


Analytical Evaluation of Behavior of Composite Columns Under Axial Load

Serkan Etlı

Munzur University, Faculty of Engineering, Department of Civil Engineering, Tunceli, Turkey
serkanetli@munzur.edu.tr 

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Abstract

In the literature, various studies have been carried out for different nonlinear modeling strategies to model the response of such composite column members subjected to dynamic loads. In studies of concrete filled steel tubes elements with software using a finite element method such as ABAQUS, ANSYS and LS-DYNA, which have been used in the literature in recent years, it is seen that steel and concrete components are generally modeled separately with the help of plate, shell, or solid elements. To simulate the interaction between these element models, the help of some other connector or interface elements is needed. Therefore, the biggest disadvantage of using commercial packages is that very complex calculations arise by using much smaller parts of the element to be analytically modeled and the interaction structures to be produced between them. As a result, the necessity of computationally intensive and at the same time long-term work emerges. Within the scope of this study, it is aimed to calculate composite columns faster and more accurately as possible by using fiber section elements and standard material models under axial loading effects. It was observed that the selected parameters had a significant effect on the results obtained.

Keywords: Composite column, fiber section, material model

Eksenel Yük Altında Kompozit Kolonların Davranışının Analitik Değerlendirilmesi

Öz

Literatürde, dinamik yüklere maruz kalan bu tür kompozit kolon elemanlarının tepkisini modellemek için farklı doğrusal olmayan modelleme stratejileri için çeşitli çalışmalar yapılmıştır. Literatürde son yıllarda kullanılan ABAQUS, ANSYS ve LS-DYNA gibi bir sonlu elemanlar yöntemi kullanan yazılımlar ile beton dolgulu çelik tüp elemanlarına ait çalışmalarda, çelik ile beton bileşenlerin genellikle plaka, kabuk veya katı elemanların yardımı ile ayrı ayrı modellendikleri görülmektedir. Bu eleman modellerinin aralarındaki etkileşimi simüle etmek için bazı diğer bağlayıcı veya arayüz elemanlarının yardımına ihtiyaç duyulmaktadır. Dolayısıyla, ticari paketler kullanmanın en büyük dezavantajı, analitik olarak modellenecek elemana ait çok daha küçük parçalar kullanılarak ve bunlar arasında üretilecek olan etkileşim yapıları nedeniyle çok karmaşık hesaplamalar ortaya çıkmaktadır. Sonuç olarak hesaplama açısından yoğun ve aynı zaman uzun süreli çalışma gerekliliği ortaya çıkmaktadır. Bu çalışma kapsamında kompozit kolonların eksenel düşey etkiler altında fiber kesitli elemanlar ve standart malzeme modelleri kullanılarak daha hızlı ve mümkün olduğunca daha doğru hesaplanması hedeflenmiştir. Seçilen parametrelerin elde edilen sonuçlar üzerinde önemli derecede etkili olduğu gözlemlenmiştir.

Anahtar Kelimeler: Kompozit kolon, fiber kesit, malzeme modeli

INTRODUCTION

Concrete-filled steel column (CFST), which is reinforced by confinement effect with elements with steel tube sections and enhanced by utilizing the superior properties of concrete and steel, is normally used in concrete columns to meet the extra stresses that may occur due to structural effects. This technique can be used in the literature to increase the strength of an existing column in the structure, or it

can be produced as a new element in high-rise buildings with large spans or designed on a large scale. (Etlı & Güneyisi, 2020, 2021; Li et al., 2018; Matsui, 1986). The higher ductility, higher rigidity and higher strength provided by CFST elements are used in earthquake resistant structures of these structures or in the construction of bridge piers that are often exposed to impact and dynamic loads (Etlı

& Güneyisi, 2020, 2021; Lee et al., 2009; Shanmugam & Lakshmi, 2001).

Experimental studies have been carried out on the behavior of CFST elements with different cross-section properties and geometries, such as circular, rectangular, elliptical, and square sections, under pure axial and eccentric compression, tension, and torsional forces, recently studied with CFST elements (Han et al., 2006, 2011, 2014; Lee et al., 2009; Ou et al., 2011; Perea et al., 2013; Shanmugam & Lakshmi, 2001). Also, different codes (ACI (ACI 318-08, 2008), AISC (AISC, 2003) and EC4 (EN 1994-1-1, 2004)) included design provisions for CFST columns.

