

## MULTI-CRITERIA DECISION MAKING FOR CEMENT MORTAR MIXTURE SELECTION BY FUZZY TOPSIS

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Keywords	Abstract
<i>Fuzzy TOPSIS, Multi-Criteria Decision Making, Cement mortar, Compressive strength.</i>	<i>Cement mortar mixture consists of different materials as the content. The materials which make up this mixture and the selection of this mixture have a vital proposition for the constructions in which this mixture is used. In this selection process, it is very complicated to decide which one material and how to use in the selection. Fuzzy decision-making theory is a very useful method that can be used in such decision-making problems. In this study, it was preferred to use the fuzzy TOPSIS (Technique for Order Preference by Similarity to Ideal Solution) method to find the best cement mortar mixture. For this purpose, the optimum sorting was done for 40 alternatives using five criteria. These five criteria used are; The age of the samples (days), fly ash (FA), silica fume (SF), compressive strength (MPa) and ration of FA+SF mixtures. As a result, this study shows that the presented fuzzy TOPSIS model is able to effectively evaluate fuzziness in the multi-criteria decision process.</i>

## BULANIK TOPSIS İLE ÇİMENTO HARCİ KARIŞIMI SEÇİMİ İÇİN ÇOKLU KRİTERLİ KARAR VERME

Anahtar Kelimeler	Öz
<i>Bulanık TOPSIS, Çok Kriterli Karar Verme, Çimento Karışımı, Basınç dayanımı</i>	<i>Çimento harcı karışımı, içerik olarak farklı malzemelerden oluşmaktadır. Bu karışımı oluşturan malzemeler ve bu karışımın seçimi, bu karışımın kullanıldığı yapılar için hayati öneme sahiptir. Bu seçim sürecinde hangi malzemenin seçileceğine ve nasıl kullanılacağına karar vermek çok karmaşıktır. Bulanık karar verme teorisi, bu tür karar verme problemlerinde kullanılabilecek çok kullanışlı bir yöntemdir. Bu çalışmada, en iyi çimento harcı karışımını bulmak için bulanık TOPSIS yönteminin kullanılması tercih edilmiştir. Bu amaçla, beş kriter kullanılarak 40 adet alternatif için ideal sıralama yapılmıştır. Kullanılan bu beş kriter; numunelerin yaşı (gün), uçucu kül (FA), silis dumanı (SF), basınç dayanımı (MPa) ve FA + SF karışımları oranıdır. Sonuç olarak, bu çalışma sunulan bulanık TOPSIS modelinin çok kriterli karar sürecinde belirsizliği etkili bir şekilde değerlendirebildiğini göstermektedir.</i>
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### 1. Introduction

In recent years, in many studies were assessed the effects of the partial chancing of cement by different types of additions. The added materials are usually trass, blast furnace slag, burned clay, silica fume, zeolite, fly ash, volcanic tuff and metakaolin (Behnood and Ziari,

2008; Kocak, 2010). Additional materials of cementitious usage in concrete and cement technology are preferred because of economic, technical and environmental reasons (Fu et al., 2002; Subasi, 2009; Worrell, Martin and Price, 2000). These cement materials consist of silica fume and fly ash.

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Fly ash is a by-product of coal-fired power plants, which is obtained by separating the powder-burning power plant from flue gas. There are two general classes of fly ash as defined by ASTM C618: class C; high-calcium fly ash and class F; low-calcium fly ash. The on burning conditions and coal quality used determine the its chemical and physical properties (Behnood and Ziari, 2008). Fly ash is added to concretes or directly to mortars or cement of Portland (PC). For different purposes, it is added to the cement as an additive material during the production phase (Aruntas, 2006). The hydration heat is reduced by the use of fly ash, the alkali-silicate reactions are blocked, when used as a cement replacement in the concrete and also the durability is increased. It also contributes to cement and concrete mortars compressive strength by filler effects and pozzolanic (Neville, 2006; Saraswathy, Muralidharan, Thangavel and Srinivasan, 2003). In addition, the use of fly ash partially displaces the production of other concrete components. which in turn reduces CO<sub>2</sub> emissions, protects resources and significantly save energy (Saridemir, 2009). Moreover, the addition of fly ash improves the chemical resistance of the material and contributes significantly to its workability (Garces, Andion, Zornoza, Bonilla and Paya, 2010).

