

## Solar assisted heat pump modelling

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**Abstract**: The Solar Energy Assisted Heat Pump (SAHP) system is modeled by creating different processes with the help of various models created in the JAVA program. The SAHP model was created in order to obtain hot water by utilizing solar energy. The inlet water temperature in the system was taken as 10 °C in December and 20.5 °C in June and the SAHP model was analyzed by numerical method. In the evaporator model, considering the coordinates of the city of Izmir, various graphs were created by calculating the different spectral solar energy values falling on 1 m2 evaporator plate on certain days of 2019. In the graphics, the highest energy density on 1 m2 evaporator plate for İzmir province was 852.095 W/m2 on 21 June at 12:00, and the lowest energy density was 455.143 W/m2 on 21 December at 12:00. In the SAHP system, the evaporator plate area was determined as 2.40 m2 and the compressor power was 0.56kW, and a condenser model was created. The required condenser surface areas were found by calculating the thermal energies given by the condenser for different dates in the system. In the modeling of the heat pump, the Coefficient of Performance (COP) of the SAHP system for R134a and R404A was obtained by taking the date of June 21, 12:00, when the spectral energy is most intense, as a reference.

Keywords: Solar Energy; Solar Powered Heat Pump; JAVA; Modeling; Energy Efficiency; Performance Analysis

### I. Introduction

Harmful effects of burning fossil fuels on the global climate occur day by day. Some institutions have aware of this situation increase environmental protection laws in the world. The European continent aims to be the first climate-neutral continent in the world in 2050, especially with the European green agreement signed by the European Union member states. For this important goal, the European Commission has committed to amending existing environmental legislation, which will reduce the emission rate on the continent by 55% by 2030 [1]. Characteristics of solar energy are intermittence and low density so solar heating has largely been restricted. The solar-assisted heat pump (SAHP) system could be solving the intermittence and low-density solar energy problem. Low-grade thermal energy can be exposed by using SAHP systems. Thus residual heat is useable for applications water heating and space heating, while thermal solar energy must be useful for heating and cooling processes, target utilization areas for solar technologies are those that require low-temperature heat like water heating, space heating, drying process, pool heating, and certain industrial processes [2]. Heat pumps are widely used to upgrade free heat from renewable energy sources and they can provide a dramatic reduction in energy consumption between house utility costs [3]. In the study, solar-assisted evaporator plate modeling was made instead of the fan evaporator which

is used as an evaporator in air-assisted heat pump systems. The solar boosted evaporator plate model was aimed to increase the energy efficiency of the heat pump system. In the JAVA program with SAHP model in the heat pump cycle by doing, it has been made an effort to optimize all systems parameters separately.

### 2. Material and Methods

SAHP model were included the energies kept, emitted and absorbed by the plate together with energy coming from the sun, thermodynamic and thermophysical properties of humid air, thermodynamic and thermophysical properties of refrigerants, double pipe heat exchanger features, Heat pump-refrigeration cycle. As a results of the data outputs of the program various solar energy graphs, JAVA data outputs, evaporate plate heat capacity, condenser heat capacity and condenser area tables have demonstrated for İzmir city.

### 2.1. Mathematical Models

SAHP regions were analyzed by making to solving the mathematical expressions of the energy balance equations of each region with the created JAVA models. As shown in Figure 1, The SAHP system cycle takes place in five main components namely: compressor, condenser (double pipe heat exchanger), expansion valve, evaparatör plate and water storage.

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#### 2.2. Solar Radiation model

The availability of very high altitude aircraft, balloons, and spacecraft have permitted direct measurements of solar radiation outside most or all of the earth's atmosphere. These measurements were made with a variety of instruments in nine separate experimental programs. They resulted in a value of the solar constant  $G_{sc}(\lambda)$  of 1353 W/  $m^2$  with an estimated error of  $\pm 1.5\%$  [4]. The function values of the wavelength of the sun's extraterrestrial solar radiation values between 0.25  $\lambda\,\mu m$  and 8  $\lambda\,\mu m$  were taken into consideration. The cubic strip curve formulas are benefitted by utilize these function values of the wavelength in model. To construct our model, we need to calculate the spectral energy density  $G(\lambda)$  falling on the earth horizontal surface. In the Equation 1  $G(\lambda)$ ,  $G_{sc}(\lambda)$ is the spectral amount of solar energy, n is the day of the year, and  $\theta_z$  zenith angle.

$$G(\lambda) = G_{sc}(\lambda) \left( 1 + 0.0333 \cos\left(\frac{360n}{365}\right) \right) \cos\left(\theta_z\right)_{\tau}$$
(1)

