



### Determination of the Factors Effecting Lactation Milk Yield of Holstein Friesian Cows by the Path Analysis

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#### ABSTRACT

The objective of this study was made to determine the factors effecting lactation milk yield of Holstein Friesian cows by the path analysis in order to improving the milk production. Namely, this study was carried out to determine the direct and indirect relationships, and total effects between lactation milk yield (LMY; Y) and lactation length (LL; X<sub>1</sub>), average daily milk yield (DMY<sub>mean</sub>; X<sub>2</sub>), maximum daily milk yield (DMY<sub>max</sub>; X<sub>3</sub>), service period (SP; X<sub>4</sub>), first calving age (FCA; X<sub>5</sub>), gestation period (GP; X<sub>6</sub>) of 130 head of first lactating Holstein Friesian cows. When the direct determination coefficients of independent variables on dependent variable were analyzed via path analysis, it was determined that the lactation length (LL; X<sub>1</sub>) and average daily milk yield (DMY<sub>mean</sub>; X<sub>2</sub>) were found to be more effective than the other independent variables. The path coefficients which show the direct effects of each variables on estimated variable were calculated as 0.60846 for X<sub>1</sub>, 0.77329 for X<sub>2</sub>, 0.03832 for X<sub>3</sub>, 0.12079 for X<sub>4</sub>, 0.00051 for X<sub>5</sub> and -0.01672 for X<sub>6</sub> respectively, and the determination coefficient (R<sup>2</sup>) were found as 0.967. As a result, it was stated that the use of path analysis would be more appropriate in determining the factors effecting lactation milk yield.

#### 1. Introduction

There are a lot of factors affecting yield on livestock. Therefore it's important to understand which environmental factor affects yield to what extent or which way, to success of selection. One of the most important proverbial statistical measures among variables is the coefficient of correlation. But solitarily coefficient of correlation is not a criteria to state that there is a cause and effect relation among the variables. As too much functional relations occur among variables, path analyze used to determine if variables have either direct or indirect effect separately or together on results and to determine interaction among variables.

Path analyze is a method that used to determine relations among variables, to determine such directly or indirectly revealed that the total effect of independent variables on dependent variables (Alpar 2011). As another feature of the path analyze, it can reveal relations among variables with diagrams that proper to purpose. As this feature make easier to identify objective relations, it also provides understandable logical flow at results interpretation (Martin and Meek 1986). Namely, path coefficients can be also described as standardized partial regression coefficients (Düzgüneş and Akman 1995; Düzgüneş et al. 1996). If causal variables do not depend on each other, path coefficients going from causal variables to outcome variables is equal to the correlation coefficient between these variable and outcome variables (Karabacak et al. 2013).

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This research was made to determine the direct or indirect relations of lactation time, daily average milk yield, maximum milk yield, service period, first calving age, gestation time which effect on lactation milk yield in Holstein Friesian Cows by Path analyze.

**2. Materials and Methods**

**2.1. Materials**

130 Holstein Friesian cows which raised in a private farm located in Karapınar County of Konya province in Turkey were used as research material. First lactation data were used. Lactation milk yield, lactation period, daily average milk yield, maximum milk yield, service period, first calving age and gestation period were determined from records.

**2.2. Methods**

Primarily, correlation coefficient of lactation milk yield, lactation period, average daily milk yield, maximum milk yield, service period, first calving age and gestation period were calculated in research. Afterwards variables standardized with regression analyze. Because of the coefficients standardized, a constant was zero. Multiple regression coefficients of this equation denotes path coefficients videlicet every variables direct effects on result variable (Gürbüz *et al.* 1999). Hereby lactation milk yield modeled as dependent variable and path analyze carried out to determine direct or indirect effects of other six variables on this variable. In path analyze it was shown as Y: lactation milk yield (1), X<sub>1</sub>: lactation time (day), X<sub>2</sub>: daily average milk yield (1), X<sub>3</sub>: maximum daily milk yield (1), X<sub>4</sub>: service period (day), X<sub>5</sub>: first calving age (day) and X<sub>6</sub>: gestation period (day).