Silica fume obtained by reduction of high-purity quartz with coal in electric arc furnaces in ferrosilicon alloys and silicon metal production (Neville, 2006), improves concrete properties when used as an additive material or it can be used a cement replacement for reducing the cement (Nochaiya, Wongkeo and Chaipanich, 2010). Due to the alkali-silicate reactions, silica fume can result in matrix expansion (Maas, Ideker and Juenger, 2007). While the resistance of concrete against corrosion is increasing, the permeability of silica fume is decreasing (Jo, Kim, Tae and Park, 2007; Qing, Zenan, Deyu and Rongshen, 2007). Furthermore, silica fume contributes to cement and concrete mortars compressive strength and durability (Song, Pack, Nam, Jong and Saraswathy, 2010).

In recent years, fuzzy multi-criteria decision-making methods have become popular and many researchers have used it to solve different problems in many engineering applications, including civil engineering. Different methods are used according to the aim. In the study which Multi-criteria decision-making applications in civil engineering, indicates on MCDM application fields (Zavadskas, Antuchevičienė and Kapliński, 2015). In the study which evaluated the sustainable decision-making in civil engineering, multiple-criteria decision-making (MCDM) theories were emphasized (Zavadskas, Antuchevičienė, Vilutiene and Adeli, 2018). Chen (1997) has solved the problem of selecting materials for tool steel with a new method. In his study, he used linguistic terms to evaluate different criteria importance weights

and alternatives under fuzzy environment. There are used 5 alternative materials and 1 objective and 6 subjective criteria. The weights of all criteria and the ratings of the candidate alternatives as tool steel materials for these criteria are represented using trapezoidal fuzzy numbers.

Ozmen (2012) used fuzzy decision methods for selecting the ideal material for marine environments. In this study, there are 8 alternative materials for using marine environments and 4 criteria and 4 sub-criteria. Selection of the material to be used in marine ambiances is provided with fuzzy TOPSIS approach. Simsek, Ic and Simsek (2013) used TOPSIS-based Taguchi optimization method for determining the ideal mixture rates for high strength self-compacting concrete (HSSCC) in a ready-mixed concrete plant. The criteria used when evaluating with the TOPSIS-based Taguchi approach in the study; T50 time, average convective heat transfer coefficient, the compressive strength, the percentage of air content, the separating tensile strength, the water absorption, the production cost and the slump flow value.

Ertugrul and Karakasoglu (2009) proposed a model using for evaluating the performance of the 15 Turkish cement firms in the Istanbul Stock Exchange. The ranking is determined according to firms financial tables results by Technique for Order Preference by Similarity to Ideal Solution (TOPSIS) and Fuzzy Analytic Hierarchy Process (FAHP) methods.

In this study, it is aimed to select the ideal cement mortar mixture according to the satisfaction criteria weights by using Fuzzy TOPSIS method. For this purpose, 40 different cement mortar mixture specimens were evaluated. We founded the best mixture of cement mortar with the five criteria and 40 alternatives. These five criteria are; the age of samples (days), fly ash (FA), compressive strength (MPa), silica fume (SF) and FA+SF. The TOPSIS method is used to compare these cement mortar mixture specimens and the best alternative was selected according to the criteria importance weight values evaluated by the decision makers.

## 2. Experimental Study

In this study, the PC (CEM I 42.5 R according to TS EN 197-1), FA, SF, standard aggregate and water were used these materials for cement production. PC were produced by Bursa Cement Plant in Turkey. FA which provided from the Kutahya Seyitomer Thermal Power Plant in Turkey has been mixed as small components for cement produce. Also, the SF was attained from the Antalya Etibank electro-ferrochrome business in Turkey. The CEM standard aggregate was arranged by SET Trakya Cement industry according to TS EN 196-1. Cement components are set using tap water in Bursa-Kestel province.