Considering that the energy absorbed by the surface is equal to the energy emitted by the surface according to Kirchhoff's law; directional-spectral emissivity ( $\varepsilon_{\lambda}$ ) = directional-spectral absorptivity ( $\rho_{\lambda}$ ) [5]. Directional-spectral emissivity coefficients ( $\varepsilon_{\lambda}$ ) of a nickel-plated copper selective surface plate were converted to function form using the cubic strip interpolation method. For thermal balance, we have to calculate the best emitter of radiation at every wavelength and in every direction for a blackbody using Planck distribution Equation 2.

$$E_{\lambda,b}\left(\lambda,T\right) = \frac{2\pi h c_0^2}{n^2 \lambda^5 \left[\exp\left(h c_0 / \left(n\lambda kT\right) - 1\right)\right]} \tag{2}$$

# **2.3. Evaporator finite difference method model**

It is assumed that the outside air is humid and its temperature does not change at the evaporator model. The evaporator plate is modeled as a flat plate located in a horizontal position, and by creating finite differences for our model, the energy input for each finite-difference step and the refrigerant enthalpy change at each step was calculated according to the following Equations 3 - 4.

$$dQ = dA (q_{Absorbed} - q_{Radiated} + q_{Natural Con.})$$
(3)

$$H_{j+1} = H_j + dH_j = H_j + \frac{dQ}{m_j}$$
(4)

# **2.4. Condenser finite difference method** model

In the condenser model, the finite difference model is mainly applied. Since the condenser is a phase-shifting heat exchanger, enthalpy steps are used as finite difference steps. By comparing the enthalpy values with the saturation zone gas and liquid enthalpies, the phase region we are in is found. Thus temperature profiles, pressure drop and heat transfer calculations are performed. Heat transfer for tube and enthalpy change step was calculated according to following Equations 5 - 6.

$$dq_{j} = U_{i-j} dA_{i-j} T_{0-i} - T_{i-j}$$
(5)

$$dH_j = \frac{dH_j}{m_j} and H_{j+1} = H_j - dH_j$$
(6)

# 2.5. Compressor and Expansion valve model

In the heat pump model designed have been referenced the Embraco NEU2168GK model (0.75 hp=0.56 kW=560 Watt), which can use R134a gas. The fluid enthalpy at the inlet and outlet of the expansion valve was accepted as constant and the following orifice Equation 7 specified in James and James (1987) was used in the modeling of the valve.

$$\dot{m} = 0.00683 x \sqrt{P_{cond} - P_{evap}} \tag{7}$$

## **2.6. Evaporative natural convection heat transfers**

The evaporator is designed basically like a flat plate. In addition to the energy coming from the sun to the evaporator plate, it is also being energy transfer from the air by natural convection and advection thus Nusslet correlations are used for heat flow in natural convection energy transfer. Natural convection energy transfer can be calculated with the following formula in Equation 8.

$$Q = h \left( T_s - T_{\infty} \right) W / m^2 \tag{8}$$

# **2.7. Thermodynamic and thermophysical properties of wet air properties**

In the numerical model, all thermodynamic properties are calculated using the Specific Helmholtz free energy of humid air at following Equation 9 by taking wet air as the real gas for the outside air [6].

$$f^{AV}(A,T,\rho) = (1-A)f^{V}(T,\rho^{V})$$
$$+ Af^{A}(T,\rho^{A}) + f^{mix}(A,T,\rho)$$
(9)

# 2.8. Thermodynamic properties of refrigerants

When modeling the evaporator and condenser, refrigerant

flows through the pipe. Therefore, we also need thermodynamic and thermophysical models of the refrigerant. For this modeling, the Helmholtz free energy dimensionless form equation is used as the standard ground state equation (The International Association for the Properties of Water and Steam-IAPWS) [7]. This Equation 10 for pure refrigerants:

$$\phi = \frac{A}{RT} = \phi_{id}\left(\rho, T\right) + \phi_r\left(\rho, T\right) \tag{10}$$

# 2.9. Single and double phase heat exchange formulas of refrigerants

To get the following Equation 11 boiling heat transfer coefficient  $(h_{rp})$  for R134a, the convective-boiling term  $(h_{cb})$ and the nucleate-boiling term  $(h_{nb})$  has used. These terms include a various parameters and correlations.

$$h_{tp} = \sqrt{h_{cb}^{2} + h_{nb}^{2}} \tag{11}$$

### 3. Results

#### 3.1. Solar Assisted Heat Pump Cycle Model

As shown in Figure 2 by creating a function graph of the atmospheric spectral energy density of solar rays in the wavelength range of 0.25 to 8 micrometers specified wavelength range, we have reached the value of 1353.9 W / m2  $\mu$ m from the cubic strip formulas. In JAVA, spectral emissivity  $\varepsilon$  ( $\lambda$ ) values of Nickel-plated copper selective surface were converted to function form with cubic strip interpolation algorithm.



