



## TEMPERATURE DEPENDENT (83-483 K) RAMAN SPECTROSCOPY ANALYSIS OF CVD GROWN WS<sub>2</sub> MONOLAYERS

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### ABSTRACT

For novel materials to be used in practical applications, their temperature dependent behavior and limitations need to be understood thoroughly. For example, the mobility of charge carriers, one of the important performance parameters in transistors, strongly depend on the change in the ambient temperature. Hence, characterization of potential optoelectronic materials at extreme temperatures is critical for future applications. In this study, we report on the changes of Raman scattering spectra as the temperature is changed from 83 K to 483 K for the 2D transition metal dichalcogenide materials, namely WS<sub>2</sub> monolayers formed by chemical vapor deposition technique (CVD). Our results show that both E' (E<sub>12g</sub>) and A<sub>1</sub>(A<sub>1g</sub>) modes red shift linearly as the temperature increases. The first order thermal coefficients have been calculated with the Grüneisen model, which suggests that in-plane mode is affected more by the increased temperature than that of out of plane mode. This difference is attributed to the defects in the sample as the flakes are grown by the CVD method. We also investigated the temperature dependence of the second order, 2LA(M) (at 345.7 cm<sup>-1</sup>) which is one of the most intense peaks in the spectra.

**Keywords:** WS<sub>2</sub>, Raman Spectroscopy, Temperature Dependence, Two-dimensional Materials

### 1. INTRODUCTION

Graphene is an exceptional, 2D material and their sheets offers high mobility (200 000 cm<sup>2</sup> v<sup>-1</sup> s<sup>-1</sup>), high thermal conductivity (5300 W/mK) and high Young modulus (~1 TPa) [1-3]. It is a semimetal; it does not have an electronic bandgap around Fermi level, which means its valence and conduction bands touch each other at the Dirac point [4]. This is one of the most important obstacles for the graphene to commercialize in electronic applications, which results in a very low current on-off/ratio and excess heat dissipation when used in different active devices [5, 6]. Such drawbacks of graphene urged scientists to search for other two-dimensional materials, and transition metal dichalcogenide studies have been among the 2D materials that have drawn attention for future optoelectronic applications.

The common form of transition metal dichalcogenides (TMDs) is MX<sub>2</sub>. M corresponds to an element from transition metal group -IV, V or VI- (Ti, Zr, V, Ta, Mo, W) and X is a chalcogen atom such as S, Se or Te; M is sandwiched between two chalcogen atoms [7]. We can categorize them as hexagonal, tetragonal or their distorted form, which depends on the arrangements of the atoms [8]. Generally, while interlayer bonds of TMDs are weak van der Waals type, their intralayer bonds are strong and covalent [9]. While these covalent bonds provide strong in-plane stability, the van der Waals bonds keep the stack together [10]. However, thanks to such weak van der Waals bonds, it is possible to obtain monolayer TMDs by using different techniques where even mechanical exfoliation can be used to isolate them [11]. Earlier theoretical and experimental studies unveiled that when we decrease the number of layers of TMDs, they exhibit a transition from indirect to direct band gap [12, 13]. For example, MoS<sub>2</sub> has an indirect bandgap of 1.29 eV in its bulk form, but when we reduce it to a monolayer, it becomes a direct bandgap material with a 1.90 eV bandgap [12]. WS<sub>2</sub> crystals also show a similar behavior, their bandgap is 1.3 eV in their bulk form, and become direct bandgap material, which is ~2.05 eV. For these TMDs, both the conduction bands (CB) and valence bands (VB) are located at the K points in the Brillouin zone