Based on the PC, the experiment is designed using eight different combinations. The total weight of experimental samples is kept constant, three different samples by adding FA is obtained by 10%, 20% and 30% of the total weight into the PC sample. Similarly, two different samples by adding SF is achieved by mixed 5% to 10% of the total weight. For the investigating the properties of triplicate mixtures, The FA and SF are obtained by adding 10% and 20% of total weight in to the PC sample, respectively. In addition, a sample mixture was obtained by displacing the FA and SF ratios. Finally, FA and SF amounts are mixed equally. The samples used in the study were obtained from the experiments in which the chemical and physical properties were analyzed made by Kocak (2010). In this study, the output parameter that compressive strength obtained from experiments is used as criteria.

### 3. Fuzzy TOPSIS Method

For most situations that need to be decided, there is no single criterion. Like these, in situations where a single-criterion approach does not provide a solution, are expressed by multi-criteria decision-making methods (MCDM) (Kelemenis and Askounis, 2010). There are MCDMs with different algorithms in the literature (Lin, Zhangb and Meng, 2015; Ma, Lu and Zhang, 2010; Maity and Chakraborty, 2015). And there are several methods as AHP, ELECTRE, VIKOR, TOPSIS. TOPSIS, one of these methods, developed by Hwang and Yoon, is recommended to approach the selection of the most ideal alternative. The method's focused on the concept that the chosen alternative should have the shortest distance from the positive ideal solution. İdeal solution maximizes the benefit criteria; and the farthest from the negative ideal solution and minimizes the benefit criteria (Dalalah, Hayajneh and Batieha, 2011).

In this paper, all the fuzzy evaluation processes have defined using triangular fuzzy numbers. Thus, before moving onto the fuzzy TOPSIS method, information about the triangular fuzzy number term used in the method will be given.

Triangular fuzzy numbers can be expressed as  $(l, m, u)$  in Figure 1; being a specific type of fuzzy numbers defined with three floating point numbers. Parameters  $(l, m, u)$  express minimum possible number value, the most probable value, and maximum possible value in order.

When processing with a triangular number, linear representation of the number with regard to its right and left values are as such Eq. (1);

$$\mu(x) = \begin{cases} 0 & \text{for } x < l, \\ \frac{x-l}{m-l} & \text{for } l \leq x \leq m, \\ \frac{u-x}{u-m} & \text{for } m \leq x \leq u, \\ 0 & \text{for } x \geq u. \end{cases} \quad (1)$$

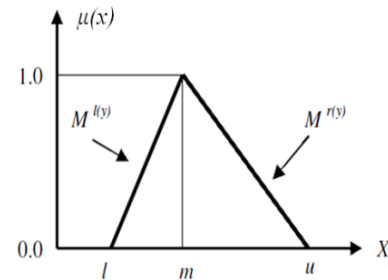


Figure 1. Fuzzy triangular number  $(l, m, u)$

The method is the arrangement of factoring the distance to the ideal solution (TOPSIS). When providing a solution with this method, the distance of all positive and negative alternatives to the ideal solution is calculated. The case of a selected alternative being in the shortest distance to the positive ideal solution and in the longest distance to the negative ideal solution at the same time forms the basis of TOPSIS approach (Chen, 2000).

Steps of the methods are briefly explained:

*Step 1:* Decision maker group and evaluating criteria are determined.

*Step 2:* Linguistic terms in Table 1 for criteria to be weighted and linguistic scores in Table 2 for alternatives to be evaluated are generated.

Table 1  
Linguistic terms and their corresponding fuzzy numbers of the criteria

Linguistic Terms	Fuzzy Numbers
Very important (VI)	(0.75, 1.0, 1.0)
Important (I)	(0.5, 0.75, 1.0)
Fair (F)	(0.25, 0.5, 0.75)
Unimportant (U)	(0, 0.25, 0.5)
Very unimportant (VU)	(0, 0, 0.25)

Table 2  
Linguistic terms and their corresponding fuzzy numbers of the alternatives