It has been determined that the solar radiation was a change for Photovoltaic/Thermal-Solar Assisted Heat Pump (PV/T-SAHP) between 300 W/m<sup>2</sup> and 1000 W/m<sup>2</sup> [8]. In the study by doing the 2019 spectral analyze of solar energy intensity for the city of Izmir has been determined between 400 W/m<sup>2</sup> and 900 W/m<sup>2</sup>. According to spectral solar energy functions at Figure 3, it is striking that the amount of energy density per 1 m<sup>2</sup> evaporator plate is the lowest on December 21 and the highest on June 21.  $1m^2$  nickel-plated copper type plate used as

evaporator surface with the integration values of the cubic strip algorithm of spectral data; For the date of 21 December 2019, the amount of energy falling on the evaporator plate was 455.143 W/m<sup>2</sup>, the energy absorbed in the plate was 388.508 W/m<sup>2</sup> and the radiation emitted from the plate was obtained as 60.307 W/m<sup>2</sup>. On 21 June 2019 the energy amount falling on the evaporator plate was 852.095 W/m<sup>2</sup>, the energy absorbed in the plate is 727.344 W/m<sup>2</sup> and the radiation emitted from the plate is as 112.904 W/m<sup>2</sup>.



**Figure 3.**The annual graph of the spectral solar energy absorbed by the 1m<sup>2</sup> evaporator plate

#### 3.2. Solar-Boosted Evaporator Plate Model Results

21 December 2019 and 21 June 2019 were taken as reference for the heat energy required for the evaporator plate in the Java program data output. The amount of energy absorbed and reflected in the 2.40m<sup>2</sup> evaporator plate at the dates determined in the analysis is shown in Table 1.

1 in 2.40m2 Evaporator F	Plate of Two Differ-
21 December 2019	21 June 2019
787.682 Watt	1.474.656 Watt
	n in 2.40m2 Evaporator F 21 December 2019 787.682 Watt

### 3.3. Double Pipe Reverse Parallel Flow Condenser Model Results

The condenser thermal capacity is obtained according to this following Equation 12 and in Table 1, the sum of the solar energy obtained in the 2.40 m2 evaporator plate and the 560watt energy from compressor is shown in Table 2.

$$Q_{condenser} = W_{comp} + Q_{evaporator}$$
(12)

Table 2. The Heat from the Condenser at Different Dates				
Dates	21 December 2019	21 June 2019		
Heat From Condenser	1.347.682 Watt	2034.656 Watt		

In the finite difference model of the condenser, the heat transfer coefficient (U) term varies as a function of the mass velocity is changed at each step by using Equation 13 for the surface heat transfer flowing by heat transfer. In order to determine in which phase region the refrigerant is in the condenser model, the heat transfer rate Equations 5 within the pipe is compared with the enthalpy steps Equations 6.

#### $\Delta Qi = Ui(Thi, Tci, mh, mc, Dh, Dc, \varepsilon h, \varepsilon c) \Delta Ai[Thi - Tc] \quad (13)$

In JAVA, pressure and sudden contractions losses for flow in and out the pipe are neglected, the inlet temperature of the refrigerant was determined to be 52 ° C by using R134a and R404A gas as the refrigerant. Taking as reference the monthly average water temperatures of Izmir shown in Table 3. was set the temperature of the water entering the condensers, respectively 10 °C on 21 December 2019 and 20.5 °C on 21 June 2019. Thus, the surface area of the required condenser areas was calculated by making water ingresses at different temperatures.

Table 3. JAVA Condenser area calculation results.				
Dates	21 December 2019	21 June 2019		
$Q_{condenser}$	1353.156 Watt	2056.518 Watt		
<b>ṁ</b> R134a	0.01 kg/s	0.01 kg/s		
<i>ṁ</i> H,O	0.02 kg/s	0.02 kg/s		
T <sub>H2O inlet</sub>	10 °C	20.5 °C		
T <sub>R314a inlet</sub>	52 °C	52 °C		
T <sub>H2O outlet</sub>	12.38 °C	22.98 °C		
T <sub>R314Aoutlet</sub>	38.5 °C	38.6 °C		
Pipe Length (L)	I.7 m	2.1 m		
JAVA Required Conden- ser Area	0.1353 m <sup>2</sup>	0.2116 m <sup>2</sup>		

Since the amount of solar energy obtained from the evaporator plate in the SAHP system changes, the amounts of energy obtained in the condenser on December 21 and June 21 also changes. For this reason, different condenser areas are needed in SAHP, the analysis made with different condenser areas are shown in Figure 4 and Figure 5.

