# APPLICATION OF KERNEL ESTIMATION METHOD FOR CORRECTION OF AGE DISTRIBUTION ERRORS IN CENSUS 

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#### Abstract

Age is continuous variable. Most of correction techniques assume that it is discrete variable. In this case, to correct age distribution censuses by which techniques have used it, continuous variable is very important. This study aims to discuss if the application of kernel estimation method to age distribution of data acquired in 2000 General Census can be utilized to make correction of misreported age declaration.


## INTRODUCTION

Age declarations acquired by censuses of population can be grouped into four categories as errors caused by the participant's missing age information, errors caused by inferential estimation of ages, errors during interviews, and errors during data processing stages. When literatures of Demography considered, it is observed that the methods such as Ariaga, Carrier-Farrag, Karup.King-Newton, United Nations, and Strong moving averages are applied to correct age distribution structure but they only result in minor corrections in the relevant age distribution structure. Furthermore, when the level of faulty age declarations is high, these methods cannot give any satisfactory results. In such cases, Strong moving averages method is generally appeared to be the most applied method. Thus, this study aims to discuss if it is possible to correct misreported age declarations by utilizing Kernel Estimation Method to data acquired in 2000 General Census.

## METHOD

One of the nonparametric estimation methods of Regression function is kernel estimation method (Wand and Jones, 1995). There are various methods for kernel estimation of Regression function and in this study Nadaraya-Watson kernel estimation method was used. It is assumed that independent x variable is random variable in Nadaraya-Watson kernel estimation method. This estimator is used in such conditions when both dependent and independent variables are random. Nadaraya-Watson estimator can be given as the following equation (Simonoff, 1996)

$$
\hat{m}_{N W}(x)=\frac{\sum_{i=1}^{n} Y_{i} W\left(\frac{x-X_{i}}{h}\right)}{\sum_{i=1}^{n} W\left(\frac{x-X_{i}}{h}\right)}
$$

where W is a kernel function satisfying $\int W(x) d x=1, h$ is a positive number, usually called the bandwidth or window width. $W$ kernel function can be assumed to be any function that bears the features of probability function. When $W$ kernel function is taken as a continuous function, it also maintains its features in kernel estimation. The selection of the relevant W kernel

[^0]estimation must be determined based on the features of time, calculation efficiency and derivativeness (Silverman, 1986). It is known that $W$ kernel functions do not create any significant changes on estimation whereas the bandwidth selection significantly affects the performance of kernel estimation in kernel estimations defined by the mean average which is obtained by means of utilizing weights from kernel estimation with centered observations. The selection of $h$ bandwidth in kernel estimation is very important. When $h$ is chosen to be a very low value, the estimation will be crudely made due to the fact that weighted average process applied to obtain kernel estimation in every point will be based on limited and less number of observations. This kind of estimation is called as less smoothed estimation. On the other hand, if the value of $h$ is too high, the achieved estimation value can be significantly deviated from its real value due to the fact that weighted average process will be based on observations in quite higher number. This kind of estimation is called as more smoothed estimation. The most appropriate value for $h$ bandwidth can be acquired by utilizing some error criteria. Rosenblatt (1956) states that additive mean of error squares which is widely used and easily monitored general criterion for the accuracy of density function's kernel estimator is preferred because of its mathematical easiness. The $h$ bandwidth that makes these criteria the lowest is taken as the most proper bandwidth. The most appropriate bandwidth value that makes the collected error squares mean the lowest is dependent on the second order derivative of unknown $f$ value. Many methods have been suggested to achieve $h$ bandwidth (Wand and Jones, 1995; Horova, and Zelinka, 2007). However, no method, being commonly accepted, is available yet in spite of most of the studies conducted so far. Some suggested methods are not welcomed very much because of their dependence of unknown density $f$ but considered significant to achieve initial values for some methods (Park and Marron, 1990). Each developed method has advantages and disadvantages compared to others (Cula, 1998).