Linguistic Terms	Fuzzy Numbers
Very Poor (VP)	(1, 1, 3)
Poor (P)	(1, 3, 5)
Fair (F)	(3, 5, 7)
Good (G)	(5, 7, 9)
Very Good (VG)	(7, 9, 9)

Step 3: Evaluations that N amounts of decision makers carry out for criteria and alternatives are combined. Here,  $\tilde{x}_{ij}^N$  indicates the evaluation of N decision maker and  $\tilde{w}_j^N$ ; indicates the significance of N decision maker.

$$\tilde{x}_{ij} = \frac{1}{N} [\tilde{x}_{ij}^1 \otimes \tilde{x}_{ij}^2 \otimes \dots \otimes \tilde{x}_{ij}^N] \quad (2)$$

$$\tilde{w}_j = \frac{1}{N} [\tilde{w}_j^1 \otimes \tilde{w}_j^2 \otimes \dots \otimes \tilde{w}_j^N] \quad (3)$$

Step 4: The Decision Problem is presented in matrix format in Equation 4 after a single value for all the criteria and alternatives is generated. Here,  $\tilde{x}_{ij} = (a_{ij}, b_{ij}, c_{ij})$  and  $\tilde{w}_j = (w_{j1}, w_{j2}, w_{j3})$  being triangular fuzzy numbers,  $\tilde{D}$  indicates fuzzy decision matrix, and  $\tilde{W}$  indicates fuzzy weights matrix.

$$\tilde{D} = \begin{bmatrix} \tilde{x}_{11} & \tilde{x}_{12} & \dots & \tilde{x}_{1n} \\ \tilde{x}_{21} & \tilde{x}_{22} & \dots & \tilde{x}_{2n} \\ \vdots & \vdots & \dots & \vdots \\ \tilde{x}_{m1} & \tilde{x}_{m2} & \dots & \tilde{x}_{mn} \end{bmatrix} \quad \tilde{W} = [\tilde{w}_1, \tilde{w}_2, \dots, \tilde{w}_n] \quad (4)$$

Step 5: The step after the generation of decision matrix is the normalization of the decision matrix. The fuzzy decision matrix is normalized with the help of Equation 6 and 7 and normalized fuzzy decision matrix  $\tilde{R}$  is obtained.

$$\tilde{R} = [\tilde{r}_{ij}]_{m \times n} \quad (5)$$

and C, being the profit and cost criteria;

$$\tilde{r}_{ij} = \left( \frac{a_{ij}}{c_j^*}, \frac{b_{ij}}{c_j^*}, \frac{c_{ij}}{c_j^*} \right), \quad j \in B, \quad c_j^* = \max_i c_{ij}, \quad j \in B \quad (6)$$

$$\tilde{r}_{ij} = \left( \frac{a_j^-}{c_{ij}}, \frac{a_j^-}{b_{ij}}, \frac{a_j^-}{a_{ij}} \right), \quad j \in C, \quad a_j^- = \min_i a_{ij}, \quad j \in C \quad (7)$$

calculated as. Here,  $\tilde{r}_{ij}, (\forall i, j)$  resemble normalized triangular fuzzy numbers.

Step 6: Taking the fact that each decision criteria might have different significance into factor after the normalized fuzzy deciding matrix is generated, the weighted normalized fuzzy decision matrix is generated in this manner:

$$\tilde{V} = [\tilde{v}_{ij}]_{m \times n} \quad i = 1, 2, \dots, m \quad j = 1, 2, \dots, n \quad (8)$$

Here it is expressed as,  $\tilde{v}_{ij} = \tilde{r}_{ij}(\cdot) \tilde{w}_{ij}$ .