### 3.4. Solar Assisted Heat Pump Cycle Model

In the SAHP modeling at JAVA, the spectral energy amount falling on the 2.40m2 evaporator plate at the



Figure 4. JAVA data output with R134a refrigerant and water temperature change





best solar energy efficiency date 21 June 2019 was taken as a reference. In order to compare the efficiency of refrigerants with different properties, R134a and R404A refrigerants were tested separately in the SAHP system. All data obtained from the cycle regions in the SAHP are given in. In Table 4, when we compare the R134a and R404A COP condenser performance R134a is seen better than R404A.

### 4. Discussion and Conclusions

#### 4.1. Discussion

This is the first report of applying JAVA mathematical

#### Table 4. JAVA SAHP results.

Capture Output				
Ideal refrigeration cycles	R134a	R404A		
R134a and R404A Mass flow rate <i>ṁ</i>	0.01 kg/s	0.01 kg/s		
Water Mass flow rate $\dot{m}$	0.02 kg/s	0.02 kg/s		
Condenser heat output	2.043004805882 kW	1.960730401387 kW		
Evaporator heat input Compressor work	I.488364767200 kW 0.554640038681 kW	1.409654089724 kW 0.551076311663 kW		
İsentropic comp. work	0.4437120309452	0.4408610493305 kW		
COP evaporator	2.68347876712 kW	2.558001605022 kW		
COP condenser	3.683478767126 kW	3.558001605022 kW		
COP evaporator Carnot	3.346832204799 kW	3.37304054541 kW		
COP condenser Carnot	4.34683220479 kW	4.373040545417 kW		
P1 compressor input	200.0 kPa	200.0 kPa		
TI compressor input	-0.0758453309716 °C	-20.26999999999 °C		
h1 compressor input	401.1322780063 kJ/kg	360.7661939387 kJ/kg		
S1 compressor input	1.7651661475 kJ/kgK	1.6717379366 kJ/kgK		
XI compressor input	2.0 kgvapor/kgtotal	2.0 kgvapor/kgtotal		
P2 compressor output	1500.0 kPa	1500.0 kPa		
h2 compressor output	456.5962818745	415 873825105 kl/kg		
S2 compressor output	kJ/kg 1 7968802164 kI/kgK	1 7052363382 kl/kgK		
	1.2157 kgvapor/			
	kgtotal			
P3 condenser output	1500.0 kPa	1500.0 kPa		
h3 condenser output	k]/kg	219.8007849663 kJ/kg		
T3 condenser output	37.23278849288 °C	13.93186150339 °C		
S3 condenser output	1.1774949394 kJ/kgK	1.0696918934 kJ/kgK		
X3 condenser output	0.0 kgvapor/kgtotal	0.0 kgvapor/kgtotal		
P4 Expansion output	200.0 kPa 252.2958012863	200.0 kPa		
h4 Expansion output	kJ/kg	219.8007849663 kJ/kg		
T4 Expansion output	-10.07584533097 °C	-30.71847169730 °C		
S4 Expansion output	1.2000130532 kJ/kgK	1.08272783724 kJ/kgK		
X4 Expansion output	0.0 kgvapor/kgtotal	0.0 kgvapor/kgtotal		
ration	1500.0 kPa	1500.0 kPa		
h5 compressor input	425.2294878195 kJ/kg	378.7405040638 kJ/kg		
T5 condenser satu- ration	55.23278849288 °C	32.300832851 °C		
S5 condenser satu- ration	1.7048851689 kJ/kgK	1.59143720440 kJ/kgK		
X5 condenser satu- ration	0.0 kgvapor/kgtotal	0.0 kgvapor/kgtotal		
P6 condenser satu- ration	1500.0 kPa	1500.0 kPa		
h6 compressor input	279.83987206 kJ/kg	247.0748924 kJ/kg		
T6 condenser satu- ration	55.23278849288 °C	31.93186150339 °C		
S6 condenser satu- ration	1.2621492016 kJ/ kgK	1.1599026050 kJ/kgK		
X6 condenser satu- ration	0.0 kgvapor/kgtotal	0.0 kgvapor/kgtotal		

models to compare the refrigerant R134a and R404A gas in SAHP system the best of knowledge. The main purpose of the SAHP model is to help determine the basic parameters for a prototype to be manufactured. Different experimental models have been made for the SAHP system in different applications. However, there are not many studies on the SAHP system based on mathematical models.