When taking a mass with group number $K(i=1,2, \ldots, K)$ and $i$. observation number for group $n_{i}$, total observation number $n$, and relative frequency for each group, $\bar{p}_{i}=n_{i} / n$, where in $i / K$ co-spatial design $\bar{p}_{i}$ 's are reply values, the relative frequency estimators for regression function at each group could be achieved as follows similar to Nadaraya Watson kernel estimation (Simonoff, 1996)

$$
\hat{p}_{i}=\frac{\sum_{j=1}^{K} W\left(\frac{i / K-j / K}{h}\right) \bar{p}_{j}}{\sum_{j=1}^{K} W\left(\frac{i / K-j / K}{h}\right)} .
$$

In Eq.(2), $W$ is kernel function and $h$ is bandwidth.

## APPLICATION

Accurate age data in census, the ratios of each age group in $n$ total population can be converted to continuous probability distribution that the sum equals 1 . This function of distribution shows continuity. It defines the probability function that has wide distribution and the area under the curve Equals 1.

Firstly, the computer programs have been written to obtain the values of kernel estimates. The program has been coded by Delphi 3.0. The least squares cross-validation method has been used to obtain the bandwidth h .

In this study, considering the results of 2000 general census for various age groups, the
values of kernel were found.
Standard normal kernel function for $W$ kernel function was applied. Besides, least squares cross-validation method for finding $h$ bandwidth related to data were applied as well. It is found that separately proper $h$ bandwidth for the population data for male and female. $h$ bandwidth for female population is $0.048, h$ bandwidth for male population is 0.049 . The kernel estimation related to the data achieved by using Eq. (2) putting the estimator place achieved these bandwidths. The real estimation values are calculated by multiplying the achieved estimation values and populations for each age group. The difference between total age distributions achieved by kernel estimations and observed total age distribution equaled by multiplying correction coefficient achieved by the formula is given at Eq. (3). The formula of used correction coefficient (CC) is as follows that

$$
C C=\frac{O P}{E P}
$$

where $O P=$ Observed total population, $E P=$ Estimated total population.
The graphics of new odd age structures achieved by distributions of kernel estimations are shown in Figure 1 and Figure 2 separately for female and male.

On the other hand, the aim of convergence of initial estimations of both genders to the total population with the $h$ window widths has changed. Besides, the estimations achieved by the $h$ window width that gave the most approximate results have been discussed by evaluating the other age correction methods.

Figure 1. Kernel estimates and relative frequency of cell probability for male population


Figure 2. Kernel estimates and relative frequency of cell probability for female population


It is seen from the Figures 1 and 2 that the correction in accurate ages using $W$ kernel functions does not depend upon any assumption, 2000 census does not deviate from odd age distribution, and it presents this distribution as equable distribution.

Table 1 shows age distributions groups of 2000 general census by using other correction methods and age distributions groups corrected $W$ kernel functions in gender separation together. United Nation's age-gender correction index has applied all corrected age distributions (see Table 1). United Nation's age-gender correction index has also applied the achieved estimations for both genders by using values calculated least square cross-validation method from kernel estimations and age distributions by Eq. (3), the distributions achieved by changing $h$ window width to convergent to total observed population. Especially the two estimations that have changed $h$ window width and ensuring convergence to total observed population for male $h=0.0206$ and for female $h=0.0315$ window width has 13.7 high coefficient according to United Nation's age-gender correction index. This situation changed the age structure so it is decided to use estimated distribution with ideal $h$ window width.

The error index coefficients achieved by applying United Nation's age-gender correction index to 2000 census age as well as gender distribution derived by various methods are; for CarrierFarrag 11.3, for Ariaga 10.6, for K.King- Newton 10.6, for United Nations 10.8, for strong active mean 6.5, for the suggested achieved value in this study (Please see Appendices).