X<sub>1</sub>, X<sub>2</sub>, X<sub>3</sub>, X<sub>4</sub>, X<sub>5</sub> and X<sub>6</sub> are independent variables and Y is dependent variable in the path analyze diagram given in Figure 1. Path coefficient indicates the variation caused by each feature which effects one character's formation. According to the direction of the path coefficient from reason to result, the relation was shown with one way arrow in the diagram at Figure 1, but thereby it doesn't states reason result relation, the correlation coefficients were indicated with two way arrow.

While correlation coefficient changes among +1 and -1, path coefficients could get beyond these limits. Also negative and positive efficient ones of path coefficients equalize each other's and keep correlation coefficients within these limits (Orhan and Kaşıkçı 2002).

In Figure 1, direct effect of X<sub>1</sub> variable on Y feature was indicated with P<sub>YX1</sub>. Meanwhile effect of X<sub>1</sub> variable via X<sub>2</sub>, X<sub>3</sub>, X<sub>4</sub>, X<sub>5</sub> and X<sub>6</sub> variables to Y, become X<sub>1</sub> variables indirect effects on Y.

Correlation coefficients among the lactation milk yield, lactation length, daily average milk yield, maximum daily milk yield, service period, first calving age and gestation period could be split as below.

$$r_{YX1} = P_{YX1} + r_{12}P_{YX2} + r_{13}P_{YX3} + r_{14}P_{YX4} + r_{15}P_{YX5} + r_{16}P_{YX6}$$

$$\begin{aligned} r_{YX2} &= P_{YX2} + r_{12}P_{YX1} + r_{23}P_{YX3} + r_{24}P_{YX4} + r_{25}P_{YX5} + r_{26}P_{YX6} \\ r_{YX3} &= P_{YX3} + r_{13}P_{YX1} + r_{23}P_{YX2} + r_{34}P_{YX4} + r_{35}P_{YX5} + r_{36}P_{YX6} \\ r_{YX4} &= P_{YX4} + r_{14}P_{YX1} + r_{24}P_{YX2} + r_{34}P_{YX3} + r_{45}P_{YX5} + r_{56}P_{YX6} \\ r_{YX5} &= P_{YX5} + r_{15}P_{YX1} + r_{25}P_{YX2} + r_{35}P_{YX3} + r_{45}P_{YX4} + r_{56}P_{YX6} \\ r_{YX6} &= P_{YX6} + r_{16}P_{YX1} + r_{26}P_{YX2} + r_{36}P_{YX3} + r_{46}P_{YX4} + r_{56}P_{YX5} \end{aligned}$$

