

**CORRECTION TO THE PAPER**  
**"A NOTE ON COMPACT CONVEX SETS WITH EQUAL**  
**SUPPORT PROPERTY" OF Ş. ALPAY PUBLISHED IN**  
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Since this work [1] was submitted in 1977 and appeared in 1987, we believe some remarks as well as some essential corrections are in order,

The measure  $\mu_y$  in the proof of Proposition 2.1. should be  $\mu_y = \frac{1}{2} (\epsilon_y + \epsilon_{-y})$ .

In Example 2.2,  $x$  should be  $\left(\frac{1}{2} + \frac{1}{2^2}, \frac{1}{2^3}, \frac{1}{2^4}, \dots\right)$ .

If  $X$  is a compact convex set we identify  $X$  with its canonical image in  $A(X)^*$ . If  $M$  is a weak\* closed subspace of finite codimension in  $A(X)^*$  then  $M \cap X$  is called a finite codimensional slice of  $X$ . Therefore Example 2.3. also shows that a finite codimensional slice of a compact convex set with e.s.p. need not have e.s.p.. Measures  $\mu_1, \mu_2$  of the same example should read as

$$\mu_1 = \frac{1}{2} \epsilon_{e_1} + \frac{1}{2} \epsilon_{e_2}, \mu_2 = \frac{1}{2} \epsilon_{e_3} + \frac{1}{2} \epsilon_{e_4}.$$

Simple examples in the plane show that product of compact convex sets with e.s.p. does not have e.s.p.. However the remark following Proposition 2.5. shows that if the product  $\prod_{\alpha} X_{\alpha}$  has e.s.p. then each  $X_{\alpha}$  has e.s.p..

**2.7. Definition.** A compact convex set  $X$  is  $(\alpha, n)$ -additive at  $\underline{0}$  if

$$p(x_1) + \dots + p(x_n) \leq \alpha \cdot p(x_1 + \dots + x_n) \text{ for any } x_1, \dots, x_n \text{ in } X.$$

Proposition 2.10. and its Corollary should read as follows:

**2.10. Proposition.** A compact convex set  $X$  with e.s.p. is 1-conical at each isolated extreme point.

**2.11. Corollary.** Every isolated  $G_{\delta}$ -extreme point  $x$  of  $X$  is exposed.

Remarks following Corollary 2.11. indicate that compact convex sets with s.e.s.p. are CE-compact convex sets. However a square is a CE-compact convex set that does not have the s.e.s.p. If  $X$  has the s.e.s.p. and  $\pi : X \rightarrow X'$  is a continuous affine surjection with  $\pi^{-1} \pi(F) = F$  for each closed face  $F$  of  $X$  then  $X'$  has also the s.e.s.p. [2]. However the condition  $\pi^{-1} \pi(F) = F$  on closed faces of

$X$  is indispensable as seen by projecting a tetrahedron onto a rectangle in a one-to-one fashion on the extreme boundary.

Let us note, before giving condition (\*), that if  $X$  has the e.s.p. and  $\{x_\alpha\}$  is a net in  $X_e$  converging to  $x \in X$  then  $\{x_\alpha\}$  structurally converges to  $z$  for each  $z$  in  $\Phi(x)$ .

Part of proof of Proposition 3.4. where  $F = \overline{\text{conv } R}$  is shown to be a face, can be shortened considerably if Theorem 1.4 in [3] is used.

$a$  in Corollary 3.5. should be taken as  $a \geq 0$ .

**3.6. Corollary.** Let  $X$  be a metrizable compact convex set with e.s.p. A subset  $E$  of  $X_e$  is structurally sequentially compact if and only if it is structurally compact.

We note that compact convex sets with e.s.p. were also studied in [4] and [5].

#### R E F E R E N C E S

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