Many parameters affect the structural behavior of CFST elements, such as L/D and D/t ratios (L length, D core diameter and t wall thickness), material properties such as concrete strength and steel yield strength. Experimental evaluation of all these effects is not only expensive, but also very time-consuming. Therefore, in these elements, nonlinear finite element simulation approach may be the best solution to examine and account for all the effects mentioned (Liang & Fragomeni, 2009).

In the literature, various studies have been conducted for different nonlinear modeling strategies to model the response of such composite column elements subjected to dynamic loads. In the modeling of CFST elements with a finite element package such as ABAQUS, ANSYS and LS-DYNA, steel and concrete components are generally modeled separately using a plate, shell, or solid elements. Then, these element models are combined with some binder or interface elements to simulate the interaction between steel and concrete. (Ellobody & Young, 2006; Ge & Usami, 1994; Han et al., 2007; H.-T. Hu et al., 2003; H. T. Hu et al., 2005; Schneider, 1998; Thai & Kim, 2011; Ly et al., 2021; Asteris et al., 2021; Ayough et al., 2021). The main disadvantage of using commercial packages is that the structures become very complex due to very finely divided into smaller pieces and are therefore computationally intensive. In addition, it is difficult to properly and adequately model the composite behavior that occurs between steel and concrete, i.e. the interaction between concrete and steel materials, which is necessary to show interoperability limits (Thai & Kim, 2011). Many composite beam and column models with different cross-sections have been developed by researchers in the literature under different behavior models. Tomii and Sakino (Tomii

& Kenji, 1979) presented an analytical model for beams and columns produced as CFST with the help of elastic-plastic analysis. Considering the mentioned models and their experimental studies, detailed models for stress-strain developed by considering boundary effects for concrete confinement with steel pipe elements in CFST element are proposed. Hajjar et al. (Hajjar et al., 1998) proposed a model using a distributed plastic finite element based on fiber elements to perform nonlinear inelastic analysis of CFST beam columns.

In this study, CFST column elements were modeled in 3D with fiber section modeling technique and inelastic force-based frame element type elements were modeled in SeismoStruct (SeismoStruct, 2015) software. Some experimental studies under axial force in the literature were modeled using material models commonly used in the literature in element models, and the results obtained were examined comparatively.

MATERIAL AND METHODS

Within the scope of the study, the material models frequently found in the literature were used to evaluate the behavior of these elements quickly and reliably by making use of the square section column elements examined under axial force in the literature. While the Mander (Mander et al., 1988) concrete model was used for the concrete in the core parts of the CFST elements, square steel tubular elements were used in the outer parts. In these steel parts, the bilinear steel model and Ramberg-Osgood (Gadamchetty et al., 2016) steel material models, which are widely used in the literature, are used. The technical information and calculation techniques of the models used are presented in detail below.

Material models

The concrete model used in this study was developed by Martínez-Rueda and Elnashai (Martínez-Rueda & Elnashai, 1997), and a concrete model that considers the behavior of concrete under cyclic loads was used while the model was being obtained. This model is defined as “con_ma” within the SeismoStruct software. In this study, the confinement effect on CFST columns is provided by steel SHS (square hollow section) at the outermost part of the element. The confinement effect is defined by the k_c value in the selected concrete model of the SeismoStruct (Seismosoft, 2018) software. The confinement factor k_c is described as the ratio of the

compressive strength of the confined concrete model to the plain concrete strength. The confinement effect on the concrete cores of the CFST columns is provided by the steel SHS at the outermost part of the member. The k_c value obtained from the confinement effect calculations is reflected in the concrete model of the SeismoStruct (Seismosoft, 2018) software.