Table 1. Declared and corrected population according to age and gender (2000)


## DISCUSSION AND CONCLUSION

When Table 1 is examined, for $0-4$ age group estimated Arriaga and strong active mean method estimated less than declared population in this age group. Whereas in demographic literatures lack of ages, especially 0-4 age group and 5 included for wrong age declarations. Therefore, $0-4$ age group is less than expected value. Our correction method with $W$ kernel functions estimates 0-4 age group more than declared.

On the other hand, the mod age group for both genders occurred 15-19 age group in declared 2000 census, all correction methods except for United Nations age correction method resulted that mod age group has changed 10-14 age group to mod age group. Estimation conducted by $W$ kernel function resulted proper estimation of mod age group achieved by census.

Another important manner in here, being age group transitions between $0-14$ age both declared ages and Arriaga and strong active mean method, which are increasing amount of and leaped transitions between age groups up to mod group. On the other hand, in the corrections done by $W$ kernel function, it is estimated decreasing amount of smooth transitions. Therefore, it makes the trial method more acceptable than the other methods.

The biggest difference from the active mean method was considered through using age population and 10 years period of age group. In other words, taking $h$ bandwidth constant in active mean method was noticed. On the other hand, in W kernel function estimation method, $h$ bandwidth is changeable and the ratio of age population in total census was applied. In other words, probabilities were used. Accordingly, it gives opportunity to decide ideal $h$ bandwidth in the ratio of convergence to total population at the same time. As a matter of fact, in this study $h$ window width has changed for elimination the difference estimated total population and observed total population but at the end it is decided that the age distribution has been deteriorated by the result of applied United Nations age-gender correction index, which is higher, and this method has not been used. But it is impossible to say that the method shall increase error index continuously in different populations in distribution of age and gender.

The used five methods above in age correction brought out discussion of not to make sufficient correction in 10- year- age group, the used methods utilize various convergence probabilities for this age group. The changing $h$ window width using ability of kernel functions makes it possible to reach as many as approximate results in initial and final ages.

The estimated method suggested by Cula-Hoşgör with the comparison of five different age correction methods, as the result of applied United Nations age-sex accuracy index in age distributions grouped by genders. The error index coefficient 8.6 in Cula-Hoşgör method is lower than calculated error index coefficients in all methods except for strong active mean. Applying changing of age distribution mod group, it is assumed that the age variable is discontinuous variable in Strong active mean method as well as this unchanging mod group. Moreover, it is assumed that the age variable is continuous variable, which is an important advantage of the validity of method.

As a result, age is continuous variable that has unit time and divided into so small pieces. Many correction methods experienced and used by now have considered the age variable as discontinuous variable due to its structure and applying methods. But in this study, continuous age variable declaration errors were divided by $n$ number of kernel functions as its $h$ window width and the areas under the curve for each function and correction of $W$ kernel function estimation method, which is evaluating the weighted probabilities of other areas in total made. It seems that it is a proper method when continuous variable is corrected by the continuous function.