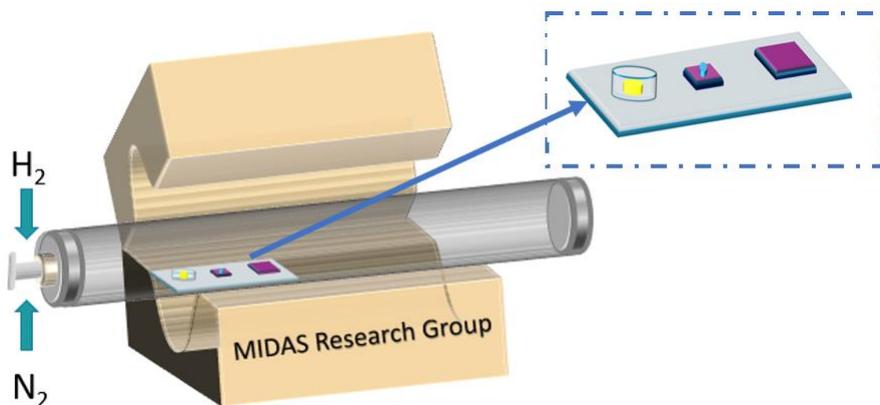
which explains the formation of the direct bandgap in its monolayer form [14]. Monolayers TMDs show high photoluminescence and high absorbance so that they can be used in different optoelectrical applications such as solar cells, photodetectors, LEDs and lasers. However, large area production of TMD materials still hinders their wide usage in practical applications. In spite of its simplicity, mechanical exfoliation is not appropriate for large area production and an alternative method is required for large area-coverage of such monolayers with high quality. In our study, we have used chemical vapor deposition (CVD), to obtain uniform, high-quality, large-area flakes and films with rather low defect density in the structure [15, 16]. CVD is also the most widely used technique for large area growth of graphene.

2D WS<sub>2</sub> has rather low electron mass among the other TMDs, so it is expected to have relatively high electron mobility [17]. In earlier studies, monolayer WS<sub>2</sub> showed a mobility of 40-60 cm<sup>2</sup>/Vs at room temperature, and since it is affected by impurities, surface roughness, defects, etc. mobility can be improved depending on the growth and preparation conditions [18-21].

Electron-phonon interactions have a critical impact on the performance of both optical and electronic properties. Therefore, understanding the vibrational characteristics of TMDs is essential for future applications [22]. In the earlier studies, researchers have investigated room temperature vibrational properties of the WS<sub>2</sub> flakes [23, 24]. Also, prior temperature-dependent studies of TMDs present that their growth techniques and their substrates affect the thermal characteristics of the structures [25-28]. In this study, we report an experimental investigation of Raman spectra of WS<sub>2</sub> single layers grown on Si/SiO<sub>2</sub> substrates where the temperature is changed from 83 K to 483 K to reveal their potential for the applications that are durable under harsh conditions such as space, defense, and marine.

## 2. EXPERIMENTAL PROCEDURE

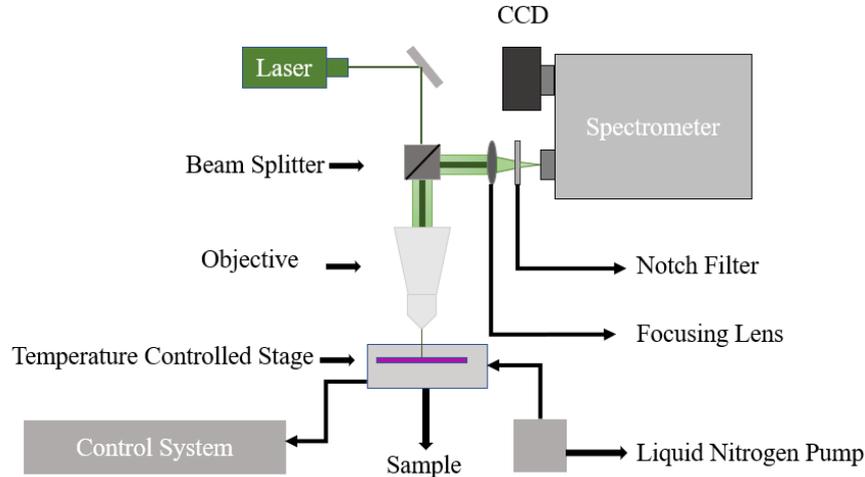
In this study, we grow two-dimensional monolayer WS<sub>2</sub> flakes with chemical vapor deposition method and we use a special design two temperature zone CVD system. Before the experiments, we clean the Si/SiO<sub>2</sub> substrates with three solvent process (acetone, isopropanol and distilled water). We utilize WO<sub>3</sub> (Sigma-Aldrich, 99.5%) and sulfur (Sigma-Aldrich, 99.5%) as precursors and use N<sub>2</sub> gas as a carrier. Also, we make use of H<sub>2</sub> for its promoting effect [29]. We change the position of the furnace at 820°C and introduce WO<sub>3</sub> to react with sulfur. We wait for 3 minutes for the chemical reactions to form monolayer flakes. When the experimental procedure is over, we leave the furnace to cool down to the ambient temperature.



