redlands, 2001.
- [43] A. G. Journel, and C. J. Huijbregts, "Mining Geostatistics", United Kingdom, Academic Press, 1976.
- [44] R. Webster, and M. A. Oliver, "Geostatistics for Environmental Scientists" Second Edition, England, John Wiley & Sons, pp. 153-197, 2007.
- [45] D. N. Moriasi, J. G. Arnold, M. W. Van Liew, R. L. Bingner, R. D. Harmel, and T. L. Veith, "Model evaluation guidelines for systematic quantification of accuracy in watershed simulations", *Transactions of the ASABE*, vol. 50, no. 3, pp. 885-900, 2007.
- [46] C. H. Kaplan, "Hidrolojik Verilerin Alansal Dağılımında Farklı Enterpolasyon Yöntemlerinin Karşılaştırılması: Uygulama Konya Kapalı Havzası", Yüksek Lisans Tezi, Konya Teknik Üniversitesi, Konya, 2023.