The calculation methods given by Sakino et al. (Sakino et al., 2004) were used in the calculations of the axial pressure load capacity. While obtaining the equation, it is assumed that the strength capacity of f_{cc} confined concrete, which is used in the calculation of the strength of the confined concrete, is calculated by Equation 1. In addition, the strength reduction factor was calculated with Equation 2 (Liang, 2009). In addition, the confinement coefficient given by k was considered as 4.1, as stated by Richart (Richart et al., 2005). On the other hand, f_{cr} confining stress (lateral pressure), γ_U (strength reduction factor for concrete), f_{cc} (strength of confined concrete), f_c' (concrete compressive strength), f_{sy} (yielding strength of steel) is given in Equation 3 (Sakino et al., 2004).

$$f_{cc} = \gamma_U \times f_c' + k \times f_{cr} \quad (1)$$

$$\gamma_U = 1.85 \times B_c^{-0.135} \quad 0.85 \leq \gamma_U \leq 1 \quad (2)$$

$$f_{cr} = \frac{2 \times t^2 \times (B - t) \times f_{sy}}{B_c^3} \quad (3)$$

The term B in the equation is the section width of SHS, while B_c refers to the section width of the concrete core, t is the thickness of section. In addition, the ε_{co} (strain at maximum stress of concrete) value calculated for plain concrete is calculated as given in Equation 4 (Sakino et al., 2004).

$$\varepsilon_{co} = 0.94 \times (0.85 \times f_c')^{0.25} \times 10^{-3} \quad 0.002 \leq \varepsilon_{co} \leq 0.0022 \quad (4)$$

For the structural steel forming the outer shell of the CFST element, two commonly used models, Bilinear steel model and Ramberg-Osgood steel model, were used. The strain-hardening modulus in

the Bilinear steel model was used as in Annex C EC3 (EN 1993-1-1, 2005), Kemp et al. (Kemp et al., 2002) and literature. In the Ramberg-Osgood steel model, the parameter n is calculated by Equation 5 and taken from literature.

$$n = \frac{\log(f_{su}) - \log(f_{sy})}{\log(\varepsilon_{su}) - \log(\varepsilon_{sy})} \quad (5)$$

It is suggested by EN 1993-1-5 (EN 1993-1-1, 2005), that the strain hardening coefficient (μ) is 0.01 in the approach of steel material behavior. On the other hand, Kemp et al. (Kemp et al., 2002) recommended that it be taken as 0.013. This value was taken as 0.005 and worked with structural analysis (Elghazouli et al., 2008). In the studies by Wang (2011), 0.013 remained very high (for steel elements), while the value of 0.01 converged, but still gave high results. In the context of the subject, it is important to examine the effect of concrete on this situation in composite elements.

As a result, strain hardening parameter is used in calculations as 0.005, 0.01, and 0.013 for Bilinear steel model, while in Ramberg-Osgood steel model, in addition to the value found by calculation, $n=20$ value, which is widely used in the literature, was used for examination purposes in the models.

While f_{sy} and ε_{sy} are the yield stress and elongation of the steel, respectively, f_{su} and ε_{su} are given as the ultimate stress and elongation of the steel, respectively. SeismoStruct software images of Mander concrete model, Bilinear steel model and Ramberg-Osgood steel models are given in Figure 1.

The column elements are modeled with the inelastic force-based frame element type. This is a force-based 3D beam-column element type that can model elements of space frames with geometric and material nonlinearities. In this element modeling technique, element sections are divided into fiber elements as given in Figure 2a. It also uses distributed elasticity elements as shown in Figure 2b during calculations. Distributed elasticity elements are widely used in earthquake engineering applications for both research and professional engineering purposes.