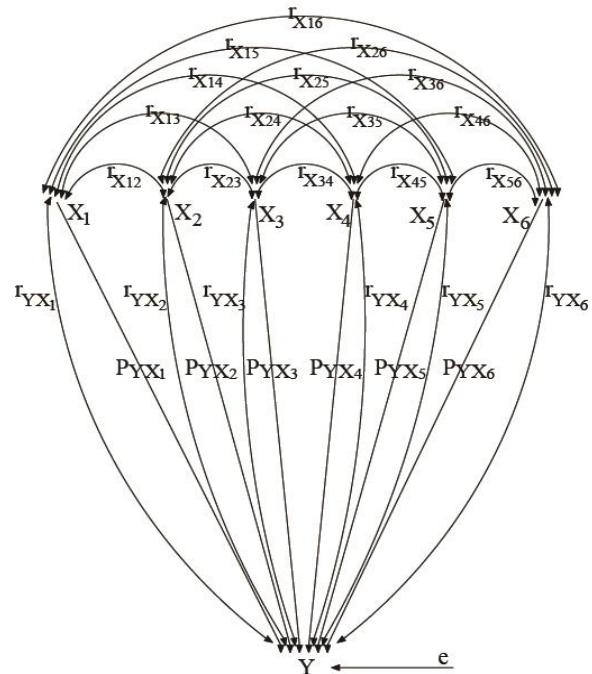


Figure 1  
Path diagram among independent and dependent variables

In equivalents they were indicated as P<sub>Y<sub>i</sub></sub>: Path coefficient among i<sup>th</sup> independent variable and Y dependent variable (direct effect), r<sub>ij</sub>P<sub>Y<sub>i</sub></sub>: Effect of i<sup>th</sup> independent variable via j<sup>th</sup> independent variable to Y variable (indirect effect), r<sub>Y<sub>i</sub></sub>: Correlation coefficient among Y and i<sup>th</sup> independent variables, r<sub>ij</sub>: Correlation coefficient among independent variables. Sum of direct and indirect effects indicates correlation coefficient among Y and X<sub>i</sub>.

These equivalents should be given with matrix notation as below;

$$\begin{pmatrix} P_{YX1} \\ P_{YX2} \\ P_{YX3} \\ P_{YX4} \\ P_{YX5} \\ P_{YX6} \end{pmatrix} = \begin{pmatrix} 1 & r_{12} & r_{13} & r_{14} & r_{15} & r_{16} \\ r_{21} & 1 & r_{23} & r_{24} & r_{25} & r_{26} \\ r_{31} & r_{32} & 1 & r_{34} & r_{35} & r_{36} \\ r_{41} & r_{42} & r_{43} & 1 & r_{45} & r_{46} \\ r_{51} & r_{52} & r_{53} & r_{54} & 1 & r_{56} \\ r_{61} & r_{62} & r_{63} & r_{64} & r_{65} & 1 \end{pmatrix}^{-1} \begin{pmatrix} r(X_1Y) \\ r(X_2Y) \\ r(X_3Y) \\ r(X_4Y) \\ r(X_5Y) \\ r(X_6Y) \end{pmatrix}$$

If we summarize this matrix equivalent as A = BC, when C matrix isolated, C = AB<sup>-1</sup> equivalent and path coefficients become estimated. A matrix which achieved

with multiplication of matrix belong to Correlation (B) and path (C) coefficients was a matrix that direct and indirect effects occur together (Sıralı and Kayaalp1995).

### 3. Results and Discussions

Definitive statistics belong to lactation milk yield, lactation length, average daily milk yield, maximum milk yield, service period, first calving age and gestation period which established with herd management program of Holstein Friesian Cows are given in Table 1.

According to Table 1, lactation milk yield was 6732.3 l, lactation length was 307.5 day, average daily milk yield was 22 l, maximum milk yield was 30.73 l, service period was 90.68 day, first calving age was 746.4 day and gestation time was determined as 276.7 day.

It was shown that determined lactation milk yield, lactation time and daily average milk yield data in this research were similar with enounced data of Holstein Friesian Cows (Orhan and Kaşıkçı 2002), but service period data of the research has lower values than published literature (Orhan and Kaşıkçı 2002).

Correlation coefficients among lactation milk yield, lactation length, average daily milk yield, maximum milk yield, service period, first calving age and gestation period of Holstein Friesian Cows were given in Table 2.

While statistically significant correlations were found among lactation milk yield and lactation length, average daily milk yield, maximum milk yield, service period ( $P < 0.01$ ) and with first calving age ( $P < 0.05$ ), statistically insignificant and low correlations determined

among lactation milk yield and gestation length ( $P > 0.05$ ).

Coefficients in standardized fractional regression equation was determined as  $LMY = 0.60846LL + 0.77329DMY_{mean} + 0.03832DMY_{max} + 0.12079SP + 0.00051FCA - 0.01672GP$ , and coefficient of determination ( $R^2$ ) was calculated as % 96.7. Hereby a invariant was became zero hence coefficient standardized. Effects of partial regression coefficients of the equation (path coefficients), which shows direct effects of coefficients on result variable related to lactation length, average daily milk yield and service period were determined as significant ( $P < 0.01$ ), but the effects of maximum milk yield, first calving age and gestation length were determined as insignificant.

Analyzed features of Holstein Friesian cows as direct effects, indirect effects, Path (P), correlations (r), coefficients of direct and simultaneous determination (CDD and CSD), effect percentages (%) were given in Table 3.