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## APPENDICES

## Appendix A: UNITED NATIONS AGE SEX ACCURACY INDEX; CARRIERFARRAG

| UNITED NATIONS AGE SEX ACCURACY INDEX; CARRİER-FARRAG |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | POPULATION |  | ANALYSIS OF SEX RATIO |  |  | ANALYSIS OF AGE RATIO |  |  |  |  |  |
|  | MALE | FEMALE | RATIO | SUC DIF | ABSUCDF | MALE | FEMALE | MALE | FEMALE | MALE | FEMALE |
|  |  |  |  |  |  | RATIO | RATIO | DF 100 | DF 100 | ABDF100 | ABDF100 |
| 10-14 | 3,665,036 | 3,432,924 | 106.76 | X | X | X | X | X | X | X | X |
| 15-19 | 3,599,491 | 3,395,545 | 106.01 | 0.8 | 0.8 | 102.6 | 102.0 | 2.6 | 2.0 | 2.6 | 2.0 |
| 20-24 | 3,351,566 | 3,223,518 | 103.97 | 2.0 | 2.0 | 100.7 | 101.4 | 0.7 | 1.4 | 0.7 | 1.4 |
| 25-29 | 3,053,916 | 2,960,744 | 103.15 | 0.8 | 0.8 | 101.5 | 101.9 | 1.5 | 1.9 | 1.5 | 1.9 |
| 30-34 | 2,667,439 | 2,590,216 | 102.98 | 0.2 | 0.2 | 98.9 | 99.0 | -1.1 | -1.0 | 1.1 | 1.0 |
| 35-39 | 2,340,338 | 2,269,453 | 103.12 | -0.1 | 0.1 | 98.7 | 99.3 | -1.3 | -0.7 | 1.3 | 0.7 |
| 40-44 | 2,074,445 | 1,982,123 | 104.66 | -1.5 | 1.5 | 102.2 | 100.8 | 2.2 | 0.8 | 2.2 | 0.8 |
| 45-49 | 1,721,228 | 1,662,295 | 103.55 | 1.1 | 1.1 | 101.7 | 101.1 | 1.7 | 1.1 | 1.7 | 1.1 |
| 50-54 | 1,309,027 | 1,306,325 | 100.21 | 3.3 | 3.3 | 94.0 | 94.7 | -6.0 | -5.3 | 6.0 | 5.3 |
| 55-59 | 1,064,485 | 1,097,579 | 96.98 | 3.2 | 3.2 | 94.4 | 94.8 | -5.6 | -5.2 | 5.6 | 5.2 |
| 60-64 | 945,565 | 1,009,738 | 93.64 | 3.3 | 3.3 | 106.3 | 106.1 | 6.3 | 6.1 | 6.3 | 6.1 |
| 65-69 | 714,219 | 806,476 | 88.56 | 5.1 | 5.1 | X | X | X | X | X | X |
| TOTAL |  |  |  |  | 21.4 |  |  |  |  | 29.0 | 25.5 |
| MEAN |  |  |  |  | 1.9 |  |  |  |  | 2.9 | 2.6 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| United nations age-sex accuracy index = |  |  |  |  | 11.3 |  |  |  |  |  |  |

## Appendix B: UNITED NATIONS AGE SEX ACCURACY INDEX; ARIAGA

| UNITED NATIONS AGE SEX ACCURACY INDEX; CARRİER-FARRAG |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | POPULATION |  | ANALYSIS OF SEX RATIO |  |  | ANALYSIS OF AGE RATIO |  |  |  |  |  |
|  | MALE | FEMALE | RATIO | SUC DIF | ABSUCDF | MALE | FEMALE | MALE | FEMALE | MALE | FEMALE |
|  |  |  |  |  |  | RATIO | RATIO | DF 100 | DF 100 | ABDF100 | ABDF100 |
| 10-14 | 3,688,035 | 3,452,611 | 106.82 | $\mathrm{x}$ | X | $\mathrm{x}$ | $\mathrm{x}$ | X | X | X | X |
| 15-19 | 3,576,492 | 3,375,858 | $105.94$ | $0.9$ | $0.9$ | $101.6$ | $101.0$ | 1.6 | $1.0$ | $1.6$ | $1.0$ |
| 20-24 | 3,355,010 | 3,229,356 | 103.89 | 2.1 | 2.1 | 101.3 | 102.0 | 1.3 | $2.0$ | $1.3$ | $2.0$ |
| 25-29 | 3,050,472 | 2,954,906 | 103.23 | 0.7 | $0.7$ | 101.4 | 101.6 | 1.4 | 1.6 | 1.4 | 1.6 |
| 30-34 | 2,663,135 | 2,586,297 | 102.97 | $0.3$ | $0.3$ | 98.7 | 98.9 | -1.3 | -1.1 | 1.3 | 1.1 |
| 35-39 | 2,344,642 | 2,273,372 | $103.13$ | $-0.2$ | $0.2$ | $99.1$ | 99.7 | -0.9 | -0.3 | 0.9 | 0.3 |
| 40-44 | 2,066,854 | 1,976,221 | $104.59$ | $-1.5$ | $1.5$ | $101.5$ | $100.3$ | $1.5$ | $0.3$ | $1.5$ | 0.3 |
| 45-49 | 1,728,819 | 1,,668,197 | 103.63 | 1.0 | 1.0 | 102.5 | 101.8 | 2.5 | 1.8 | 2.5 | 1.8 |
| 50-54 | 1,305,490 | 1,302,614 | 100.22 | 3.4 | 3.4 | $93.4$ | 94.1 | -6.6 | -5.9 | 6.6 | 5.9 |
| 55-59 | 1,068,022 | 1,101,290 | 96.98 | 3.2 | $3.2$ | $95.4$ | 95.6 | -4.6 | -4.4 | 4.6 | 4.4 |
| 60-64 | 933,563 | 1,002,425 | 93.13 | $3.8$ | $3.8$ | $104.1$ | 104.7 | 4.1 | 4.7 | 4.1 | 4.7 |
| 65-69 | 726,221 | 813,789 | 89.24 | 3.9 | 3.9 | $\mathrm{X}$ | X | X | X | X | X |
| TOTAL |  |  |  |  | 21.0 |  |  |  |  | 25.8 | 23.1 |
| MEAN |  |  |  |  | 1.9 |  |  |  |  | 2.6 | 2.3 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| United nations age-sex accuracy index $=$ |  |  |  |  | 10.6 |  |  |  |  |  |  |