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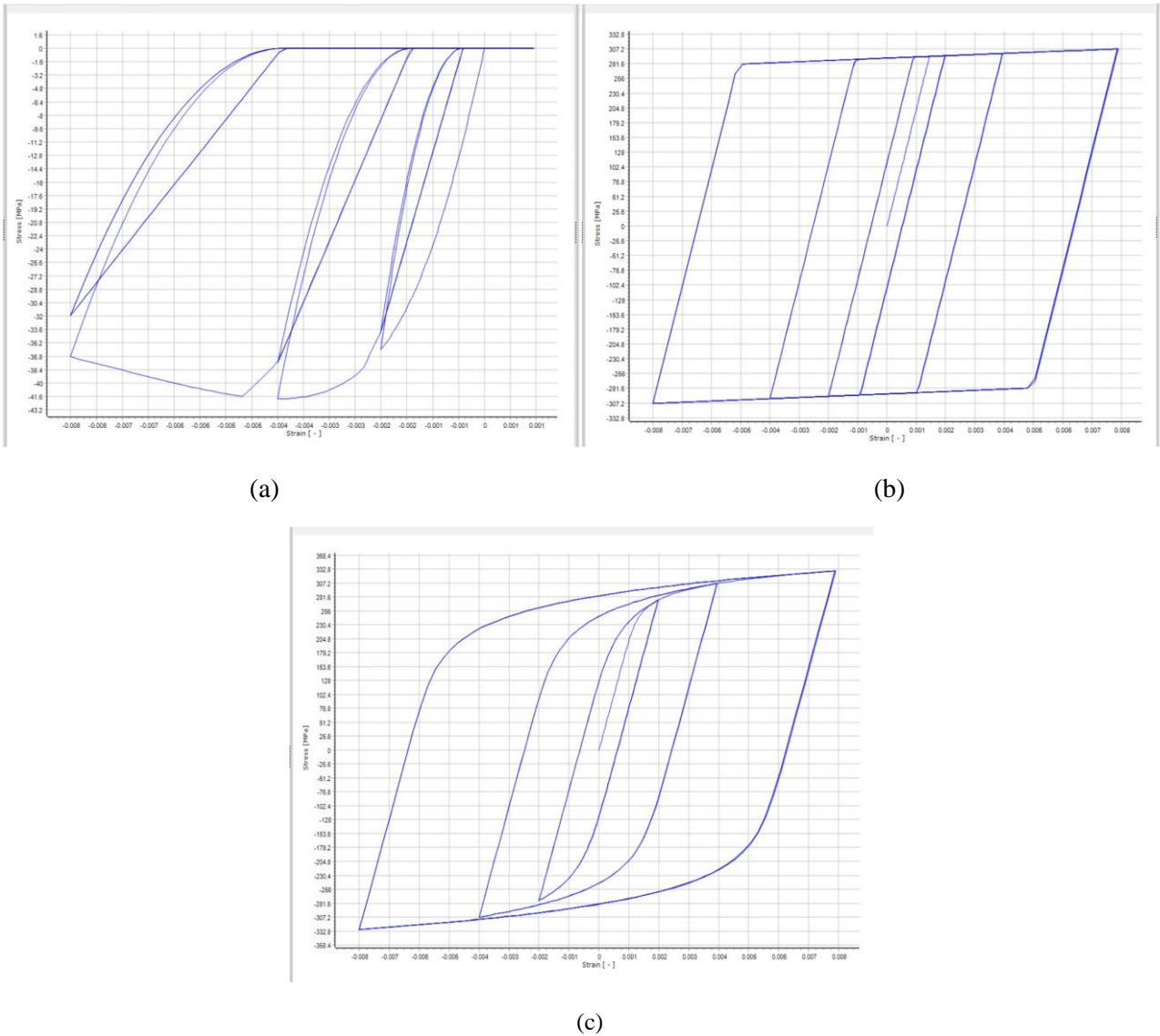


Figure 1. Material models view from SeismoStruct software a) Mander concrete model, b) Bilinear steel model and c) Ramberg-Osgood steel model

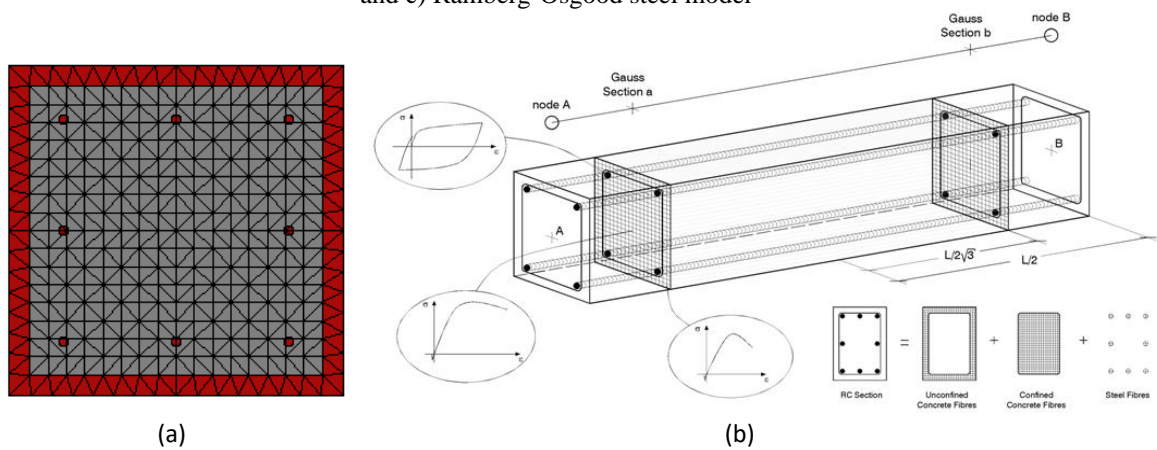


Figure 2. View from SeismoStruct software a) CFST column fiber section and b) Gauss sections