When the values that indicates direct determination coefficient of  $X_1, X_2, X_3, X_4, X_5$  and  $X_6$  independent variables which indicates Y feature were analyzed, it was shown that  $P^2_{YX1}$  and  $P^2_{YX2}$  makes the most addition. The research results indicate that the coefficients of direct determination were detected as similar with other published values about Holstein cows and Brown Swiss by Orhan and Kaşıkçı (2002). It was observed that the lactation milk yield was responded at low rate by maximum milk yield, service period, first calving age and gestation length.

Table 1

Definitive statistics belong to analyzed features of Holstein Friesian Cows

Variables	N	$\bar{X} \pm S_{\bar{X}}$	Min	Max
LMY (l)	130	6732.3±97.50	4507.2	9865.3
LL (day)	130	307.5±3.34	247.0	401.0
DMY <sub>mean</sub> (l)	130	22.00±0.26	16.13	29.62
DMY <sub>max</sub> (l)	130	30.73±0.39	20.00	43.00
SP (day)	130	90.68±2.89	32.00	175.00
FCA (day)	130	746.4±4.16	693.00	896.00
GP (day)	130	276.7±0.54	260.00	296.00

LMY: lactation milk yield, LL: lactation length, DMY<sub>mean</sub>: average daily milk yield, DMY<sub>max</sub>: maximum daily milk yield, SP: service period, FCA: first calving age, GP: gestation period

Table 2

Correlation coefficients among analyzed data of Holstein Friesian Cows

Features	LMY	LL	DMY <sub>mean</sub>	DMY <sub>max</sub>	SP	FCA
LL	0.567**					
DMY <sub>mean</sub>	0.689**	-0.174*				
DMY <sub>max</sub>	0.616**	-0.096	0.831**			
SP	0.548**	0.812**	-0.084	-0.045		
FCA	0.182*	0.208*	0.034	-0.028	0.250**	
GP	0.046	0.082	0.015	0.028	-0.002**	0.049

\*:  $P < 0.05$ ; \*\*:  $P < 0.01$

Table 3

Direct Effects, Indirect Effects, Path (P), Correlations (r), Coefficients of Direct and Simultaneous Determination (CDD and CSD), Effect Percentages (%) belonging to traits

Direct Effect	Indirect Effect	P	r ( $r_{XaXb}$ )	CDD ( $P^2_{YXn}$ )	CSD ( $2.r_{XaXb}. P_{YXa}. P_{YXb}$ )	EP (%)
X <sub>1</sub>		0.60846		0.37022		71.889
	X <sub>2</sub>	-0.13464	-0.174*		-0.1637396	15.908
	X <sub>3</sub>	-0.00369	-0.096		-0.0044767	0.436
	X <sub>4</sub>	0.09811	0.812**		0.1193573	11.592
	X <sub>5</sub>	0.00011	0.208*		0.0001291	0.013
	X <sub>6</sub>	0.00138	0.082		-0.0016684	0.163
X <sub>2</sub>		0.77329		0.59798		83.915
	X <sub>1</sub>	-0.10595				11.497
	X <sub>3</sub>	0.03183	0.831**		0.0492492	3.454
	X <sub>4</sub>	-0.01017	-0.084		-0.0156922	1.104
	X <sub>5</sub>	0.00002	0.034		0.0000268	0.002
X <sub>3</sub>		0.03832		0.00015		5.142
	X <sub>1</sub>	-0.05869				7.875
	X <sub>2</sub>	0.64232				86.185
	X <sub>4</sub>	-0.00547	-0.045		-4.17 x10 <sup>-4</sup>	0.734
	X <sub>5</sub>	-0.00001	-0.028		-0.0000011	0.001
X <sub>4</sub>		0.12079		0.01459		17.710
	X <sub>1</sub>	0.49422				72.460
	X <sub>2</sub>	-0.06514				9.550
	X <sub>3</sub>	-0.00174				0.255
	X <sub>5</sub>	0.00013	0.250**		3.08x10 <sup>-5</sup>	0.019
X <sub>5</sub>		0.00004	-0.002		0.0000081	0.006
	X <sub>1</sub>	0.00051		2.6x10 <sup>-7</sup>		0.275
	X <sub>2</sub>	0.12647				68.108
	X <sub>3</sub>	0.02663				14.341
	X <sub>4</sub>	-0.00106				0.571
X <sub>6</sub>		0.03021				16.269
	X <sub>1</sub>	-0.00081	0.049		-8.36x10 <sup>-7</sup>	0.436
	X <sub>2</sub>	-0.01672		2.8x10 <sup>-4</sup>		20.861
	X <sub>3</sub>	0.05015				62.570
	X <sub>4</sub>	0.01191				14.860
X <sub>6</sub>		0.00107				1.335
	X <sub>1</sub>	-0.00027				0.337
	X <sub>2</sub>	0.00003				0.037
	X <sub>3</sub>					
	X <sub>5</sub>					