## Appendix C: UNITED NATIONS AGE SEX ACCURACY INDEX; K.KINGNEWTON

| UNITED NATIONS AGE SEX ACCURACY INDEX; CARRİER-FARRAG |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | POPULATION |  | ANALYSIS OF SEX RATIO |  |  | ANALYSIS OF AGE RATIO |  |  |  |  |  |
|  | MALE | FEMALE | RATIO | SUC DIF | ABSUCDF | MALE | FEMALE | MALE | FEMALE | MALE | FEMALE |
|  |  |  |  |  |  | RATIO | RATIO | DF 100 | DF 100 | ABDF100 | ABDF100 |
| 10-14 | 3,662,230 | 3,431,537 | 106.72 | X | X | X | X | X | X | X | X |
| 15-19 | 3,602,297 | 3,396,932 | 106.05 | 0.7 | 0.7 | 102.8 | 102.2 | 2.8 | 2.2 | 2.8 | 2.2 |
| 20-24 | 3,343,788 | 3,215,181 | 104.00 | 2.0 | 2.0 | 100.4 | 101.0 | 0.4 | 1.0 | 0.4 | 1.0 |
| 25-29 | 3,061,694 | 2,969,081 | 103.12 | 0.9 | 0.9 | 101.9 | 102.3 | 1.9 | 2.3 | 1.9 | 2.3 |
| 30-34 | 2,667,002 | 2,588,575 | 103.03 | 0.1 | 0.1 | 98.7 | 98.8 | -1.3 | -1.2 | 1.3 | 1.2 |
| 35-39 | 2,340,775 | 2,271,094 | 103.07 | 0.0 | 0.0 | 99.0 | 99.5 | -1.0 | -0.5 | 1.0 | 0.5 |
| 40-44 | 2,062,478 | 1,975,694 | 104.39 | -1.3 | 1.3 | 101.3 | 100.3 | 1.3 | 0.3 | 1.3 | 0.3 |
| 45-49 | 1,733,195 | 1,668,724 | 103.86 | 0.5 | 0.5 | 102.5 | 101.4 | 2.5 | 1.4 | 2.5 | 1.4 |
| 50-54 | 1,320,249 | 1,316,215 | 100.31 | 3.6 | 3.6 | 94.8 | 95.5 | -5.2 | -4.5 | 5.2 | 4.5 |
| 55-59 | 1,053,263 | 1,087,689 | 96.83 | 3.5 | 3.5 | 93.6 | 94.0 | -6.4 | -6.0 | 6.4 | 6.0 |
| 60-64 | 929,949 | 997,211 | 93.25 | 3.6 | 3.6 | 104.3 | 104.6 | 4.3 | 4.6 | 4.3 | 4.6 |
| 65-69 | 729,835 | 819,003 | 89.11 | 4.1 | 4.1 | X | X | X | X | X | X |
| TOTAL |  |  |  |  | 20.3 |  |  |  |  | 27.1 | 24.0 |
| MEAN |  |  |  |  | 1.8 |  |  |  |  | 2.7 | 2.4 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| United nations age-sex accuracy index = |  |  |  |  | 10.6 |  |  |  |  |  |  |