**Figure 1.** Two-zone (temperature) CVD system, inset shows the growth configuration including the precursors and substrate.

Raman spectroscopy analysis is the backbone of this study. In Figure 2, the working principle of our system is summarized. The difference between the wavelength of the laser and the scattered light will reveal the information on the crystal structure, lattice vibrations, flake thickness of TMDs and will serve

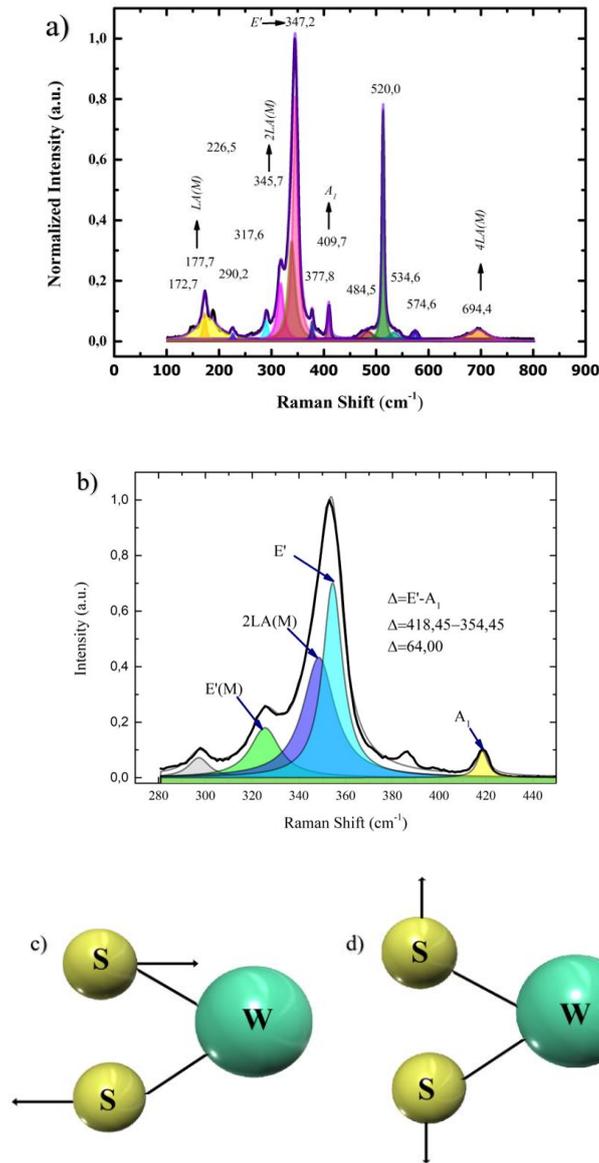
a fingerprint of the materials [30]. To perform temperature dependent measurements, we integrated a temperature stage (THMS600) to our Witec  $\alpha$ -300 R  $\mu$ -Raman system. Using this stage, we could cool down to low temperatures by liquid nitrogen and after performing the measurements, we increased the temperature step by step.



**Figure 2.** Working principle of  $\mu$ -Raman Spectroscopy with the temperature control system

For the measurements, we used 50x (Numerical aperture=0.55) long distance objective with 9.1 mm free working distance. This working distance creates an opportunity for us to work with the temperature stage. Also, to obtain higher resolution, we used a higher grating option. It provides us higher grooves per mm, and this improves the scattering characteristic. Higher number of grooves causes higher scattering, and this increases the resolution of the measurements, so we chose 1200 grooves/mm grating as the measurement parameter. For this measurement setup, our spatial resolution is 967.28 nm. We used a 532 nm laser source with 0.5 mW. We kept the power rather low not to increase the local temperature and avoid damaging the sample during the measurements. For this study, we have performed all measurements in the range of 83 K-483 K with 50 K steps.