Table 1. Specimen properties

Specimen ID	References	f_{cd} (MPa)	f_{sy} (MPa)	E_s (MPa)	b (mm)	t (mm)	l (mm)	ν
4LN	(Tomii et al., 1977)	18.1	294.3	203067	150	4.3	450	0. 3
4MN		27.8	294.3	203067	150	4.3		
4HN		36.4	294.3	203067	150	4.3		
CR4-A-2	(Baba et al., 1995)	25.4	261.2	213000	148.4	4.38	500	
CR4-A-4		40.5	261.2	213000	148.4	4.38		
27	(Grauers, 1993)	33	379	200000	250	8	500	
S1	(Srinivasan & Schneider, 1999)	30.454	356	180518	127	3.15	609.6	
S2		26.044	357	190164	127	4.34		
S3		23.805	322	205322	127	4.55		
S4		23.805	312	203944	127	5.67		
S5		23.805	347	204633	127	7.47		
A1	(Ding et al., 2016)	35	257	206000	240	4	720	
I-A	(Tomii & Sakino, 1979)	32	194	210000	100	2.29	300	
II-A		21	339	218000	100	2.2		
III-A		21	288	210000	100	2.99		
IV-A		20	284	230000	100	4.25		
CR4-A-4-1	(Sakino & Ishibashi, 1985)	40.5	262	210000	148	4.38	323	
CR4-C-4-1		41.1	262	210000	215	4.38		
CR4-D-4-1		41.1	262	210000	323	4.38		

Within the scope of the study, the material and cross-sectional properties of the experimental studies taken from the literature are given in Table 1. In Table 1, concrete compressive strength, steel yield strength, and Poisson ratio are given, respectively, with the symbols f_c , f_{sy} , E_s and ν belonging to the experimental studies taken from the literature. In addition, section width, wall thickness and element heights are classified with b, t, and l symbols, respectively, in Table 1.

RESULTS AND DISCUSSION

The k_c , ϵ_{co} and n coefficients calculated from the data collected (Table 1) within the scope of the study. Using the data, the data obtained from the SeismoStruct software are presented on the graph together with the graphs obtained from the experimental results are given in Figure 3.

The results obtained by using the data obtained by the SeismoStruct software were mutually evaluated. A total of 5 graphs were calculated for each experimental element, with 3 strain hardening coefficient (μ) for Bilinear steel model and 2 n coefficients for Ramberg-Osgood. In addition, 3 coefficients were obtained during the comparisons.