## Appendix D: UNITED NATIONS AGE SEX ACCURACY INDEX; UNITED NATIONS

| UNITED NATIONS AGE SEX ACCURACY INDEX; CARRİER-FARRAG |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | POPULATION |  | ANALYSIS OF SEX RATIO |  |  | ANALYSIS OF AGE RATIO |  |  |  |  |  |
|  | MALE | FEMALE | RATIO | SUC DIF | ABSUCDF | MALE | FEMALE | MALE | FEMALE | MALE | FEMALE |
|  |  |  |  |  |  | RATIO | RATIO | DF 100 | DF 100 | ABDF100 | ABDF100 |
| 10-14 | 3,600,753 | 3,362,648 | 107.08 | $\mathrm{x}$ | X | $\mathrm{x}$ | X | X | X | X | X |
| 15-19 | 3,653,802 | 3,456,033 | 105.72 | $1.4$ | $1.4$ | $104.0$ | $103.9$ | 4.0 | $3.9$ | $4.0$ | $3.9$ |
| 20-24 | 3,427,170 | 3,289,652 | 104.18 | 1.5 | 1.5 | 103.4 | 103.8 | 3.4 | 3.8 | 3.4 | 3.8 |
| 25-29 | 2,972,074 | 2,885,439 | 103.00 | 1.2 | 1.2 | 98.5 | 99.0 | -1.5 | -1.0 | 1.5 | 1.0 |
| 30-34 | 2,609,295 | 2,538,494 | 102.79 | $0.2$ | 0.2 | 97.1 | 97.4 | -2.9 | -2.6 | 2.9 | 2.6 |
| 35-39 | 2,400,390 | 2,325,835 | 103.21 | $-0.4$ | $0.4$ | $101.9$ | $102.1$ | 1.9 | $2.1$ | 1.9 | $2.1$ |
| 40-44 | 2,099,760 | 2,017,485 | 104.08 | $-0.9$ | $0.9$ | $102.1$ | $101.3$ | 2.1 | $1.3$ | 2.1 | 1.3 |
| 45-49 | 1,712,964 | 1,658,154 | 103.31 | 0.8 | 0.8 | $99.4$ | 98.7 | -0.6 | -1.3 | 0.6 | 1.3 |
| 50-54 | 1,345,749 | 1,341,690 | 100.30 | 3.0 | 3.0 | 98.0 | 98.1 | -2.0 | -1.9 | 2.0 | 1.9 |
| 55-59 | 1,034,106 | 1,076,400 | 96.07 | $4.2$ | $4.2$ | $93.1$ | 93.9 | -6.9 | -6.1 | 6.9 | 6.1 |
| 60-64 | 876,148 | 950,644 | 92.16 | 3.9 | 3.9 | $97.5$ | 98.6 | -2.5 | -1.4 | 2.5 | 1.4 |
| 65-69 | 763,202 | 851,531 | 89.63 | 2.5 | 2.5 | X | X | X | X | X | X |
| TOTAL |  |  |  |  | 20.0 |  |  |  |  | 27.8 | 25.4 |
| MEAN |  |  |  |  | 1.8 |  |  |  |  | 2.8 | 2.5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| United nations age-sex accuracy index $=$ |  |  |  |  | 10.8 |  |  |  |  |  |  |