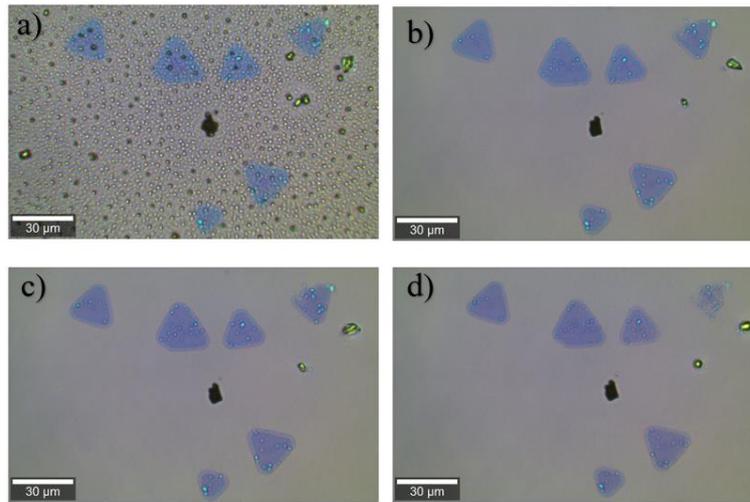
In the literature, the Raman spectra of the monolayer  $WS_2$  have already been reported showing that calculating the difference between the first-order modes at the Brillouin zone center ( $E'$  and  $A_1$ ) is a powerful tool to identify the number of layers of 2D  $WS_2$ . If the difference between  $E'$ -  $A_1$  is lower than 64.5, the flakes are accepted as monolayers [29, 31]. For this reason, in the study, we mainly focus on  $E'$  and  $A_1$  modes (Figure 3b-d). Other modes in Figure 3a represent the longitudinal acoustic (LA) phonons at M point and additional peaks are multi-phonon combination of these modes [32, 33].



**Figure 3.** (a) Lorentzian fitted Raman spectrum of monolayer WS<sub>2</sub> (b) the peaks at the Brillouin zone; (c, d) schematic representation of a typical WS<sub>2</sub> structure with the sulfur atoms in yellow and the tungsten atoms in green for in-plane mode (E') and out of plane mode (A<sub>1</sub>), respectively.

### 3. RESULTS and DISCUSSIONS

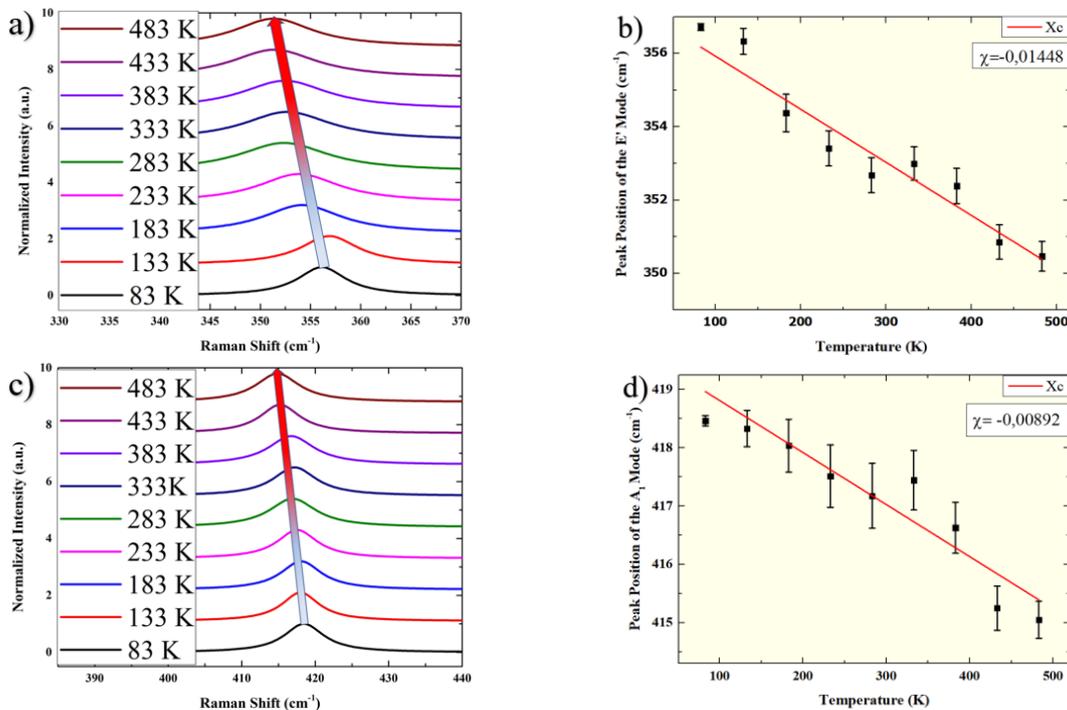
Figure 4 presents the optical images of the CVD grown WS<sub>2</sub> monolayers where these images are taken at different temperatures; Figure 4a, 4b, 4c and 4d show the same sample at different temperatures such as 83 K, 283 K, 483 K and 608 K, respectively. WS<sub>2</sub> monolayers have not been damaged up to 608 K. This shows that WS<sub>2</sub> monolayer based devices will be durable even at extreme conditions such as very high temperatures. The Raman spectral measurements performed at 608 K are not included in the other graphs as the intensity of the measured signal at this temperature becomes very low.