Step 7: After normalized fuzzy decision matrix is generated, fuzzy positive ideal solution (FPIS,  $A^*$ ) and fuzzy negative ideal solution (FNIS,  $\bar{A}$ ) are identified as:

$$A^* = (\tilde{v}_1^*, \tilde{v}_2^*, \dots, \tilde{v}_n^*) \quad A^- = (\tilde{v}_1^-, \tilde{v}_2^-, \dots, \tilde{v}_n^-) \quad (9)$$

Here it is expressed as,  $\tilde{v}_j^* = (1, 1, 1)$  and  $\tilde{v}_j^- = (0, 0, 0) \quad j = 1, 2, \dots, n$

Step 8: And then, the distance of each alternative to the positive ideal solution ( $A^*$ ) and negative ideal solution ( $\bar{A}$ ) is calculated. Here,  $d(\cdot, \cdot)$  indicates the distance between two fuzzy numbers and is calculated with the help of vertex method.

$$d_i^* = \sum_{j=1}^n d_v(\tilde{v}_{ij}, \tilde{v}_j^*) \quad i = 1, 2, \dots, m$$

$$d_i^- = \sum_{j=1}^n d_v(\tilde{v}_{ij}, \tilde{v}_j^-) \quad i = 1, 2, \dots, m \quad (10)$$

Step 9: Affinity parameters of each alternative are calculated.

$$CC_i = \frac{d_i^-}{d_i^* + d_i^-}, \quad i = 1, 2, \dots, m \quad (11)$$

Step 10: With the action of distance parameters are sorted descending, preference order of the alternatives is obtained (Chen, 2000).

According to these rules, 40 cement mortar mixture species ( $A_1 \dots A_{40}$ ) are evaluated with fuzzy TOPSIS method. For this purpose, 5 criteria which were determined by the decision maker, are evaluated. The cement mortar mixture selection criteria and the importance weights of the criteria are shown in Table 3 and Table 4, respectively.

Table 3  
Selection criteria

Subjective Criteria	Objective Criteria
Age of samples (days) (C1)	Compressive strength (MPa)(C5)
FA (C2)	
SF (C3)	
FA+SF (C4)	

(8) Table 4  
The importance weights of the five criteria

Criteria	Decision-maker
C1	Very Important (VI)
C2	Important (I)
C3	Unimportant (U)
C4	Fair (F)
C5	Very Important (VI)

In this study, linguistic terms used in the evaluation of alternatives and criteria were indicated by positive triangular fuzzy numbers. The ratings of the candidate cement mortar mixtures under the five criteria are shown in Table 5. The decision matrix is calculated with linguistic terms and their fuzzy numbers values of the alternatives.

The matrix of normalized alternative and the matrix of finally the weighted normalized alternative are calculated with Equations 5-8. The distances of each candidate cement mortar mixture from the ideal and the rank the alternatives are calculated. The closeness coefficient (CC) values of the alternatives are shown Table 6.

Table 5. Ratings of the candidate cement mortar mixtures

Candidate Alternatives	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>	C <sub>5</sub> (MPa)
A1	P	P	P	VP	32,7
A2	F	VG	VG	VP	59,5
A3	F	F	F	VP	50,9
A4	G	VG	VG	VP	62,7
A5	VG	F	F	VP	64,6
A6	VG	VP	VP	VP	25,9
A7	VP	VP	VP	VP	11,7
A8	VP	F	VG	VG	23,3
A9	VP	P	F	VG	19,2
A10	P	VG	VG	VP	46,5
A11	VG	VG	VG	VP	63,6
A12	VG	P	P	VP	52,3
A13	VP	F	F	VP	24
A14	VP	P	P	VP	19,5
A15	VP	F	G	F	26,1
A16	P	F	F	VP	39
A17	F	P	F	VG	52,9
A18	G	P	P	VP	50,8
A19	G	VP	VP	VP	23,1
A20	VG	G	VG	F	63,2

Candidate Alternatives	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>	C <sub>5</sub> (MPa)
A21	VG	F	G	F	63,8
A22	P	F	G	F	40,3
A23	F	G	VG	F	57,8
A24	VP	VG	VG	VP	29,7
A25	VP	G	VG	F	26,3
A26	P	F	VG	VG	37,8
A27	F	F	F	VP	52
A28	F	P	P	VP	48
A29	F	F	VG	VG	54,3
A30	G	G	VG	F	65,2
A31	G	F	VG	VG	60,6
A32	G	F	G	F	58,2
A33	G	P	F	VG	57,5
A34	P	VP	VP	VP	14,7
A35	P	G	VG	F	42,6
A36	P	P	F	VG	33
A37	F	VP	VP	VP	32,3
A38	F	F	G	F	53,2
A39	VG	F	VG	VG	62,6
A40	VG	P	F	VG	58,4