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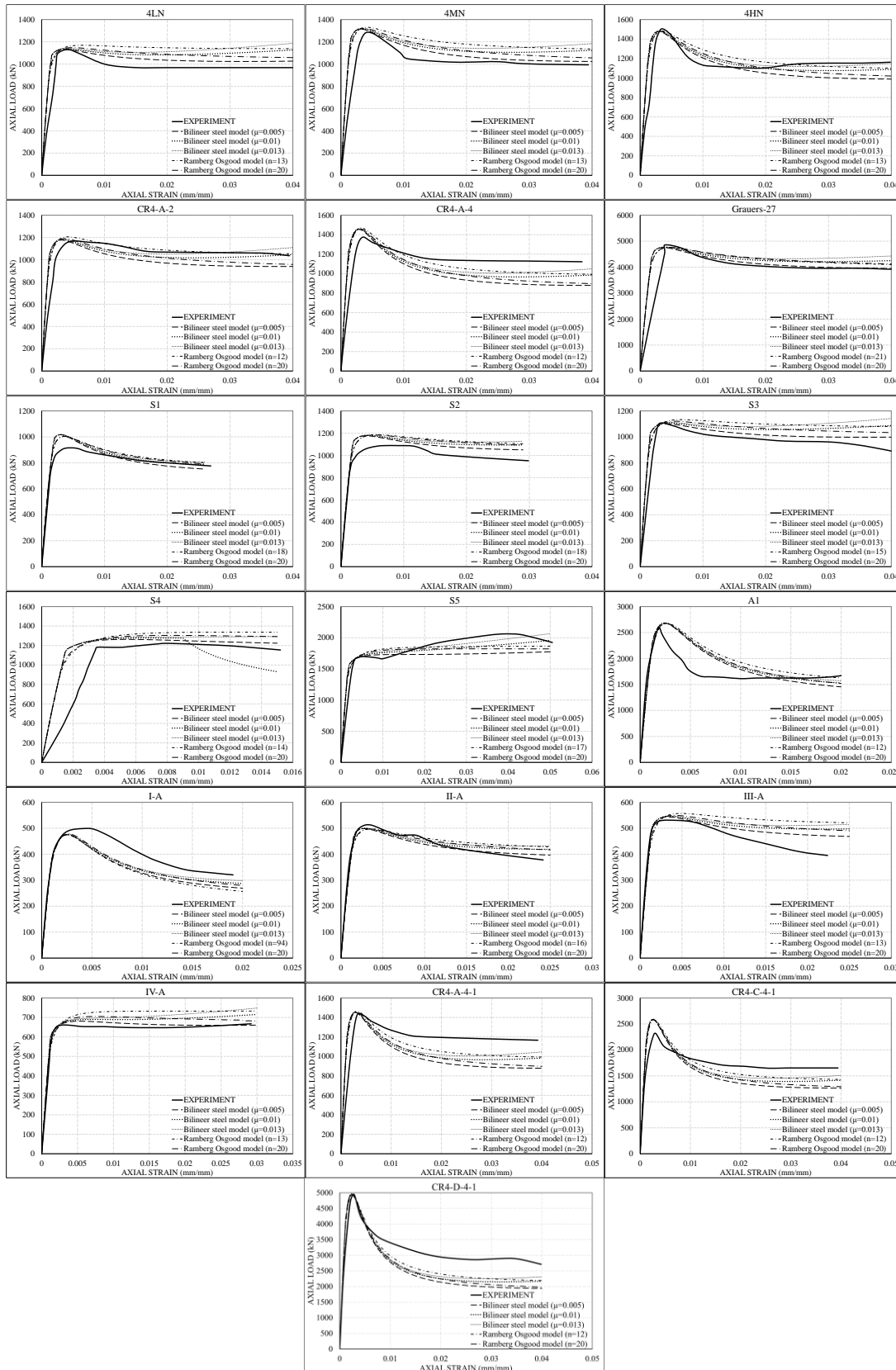


Figure 3. Axial displacement-load graph obtained from SeismoStruct software vs. experimental results

Table 2. $N_{ult,exp}/N_{ult,SeismoStruct}$ coefficients

Specimen ID	$N_{ult,exp}$ (kN)	$N_{ult,exp}/N_{ult,SeismoStruct}$				
		Bilinear steel model			Ramberg Osgood model	
		$\mu=0.005$	$\mu=0.01$	$\mu=0.013$	$n_{calculated}$	$n=20$
4LN	1128.570	0.997	0.993	0.951	0.966	0.984
4MN	1278.570	0.973	0.969	0.967	0.961	0.968
4HN	1504.760	1.019	1.016	1.015	1.015	1.018
CR4-A-2	1167.860	0.992	0.988	0.985	0.968	0.982
CR4-A-4	1375.300	0.945	0.942	0.941	0.936	0.942
27	4850.950	1.020	1.017	1.015	1.019	1.019
S1	912.338	0.898	0.896	0.895	0.909	0.909
S2	1088.260	0.925	0.922	0.920	0.917	0.919
S3	1103.880	1.002	0.996	0.967	0.974	0.985
S4	1222.730	0.968	0.957	0.946	0.914	0.937
S5	2061.690	1.161	1.054	0.998	1.105	1.131
A1	2596.840	0.969	0.967	0.966	0.970	0.970
I-A	498.708	1.050	1.047	1.045	1.051	1.042
II-A	512.432	1.028	1.025	1.024	1.030	1.031
III-A	530.081	0.975	0.970	0.968	0.952	0.964
IV-A	667.442	0.981	0.933	0.892	0.911	0.947
CR4-A-4-1	1432.870	0.987	0.984	0.983	0.978	0.984
CR4-C-4-1	2318.060	0.896	0.894	0.893	0.895	0.898
CR4-D-4-1	4944.470	0.996	0.995	0.994	1.000	0.999