**Figure 4.** Optical image of the WS<sub>2</sub> flakes on Si/SiO<sub>2</sub> substrate with 50x magnification (a) at 83 K, (b) 283 K, (c) 483 K, (d) 608 K

Determining the peak parameters such as peak position, width, intensity, etc. is the goal of Raman peak fitting operation. Since we have sharp peaks in center without long wings, we choose to analyze our experimental data with Lorentzian Function [34]. After analyzing the data, we have separated E' and A<sub>1</sub> modes, and we examined them separately. Grüneisen model provides a quantitative connection between thermal and mechanical properties [35]. We use it to obtain the first-order thermal coefficients of the sample. In Figure 5, we illustrate change the peak position of the E' and A<sub>1</sub> modes depending on the rising temperature. Then we fit our graph with Equation 1. In the equation,  $\chi$  corresponds to the thermal coefficient and,  $\omega_0$  is the frequency of vibrations.

$$\omega(t) = \omega_0 + \chi T \quad (1)$$



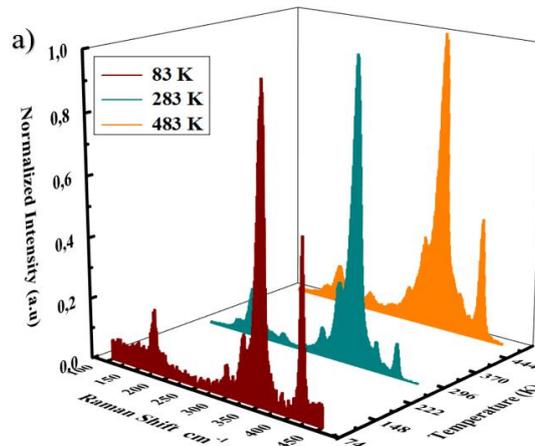
**Figure 5.** Raman shift of E' and A<sub>1</sub> modes as a function of temperature, respectively (a, c). Peak positions of E' and A<sub>1</sub> modes as a function of temperature, respectively (b, d).

The extracted thermal coefficient values for E' and A<sub>1</sub> modes are -0.01448 cm<sup>-1</sup>/K and -0.00892 cm<sup>-1</sup>/K, respectively. It can be seen from the data in Table 1 that the total redshifts of the centers from the starting point (83 K) to the finishing point (483 K) are 6.87 (from 357.30 cm<sup>-1</sup> to 350.43 cm<sup>-1</sup>) and 3.28 (from 418.54 cm<sup>-1</sup> to 415.26 cm<sup>-1</sup>) for E' mode and A<sub>1</sub> mode, respectively. Our results show that temperature change affects E' mode more than that of the A<sub>1</sub> mode. This can be explained by the combined effect of anharmonicity and thermal expansion of the flakes considering that E' mode is in-plane. Also, the observed difference in the behavior of the modes can be attributed to the defects in the sample as the defects such as S deficiency, which becomes more significant with the increased temperature.