The numerical model created under Kazakhstan climatic conditions is based on energy and mass balance. The numerical simulation was performed between -30 °C and 30 °C with solar intensities between 100 and 900 W/m<sup>2</sup>. The numerical simulation results showed that heat pump assisted re-generative solar still has more energy efficiency according to a conventional simple solar still [9]. In the study, four different solar assisted heat pump systems were simulated and the energy and financial status of the systems were evaluated. As a result of the analyzes, it was seen that the PV energy supported air source heat pump heating system was the most financially sustainable system with  $0.23 \notin / kWh$  electricity cost [10]. In the simulation, using R134a refrigerant in the PV assisted heat pump system, the solar radiation variation in the panel is between 300 w/m2 and 1000 w/m2. It was determined that the PV panel of the heat pump system was at a maximum of 35.68 °C at 14:00, and the average COP and COP values were obtained as 6.14 and 1.49, respectively [11]. In the city of Montreal, Canada, renewable source heat pump systems were installed in houses with an area of 210 m2, which were built in accordance with the energy-efficient detached house concept of the 1980s. Looking at the houses in general, it is seen that the (Air Sources Heat Pump-ASHP) system has the lowest lifetime cost and energy savings [12]. (Direct Expansion / Solar Assisted Heat Pump-DX/SAHP) system was studied experimentally under the meteorological condition of Qingdao located in the East China, and under the sunny and overcast day conditions in the autumn, the average COP was higher than 4.0 and 3.0, respectively. The average COP value of (DX/SAHP) system was seen higher than 2.5 even in extreme weather of the winter conditions [13].

Experimental or Numerical analyzes of heat pump systems are made in studies. However, generally the operating cost or investment cost of the heat pump systems were focused on. It is extremely important to develop efficiency-based projects in heat pump systems, and together with numerical analysis, it is seen that this is possible with a lower cost.

#### 4.2. Conclusions

Parameters to be carried out on the applicable SAHP prototype can be based on the data to be obtained with the JAVA program as in Figure 6. Thus, a faster and lower-cost development process can be created for the SAHP system. Under the data obtained from the studies conducted, it

is aimed to increase the thermal performance values of the systems by making improvements day by day in the disadvantageous applications in SAHP systems [14]. To analyze the researches on low-temperature heating applications of SAHP systems, basic performance data of SAHP systems were collected and various conventions of these data were compared [15]. All Equations in the SAHP cycle are programmed in JAVA in a computer environment and a typical output of the program is shown in Table 4. When the cycle data of R404A and R134a refrigerants are examined, the COP values of R404A and R134a are seen above 3.5 in Table 4. Since the COP condenser performance of the R134a refrigerant in the cycle is better in Table 4. R134a T-s diagram was created for SAHP at JAVA in Figure 6. In the analysis made in the T-s diagram, it is seen that the results obtained from all numerical models made with the algorithms created in the JAVA program are compared and the results are close and consistent with each other.



Figure 6. JAVA SAHP R134Aa T-s diagram

#### 5. Nomenclature

 $G_{\rm sc}$  Solar radiation constant

- $\theta_z$  Zenith angle
- n Day of the year
- $\mathcal{E}_{\lambda}$  Directional-spectral emissivity
- $\rho_{\lambda}$  Directional-spectral absorptivity
- $E_{\lambda h}$  Planck's laws distribution
- dQ Energy input for each finite-difference
- $H_{i+1}$  Refrigerant enthalpy changes at each step
- $dq_i$  Heat transfer for tube
- $dH_i$  Enthalpy change step for tube
- *m* Orifice Equation
- *Q* Natural convection energy transfer

- $f^{AV}$  Specific Helmholtz free energy of humid air
- $f^V$  Water properties of Specific Helmholtz free energy
- $f^A$  Dry air properties of Specific Helmholtz free energy
- $f^{mix}$  Air-water cross virial part properties of Specific Helmholtz free energy
- A Dry-air mass fraction
- *T* Absolute temperature
- ho Mass density
- *R* Specific gas constant
- $\phi$  Helmholtz free energy dimensionless form
- $\phi_{id}$  The ideal-gas part of the dimensionless Helmholtz free energy
- $\phi_r$  The residual part of the dimensionless Helmholtz free energy
- $h_{tn}$  Boiling heat transfer coefficient
- $h_{cb}$  Convective-boiling term
- $h_{nb}$  Nucleate-boiling term
- COP Coefficient of Performance

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