Firstly, $N_{ult,exp}/N_{ult,SeismoStruct}$ are calculated (Table 2), while $N_{ult,exp}$ and $N_{ult,SeismoStruct}$ values represent the ultimate axial loading capacities obtained from experimental and SeismoStruct calculations, respectively. If the values of the $N_{ult,exp}/N_{ult,SeismoStruct}$ parameter are examined, in the analysis obtained, the strain hardening coefficient for the Bilinear steel model is 0.005, with more than 52% of the samples reaching the values closest to the experimental data, but the obtained values converge between 0.2-7.5%. In the models made with $n_{calculated}$ coefficients together with the Ramberg-Osgood model, only 10% gave the values closest to the experimental results. On the other hand, all the results obtained from theoretically converge to the experimental results between 0.04-16.1%. The highest diverge was obtained in the models made with $n_{calculated}$ coefficients together with the Ramberg-Osgood model for 42% of the elements (Table 2).

Secondly, $N_{exp}/N_{SeismoStruct}$ values were calculated (Table 3), as average of the ratio of experimental axial loading capacities (N_{exp}) to SeismoStruct experimental axial loading capacities ($N_{SeismoStruct}$) for each increasing strain value of 0.001. The $N_{exp}/N_{SeismoStruct}$ value acts as a kind of scaling factor. It can be considered as a scale of experimental

graphic values to the values obtained from theoretical calculations. Similar to the $N_{ult,exp}/N_{ult,SeismoStruct}$ parameter value, the highest convergence was observed in 52% of the elements when the μ value used in the Bilinear steel model was 0.005. These convergence values vary between 2-17%. On the other hand, when the $n_{calculated}$ parameter with Ramberg-Osgood is used, more than 63% of the theoretical modeling studies are among the most divergent values according to the experimental results, and this divergence rate is in the range of 6-22% (Table 3).

Finally, the $A_{exp}/A_{SeismoStruct}$ coefficient (Table 4) indicates the ratio between the area under the graph obtained experimentally (A_{exp}) and the area under the graph obtained theoretically from SeismoStruct ($A_{SeismoStruct}$). $A_{exp}/A_{SeismoStruct}$ value was evaluated as a second scaling coefficient within the scope of the study. It was evaluated as the ratio of the value of the area under the experimental axial displacement and load change graph to the value calculated as the graph area obtained from the theoretical calculations. Similar to the value of the $N_{exp}/N_{SeismoStruct}$ parameter, the highest convergence was observed in 52% of the elements when the μ value used in the Bilinear steel model was 0.005. These convergence values vary

between 1.5-16%. On the other hand, when the $n_{calculated}$ parameter with Ramberg-Osgood is used, more than 57% of the theoretical modeling studies are among the most divergent values according to the experimental results, and this divergence rate is in the range of 4-22%.

Table 3. $N_{exp}/N_{SeismoStruct}$ coefficients

Specimen ID	$N_{exp}/N_{SeismoStruct}$				
	Bilinear steel model			Ramberg Osgood model	
	$\mu=0.005$	$\mu=0.01$	$\mu=0.013$	$n_{calculated}$	$n=20$
4LN	0.920	0.879	0.856	0.846	0.886
4MN	0.908	0.868	0.847	0.836	0.875
4HN	1.026	0.978	0.953	0.942	0.988
CR4-A-2	1.037	0.984	0.956	0.942	1.002
CR4-A-4	1.094	1.035	1.004	0.990	1.056
27	0.951	0.913	0.892	0.918	0.914
S1	0.977	0.957	0.946	0.941	0.946
S2	0.919	0.902	0.889	0.887	0.893
S3	0.935	0.896	0.876	0.876	0.900
S4	0.852	0.916	0.829	0.810	0.825
S5	1.060	1.008	0.980	1.005	1.021
A1	0.943	0.923	0.911	0.886	0.917
I-A	1.093	1.065	1.048	1.111	1.062
II-A	0.958	0.936	0.924	0.915	0.928
III-A	0.826	0.807	0.796	0.776	0.800
IV-A	0.937	0.903	0.883	0.867	0.904
CR4-A-4-1	1.167	1.105	1.071	1.056	1.126
CR4-C-4-1	1.138	1.076	1.043	1.029	1.098
CR4-D-4-1	1.280	1.212	1.176	1.161	1.237