## Appendix E: UNITED NATIONS AGE SEX ACCURACY INDEX; MOVING AVERAGE

| UNITED NATIONS AGE SEX ACCURACY INDEX; CARRİER-FARRAG |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | POPULATION |  | ANALYSIS OF SEX RATIO |  |  | ANALYSIS OF AGE RATIO |  |  |  |  |  |
|  | MALE | FEMALE | RATIO | SUC DIF | ABSUCDF | MALE | FEMALE | MALE | FEMALE | MALE | FEMALE |
|  |  |  |  |  |  | RATIO | RATIO | DF 100 | DF 100 | ABDF100 | ABDF100 |
| 10-14 | 3,570,761 | 3,366,060 | 106.08 | X | X | X | X | X | X | X | X |
| 15-19 | 3,468,209 | 3,287,415 | 105.50 | 0.6 | 0.6 | 100.9 | 100.7 | 0.9 | 0.7 | 0.9 | 0.7 |
| 20-24 | 3,304,782 | 3,161,419 | 104.53 | 1.0 | 1.0 | 101.5 | 101.8 | 1.5 | 1.8 | 1.5 | 1.8 |
| 25-29 | 3,041,862 | 2,923,996 | 104.03 | 0.5 | 0.5 | 101.0 | 101.1 | 1.0 | 1.1 | 1.0 | 1.1 |
| 30-34 | 2,719,526 | 2,625,280 | 103.59 | 0.4 | 0.4 | 100.0 | 100.1 | 0.0 | 0.1 | 0.0 | 0.1 |
| 35-39 | 2,395,767 | 2,319,621 | 103.28 | 0.3 | 0.3 | 100.5 | 100.7 | 0.5 | 0.7 | 0.5 | 0.7 |
| 40-44 | 2,050,077 | 1,983,562 | 103.35 | -0.1 | 1.0 | 99.2 | 98.8 | -0.8 | -1.2 | 0.8 | 1.2 |
| 45-49 | 1,738,344 | 1,697,641 | 102.40 | 1.0 | 1.0 | 100.2 | 100.0 | 0.2 | 0.0 | 0.2 | 0.0 |
| 50-54 | 1,419,812 | 1,412,507 | 100.52 | 1.9 | 1.9 | 97.9 | 98.0 | -2.1 | -2.0 | 2.1 | 2.0 |
| 55-59 | 1,161,650 | 1,185,016 | 98.03 | 2.5 | 2.5 | 98.9 | 98.7 | -1.1 | -1.3 | 1.1 | 1.3 |
| 60-64 | 929,325 | 987,854 | 94.08 | 4.0 | 4.0 | 99.5 | 100.2 | -0.5 | 0.2 | 0.5 | 0.2 |
| 65-69 | 706,639 | 786,566 | 89.84 | 4.2 | 4.2 | X | X | X | X | X | X |
| TOTAL |  |  |  |  | 17.4 |  |  |  |  | 8.6 | 9.1 |
| MEAN |  |  |  |  | 1.6 |  |  |  |  | 0.9 | 0.9 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| United nations age-sex accuracy index = |  |  |  |  | 6.5 |  |  |  |  |  |  |