Table 6. Closeness coefficient table

Candidate Alternatives	CC <sub>i</sub>	Ranking
A1	0,37678	35
A2	0,47528	12
A3	0,43940	22
A4	0,49382	5
A5	0,47806	10
A6	0,40094	31
A7	0,30161	40
A8	0,40934	29
A9	0,37957	34
A10	0,44662	19
A11	0,50486	3
A12	0,44860	17
A13	0,37387	37
A14	0,34097	38
A15	0,39712	32
A16	0,40825	30
A17	0,45009	16
A18	0,43599	23
A19	0,38514	33
A20	0,50757	1

Candidate Alternatives	CC <sub>i</sub>	Ranking
A21	0,49360	7
A22	0,42838	24
A23	0,47740	11
A24	0,41402	27
A25	0,41489	25
A26	0,43985	21
A27	0,44041	20
A28	0,41466	26
A29	0,47274	13
A30	0,49830	4
A31	0,49368	6
A32	0,47943	9
A33	0,47083	14
A34	0,32858	39
A35	0,44675	18
A36	0,41159	28
A37	0,37456	36
A38	0,45875	15
A39	0,50534	2
A40	0,48213	8

The alternative that has the greatest value according to the alternative CC closest to the ideal. The ranking of the cement mortar mixture alternatives is shown Table 7.

Table 7.  
Ranked Fuzzy TOPSIS results

Ranking	Candidate Alternatives
1	A20
2	A39
3	A11
4	A30
5	A4
6	A31
7	A21
8	A40
9	A32
10	A5
11	A23
12	A2
13	A29
14	A33
15	A38
16	A17
17	A12
18	A35
19	A10
20	A27

Ranking	Candidate Alternatives
21	A26
22	A3
23	A18
24	A22
25	A25
26	A28
27	A24
28	A36
29	A8
30	A16
31	A6
32	A15
33	A19
34	A9
35	A1
36	A37
37	A13
38	A14
39	A34
40	A7

#### 4. Results and Discussion

The TOPSIS method can be used with linguistic variables, where alternatives are evaluated for multi-decision criteria, and where group decisions are required. The reason for choosing the TOPSIS method in this study is the multitude of alternatives and a MCDM process.

In this study 40 cement mortar mixture species were evaluated for 5 criteria and the results were obtained. According to the closeness coefficients of the 40 alternatives examined in the study, the A<sub>20</sub> alternative appears to be the best result with the highest CC value. Thus, the best selection is cement mortar mixture is A<sub>20</sub>. The A<sub>7</sub> is the worst alternative that can be selected according to the weight of criteria. It is seen that the alternative coefficients have a narrow range (0,30161-0,50757) of convergence coefficients and that their coefficients of closeness are very close to each other. The best alternative chosen is determined by the criteria weighted by the decision-maker. Another decision-maker may obtain a different selected alternative by evaluating the criterion weights of the alternative it satisfied to select. Fuzzy TOPSIS method facilitates the decision-making process in such cases where the qualities of the candidates are very close to each other and it is difficult to decide.

#### 5. Conclusion

In this paper, TOPSIS method was used as a decision tool to solve the cement mortar selection problem. TOPSIS

method can be used for the selection the 2, 7, 28, 56 and 90 day's compressive strength values of cement mortars containing FA, SF and FA+SF. In this study, analysis has been made for a decision maker. The number of decision makers can be increased. It is possible to have multiple decision makers participate in the decision with different weights. Proximity coefficients of the alternatives were found, and alternatives were sorted according to these values. The ranking is based on the criteria weighted by the decision maker. The reason for choosing the fuzzy TOPSIS method is when selecting the best alternative to evaluate both the most suitable and the most unsuitable alternative together.

As a result, TOPSIS, which is used as a multi-criteria decision-making method, aims to find the best alternative among the alternatives according to the weight determined by the decision makers.

#### Conflict of Interest

No conflict of interest was declared by the authors.

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