P: Path Coefficient, r: Correlations ( $r_{XaXb}$ ), CDD: Coefficient of Direct Determination ( $P^2_{YXn}$ ), CSD: Coefficient of Simultaneous Determination ( $2.r_{XaXb}. P_{YXa}. P_{YXb}$ ), EP: Effect Percentages, n-a-b: X<sub>1</sub>, X<sub>2</sub>, ..., X<sub>6</sub>

There are indirect ways ( $r_{YX1} = P_{YX1} + r_{12}P_{YX2} + r_{13}P_{YX3} + r_{14}P_{YX4} + r_{15}P_{YX5} + r_{16}P_{YX6}$ ) which cross over X<sub>2</sub>, X<sub>3</sub>, X<sub>4</sub>, X<sub>5</sub> and X<sub>6</sub>, except path coefficient among X<sub>1</sub> factor and Y feature and they are called as coefficient of associate determining (Table 3). Similarly there are other ways cross over X<sub>n</sub> among other X factors (X<sub>2</sub>, X<sub>3</sub>, X<sub>4</sub>, X<sub>5</sub> and X<sub>6</sub>) and Y feature except  $P_{YXn}$  path coefficient ( $r_{YX2} = P_{YX2} + r_{12}P_{YX1} + r_{23}P_{YX3} + r_{24}P_{YX4} + r_{25}P_{YX5} + r_{26}P_{YX6}$ ,  $r_{YX3} = P_{YX3} + r_{13}P_{YX1} + r_{23}P_{YX2} + r_{34}P_{YX4} + r_{35}P_{YX5} + r_{36}P_{YX6}$ ,  $r_{YX4} = P_{YX4} + r_{14}P_{YX1} + r_{24}P_{YX2} + r_{34}P_{YX3} + r_{45}P_{YX5} + r_{56}P_{YX6}$ ,  $r_{YX5} = P_{YX5} + r_{15}P_{YX1} + r_{25}P_{YX2} + r_{35}P_{YX3} + r_{45}P_{YX4} + r_{56}P_{YX6}$ ,  $r_{YX6} = P_{YX6} + r_{16}P_{YX1} +$

$r_{26}P_{YX2} + r_{36}P_{YX3} + r_{46}P_{YX4} + r_{56}P_{YX5}$ ). It was detected that coefficient of simultaneous determination has broadly lower values.

#### 4. Conclusions

When the values of the independent variables are examined, it is seen that lactation length and average daily milk yield are more effective than maximum milk yield, service period, first calving age, and gestation length which shows direct determination coefficients of lactation milk yield.

Relationship between cause variable which is undertaken as independent variable and effect variable which is undertaken as dependent variable can be analyzed in details according to elements of the relationship in path analysis. So that, when cause and effect relations are interpreted, not only direct effects but also indirect effects can be seen.

In short, the most important part of the path analysis is the creation of path diagram. It is important to reveal the relationship between direct and indirect variables. If relations are regulated wrong, these leads to incorrect results such as  $R^2 > 1$  or  $R^2 < 0$ . Therefore, path analysis is been convenient to detect the factors effecting lactation milk yield to see its both direct and indirect effects.

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