## Appendix F: UNITED NATIONS AGE SEX ACCURACY INDEX; CULA-HOŞGÖR

| UNITED NATIONS AGE SEX ACCURACY INDEX; CARRİER-FARRAG |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | POPULATION |  | ANALYSIS OF SEX RATIO |  |  | ANALYSIS OF AGE RATIO |  |  |  |  |  |
|  | MALE | FEMALE | RATIO | SUC DIF | ABSUCDF | MALE | FEMALE | MALE | FEMALE | MALE | FEMALE |
|  |  |  |  |  |  | RATIO | RATIO | DF 100 | DF 100 | ABDF100 | ABDF100 |
| 10-14 | 3,572,825 | 3,347,389 | 106.73 | X | X | X | X | X | X | X | X |
| 15-19 | 3,582,906 | 3,394,471 | 105.55 | 1.2 | 1.2 | 103.2 | 103.1 | 3.2 | 3.1 | 3.2 | 3.1 |
| 20-24 | 3,369,568 | 3,234,960 | 104.16 | 1.4 | 1.4 | 102.5 | 102.8 | 2.5 | 2.8 | 2.5 | 2.8 |
| 25-29 | 2,992,789 | 2,899,211 | 103.23 | 0.9 | 0.9 | 99.4 | 99.8 | -0.6 | -0.2 | 0.6 | 0.2 |
| 30-34 | 2,654,807 | 2,575,866 | 103.06 | 0.2 | 0.2 | 98.8 | 98.8 | -1.2 | -1.2 | 1.2 | 1.2 |
| 35-39 | 2,383,954 | 2,313,072 | 103.06 | 0.0 | 0.0 | 100.9 | 101.0 | 0.9 | 1.0 | 0.9 | 1.0 |
| 40-44 | 2,072,097 | 2,002,515 | 103.47 | -0.4 | 0.4 | 101.0 | 100.5 | 1.0 | 0.5 | 1.0 | 0.5 |
| 45-49 | 1,717,482 | 1,670,770 | 102.80 | 0.7 | 0.7 | 100.3 | 99.6 | 0.3 | -0.4 | 0.3 | 0.4 |
| 50-54 | 1,354,052 | 1,350,807 | 100.24 | 2.6 | 2.6 | 97.4 | 97.4 | -2.6 | -2.6 | 2.6 | 2.6 |
| 55-59 | 1,061,697 | 1,103,178 | 96.24 | 4.0 | 4.0 | 95.2 | 95.8 | -4.8 | -4.2 | 4.8 | 4.2 |
| 60-64 | 877,432 | 951,288 | 92.24 | 4.0 | 4.0 | 98.1 | 99.3 | -1.9 | -0.7 | 1.9 | 0.7 |
| 65-69 | 726,658 | 813,425 | 89.33 | 2.9 | 2.9 | X | X | X | X | X | X |
| TOTAL |  |  |  |  | 18.3 |  |  |  |  | 19.0 | 16.7 |
| MEAN |  |  |  |  | 1.7 |  |  |  |  | 1.9 | 1.7 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| United nations age-sex accuracy index = |  |  |  |  | 8.6 |  |  |  |  |  |  |

## ÖZET

## NÜFUS SAYIMLARINDAKİ YAŞ DAĞILIM HATALARININ DÜZELTİLMESİ İÇíN KERNEL TAHMİN YÖNTEMİNİN UYGULAMASI

Bu çalışmada, 2000 genel nüfus sayımındaki yaş verilerine, çekirdek kestirim yöntemi, uygulayıp hatalı yaş beyanlarının düzeltilmesinde bu yöntemin kullanılıp kullanılamayacağı tartışılmıştır. Bu amaçla çekirdek kestirim yöntemi ile düzeltilen yaş verilerine, literatürde belirtilen ve sıkça kullanılan Ariaga, Carrier-Farag, K.King-Newton, Birleşmiş Milletler, Hareketli ortalamalar, gibi yaş düzeltme teknikleri uygulanmış, 2000 nüfus sayımı verisi ile Birleşmiş Milletler Yaş -Cinsiyet hata indeksi kullanılarak karşlaştırılmıştır. Karşılaştırma sonucunda, uygulanan tekniğin stralamada hata indeksi yönünden en iyi ikinci sonucu verdiği görülmüştür. Bu nedenle çekirdek kestirim yöntemi, nüfus sayımlarındaki hatalı yaş dağılımlarını düzeltmek için uygun ve kabul edilebilir bir yöntem olduğu kanaati ile tartışmaya açılmış ve kullanıcılara yeni bir yöntem olarak sunulmuştur.


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