Table 4. $A_{exp}/A_{SeismoStruct}$ coefficients

Specimen ID	$A_{exp}/A_{SeismoStruct}$				
	Bilinear steel model			Ramberg Osgood model	
	$\mu=0.005$	$\mu=0.01$	$\mu=0.013$	$n_{calculated}$	$n=20$
4LN	0.933	0.892	0.869	0.858	0.899
4MN	0.925	0.886	0.864	0.854	0.893
4HN	1.036	0.993	0.968	0.957	1.001
CR4-A-2	1.054	1.002	0.973	0.961	1.020
CR4-A-4	1.100	1.046	1.016	1.004	1.065
27	0.966	0.929	0.908	0.934	0.930
S1	0.985	0.967	0.956	0.951	0.956
S2	0.929	0.911	0.899	0.897	0.903
S3	0.949	0.911	0.889	0.890	0.915
S4	0.887	0.939	0.865	0.848	0.863
S5	1.078	1.025	0.996	1.022	1.039
A1	0.929	0.912	0.903	0.879	0.906
I-A	1.115	1.088	1.072	1.132	1.085
II-A	0.976	0.953	0.939	0.930	0.944
III-A	0.841	0.818	0.805	0.784	0.812
IV-A	0.953	0.917	0.896	0.879	0.919
CR4-A-4-1	1.171	1.115	1.084	1.069	1.133
CR4-C-4-1	1.126	1.074	1.045	1.031	1.091
CR4-D-4-1	1.251	1.198	1.168	1.153	1.214

Experimental studies on some parameter changes in the sample, such as b/t changes, have been made on the effect of these parameters. In the analytical analysis methods used in the studies examined, if new models are proposed to affect this parameter on material models, the convergence is greater (Sakino et al., 2004). However, only the general material model is available in SeismoStruct. The aim of the study is to model the behavior of composite sections easily by the user using practical material models. For this reason, it can be observed that there are divergences between analytical results and experimental results in some models.

CONCLUSION

Experimental studies of CFST elements produced with SHS selected from the literature were re-examined using modeling techniques in SeismoStruct software. When the results of these material models and modeling technique, which are widely used in the literature, are examined comparatively within the scope of the study, the following conclusions are reached.

- When the μ value used in the Bilinear steel model is taken as 0.005, the best convergences are obtained for $N_{ult,exp}/N_{ult,SeismoStruct}$, $N_{exp}/N_{SeismoStruct}$ and $A_{exp}/A_{SeismoStruct}$ parameters in many modeled elements. This value is frequently used in theoretical and analytical analysis in the literature.
- For the $N_{ult,exp}/N_{ult,SeismoStruct}$ parameter, the change depends on the change in the μ and n parameters, but diverges up to 16%. In addition, when we look at the general results, this value has an average of 4-5% convergence for all.
- When the $N_{exp}/N_{SeismoStruct}$ parameter is examined, the closest values are obtained when the μ value used in the Bilinear steel model is taken as 0.005, while the most divergent values diverge up to 28% from the experimental data when the n value used in the Ramberg-Osgood steel model is taken as $n_{calculated}$. On the other hand, although there is an average of 8-10% error margin in μ and n values, a convergence between 0.2-2.5% is

observed, but a divergence range of 20-28% is also observed.

- Finally, when the $A_{exp}/A_{SeismoStruct}$ parameter is examined, the closest values are obtained when the μ value used in the Bilinear steel model is taken as 0.005. Similar to the $N_{exp}/N_{SeismoStruct}$ parameter, the most divergent values diverge up to 25% from the experimental data when the n value used in the Ramberg-Osgood steel model is taken as $n_{calculated}$. On the other hand, an average of 8-9.5% margin of error occurs in μ and n values. In addition, while a convergence of 0.05-1.6% is observed in the most converging models, a divergence range of 19-25% is observed in the models where the largest differences occur.

CONFLICT OF INTEREST

The Author report no conflict of interest relevant to this article

RESEARCH AND PUBLICATION ETHICS STATEMENT

The author declares that this study complies with research and publication ethics.

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