**Table 1.** Thermal coefficients and frequency shifts of the peak centers and FWHM values

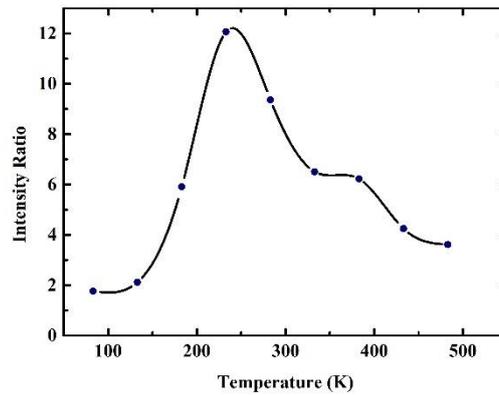
		Thermal Coefficient (cm <sup>-1</sup> /K)	Peak Center Δw (cm <sup>-1</sup> )	FWHM Δw (cm <sup>-1</sup> )
Modes	E'	-0.01448	6.87	6.42
	A <sub>1</sub>	-0.00892	3.28	1.62

Also, the full width at half maximum (FWHM) of the peaks broadens with the escalating temperature. Anharmonicity changes the crystallinity of the material and increase in the temperature activates non-radiative recombination mechanisms. As a consequence, they cause the peaks to broaden with a shift of the peak centers (Figure 6) [36, 37]. As the thermal energy becomes higher, the scattering rate is enhanced. In addition to this, with the increasing anharmonicity, the overtone peaks such as the ones at 228.2 and 377.6 cm<sup>-1</sup> become more visible in the Raman spectra when they are deconvoluted.



**Figure 6.** Three-dimensional representation of normalized intensity vs Raman shift at 83, 283 and 483 K.

2LA(M) (at 345.7 cm<sup>-1</sup>) is a second order mode but at room temperature, it approximately has twice the intensity of A<sub>1</sub> mode [33]. To examine this relationship regarding the temperature effect on these modes, we draw the curve representing the ratio: (intensity of 2LA(M)) / (intensity of A<sub>1</sub>) in Figure 7. At very low and very high temperatures, we observe an unexpected behavior with a significant decrease of the ratio for both low and high temperature cases. We attribute this change to the scattering mechanisms. At low temperatures, impurities affect the scattering and with the increased temperature, probability of lattice scattering enhances [38]. Such higher level of lattice scattering can be caused by anharmonicity. We suggest abnormal impurity scattering at low temperatures due to inefficient purging process. Icing on the sample can cause the decreasing of the intensity (Figure 4 (a)). Since 2LA(M) is a second order mode, it can be affected from the occurrence of the additional scattering processes.



**Figure 7.** The intensity ratio of 2LA(M) and  $A_1$  modes, (intensity of 2LA(M)) / (intensity of  $A_1$ )

#### 4. CONCLUSIONS

In conclusion, we have systematically examined the Raman shifts of different modes of the CVD grown  $WS_2$  flakes on Si/SiO<sub>2</sub> samples within the range of 83 K and 483 K. First of all, we have demonstrated that our atomically thin layers which were grown by CVD are durable down to very low (83 K) and up to very high (608 K) temperatures. With the increased temperature, both  $E'$  and  $A_1$  modes exhibit redshift and broadening in the modes, which can be explained primarily due to change in the anharmonicity and suggestively due to thermal expansion. In addition to this, the  $A_1$  mode shows less temperature dependence. This can be related to the more dominant effect of defects on the in plane ( $E'$ ) mode. Our experimental results provide information on the fundamental thermal parameters of the CVD grown monolayer  $WS_2$  flakes, which is a critical step for the design of novel optoelectronic applications based on two-dimensional transition metal dichalcogenides at extreme temperatures.

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