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Research Article

## Detemination of The Best Method (HF, MP2 and B3LYP) in Calculation of Chemical Hardness

Zinet Zaim, Tuba Alagöz Sayın, Koray Sayın<sup>1</sup>, Duran Karakaş

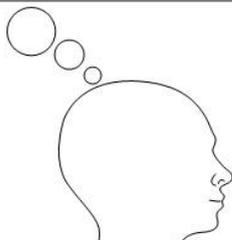
Chemistry Department, Faculty of Science, Sivas Cumhuriyet University, 58140 Sivas, Turkey

**Abstract:** Chemical hardness of 62 molecules are calculated at different 18 levels. No imaginary frequency is observed in optimization results for each level. Correlation between experimental and calculated hardness values are investigated. To analyze this investigation, correlation coefficient and scale factor are calculated for each level. As a results, HF method is better in calculation of chemical hardness and molecular orbital energy than B3LYP and MP2 methods.

**Keywords:** Molecular Orbital Energy, Chemical Hardness, HF, B3LYP, MP2

### Graphical Abstract

There are a lot paper in literature about chemical hardness. Researcher mainly used B3LYP and HF method in their study. Generally researchers use the energy of frontier molecular orbital. BUT which is the best method in calculation of chemical hardness? HF, MP2 or B3LYP...



- Investigations of the best method in calculation of chemical hardness were performed.
- Some organic and inorganic molecules were optimized at different level.
- Calculated and Experimental chemical hardness values were compared with each other.
- It was found that HF method is the best in calculation of chemical hardness.

### 1. Introduction

Chemical hardness is hot topic in chemistry and there are a lot of published papers over it [1-9]. Story of chemical hardness started in the hands of Pearson [10]. According to his opinions hard acids have low polarizability due to the stable electron distributions while soft acids have opposite properties [11]. Pearson's hard acid/base and soft acid/base principle imply that "hard acids or bases prefer to coordinate to hard bases or acids". This

principle is very practical in chemistry field. However, definition of hardness or softness is incomplete in hard-soft-acid-base (HSAB) principle. These troubles were solved in 1983 by Pearson and Parr. According to Pearson study, absolute hardness have been introduced as in Eq. (1) [12, 13].

$$\eta = \frac{(I-A)}{2} \quad (1)$$

<sup>1</sup> Corresponding Author

e-mail: krysayin@gmail.com and ksayin@cumhuriyet.edu.tr

where  $I$  and  $A$  are ionization potential and electron affinity of any chemical species (atom, ions, molecule or radical). These parameters is useful in determination of behaviors of chemical species. Ionization potential and electron affinity can be calculated by using Eq. (2) and (3).

$$I = E_{N-1} - E_N \quad (2)$$

$$A = E_N - E_{N+1} \quad (3)$$

where  $E_{N+1}$ ,  $E_N$  and  $E_{N-1}$  are total energy of system with (N+1), (N) and (N-1) electron, respectively. In addition to these equations, many researchers have being used the Koopmans theorem, recently. According to this theorem, ionization potential and electron affinity can be calculated from frontier molecular orbital , HOMO and LUMO, and their mathematical definations are given in Eq. (4) and (5).

$$I = -E_{HOMO} \quad (4)$$

$$A = -E_{LUMO} \quad (5)$$

One of the other hardness type is optical hardness ( $\eta_o$ ) and can be easily calculated by using Eq. (6).

$$\eta_o = E_{LUMO} - E_{HOMO} \quad (6)$$

This hardness is related to polarizabilities of chemical species and can be used in investigation of optical properties of related chemical species. According to hardness equations, energies of frontier molecular orbitals are important to calculation of hardness.

As for the quantum chemical calculations, some quantum chemical descriptors have been calculated by using the energy of frontier molecular orbitals [14-21]. These parameters have been used in determination of reactivity of molecules towards enzyme, protein and metal surface etc. Additionally, some theoretical formulas are derived by using some quantum chemical descriptors in quantitive structure-activity relationship (QSAR) studies. Because of that, calculation of these parameters is important to correct results. Generally, DFT methods have been used in calculation of these parameters.

Recently, computational chemistry has been fashion in academic invstigations. In this study, performance of HF, B3LYP and MP2 methods in calculation of chemical hardness is investigated in detail. Experimental hardness values of 62 molecules are optimized. In calculations, HF, B3LYP and MP2 methods are used. In addition to mentioned methods, 6-31++G(d,p), 6-311G, LANL2DZ, LANL2MB, SDD and SDDALL basis sets are used. Corelations between experimental and calculated results are examined by plotting distribution graphs and correlation coefficient are founds for each graph.

## 2. Computational Details

Computational processes of were performed by using GaussView 5.0.8 [22], Gaussian 09 AML64-G09 Revision-D01 programs [23], Gaussian 09 IA32W-G09 Revision-A02 programs [24]. Firstly, geometries of investigated compounds were optimized by using universal force field (UFF) method which is one of the molecular mechanics methods. After that, the geometries of mentioned complexes reoptimized at HF, B3LYP and MP2 methods with 6-31++G(d,p), 6-311G, LANL2DZ, LANL2MB, SDD and SDDALL basis sets. The vibrational frequency analyses indicate that optimized structures of relevant molecules are at stationary points corresponding to local minima without imaginary frequencies. Chemical hardness of these molecules are calculated by using Eq. (1).

## 3. Results and discussion

### 3.1. Chemical Hardness in HF Method

The fully optimizations of related molecules are done at each basis set in vacuum. Experimental hardness values ( $\eta$ ) of investigated molecules are given in Table 1 [25]. Chemical hardness value of mentioned molecules are calculated at 6-31++G(d,p), 6-311G and LANL2DZ basis sets and given in Table 2 – 4, respectively. As for the other basis sets, Calculated results in LANL2MB, SDD and SDDALL basis sets are given in Supp. Table S1 – S3, respectively.

**Table 1.** Studied molecules and their experimental hardness values

Molecule	$\eta^a$	Molecule	$\eta^a$	Molecule	$\eta^a$	Molecule	$\eta^a$
SF <sub>6</sub>	7.40	BBr <sub>3</sub>	4.85	C <sub>5</sub> H <sub>5</sub> N	5.00	cyclohexene	5.50
BF <sub>3</sub>	9.70	PBr <sub>3</sub>	4.20	butadiene	4.90	DMF	5.80
SO <sub>3</sub>	5.50	S <sub>2</sub>	3.85	H <sub>2</sub> S	6.20	C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub>	4.40
Cl <sub>2</sub>	4.60	C <sub>6</sub> H <sub>5</sub> NO <sub>2</sub>	4.40	C <sub>2</sub> H <sub>2</sub>	7.00	CH <sub>3</sub> CH=C(CH <sub>3</sub> ) <sub>2</sub>	5.50
H <sub>2</sub>	8.70	PCl <sub>3</sub>	4.70	HCONH <sub>2</sub>	6.20	CH <sub>3</sub> F	9.40
SO <sub>2</sub>	5.60	N <sub>2</sub> O	7.60	styrene	4.36	H <sub>2</sub> O	9.50
N <sub>2</sub>	8.90	acrylonitrile	5.56	CH <sub>3</sub> COCH <sub>3</sub>	5.60	(CH <sub>3</sub> ) <sub>3</sub> As	5.70
Br <sub>2</sub>	4.00	CS <sub>2</sub>	5.56	PH <sub>3</sub>	6.00	(CH <sub>3</sub> ) <sub>3</sub> P	5.90
O <sub>2</sub>	5.90	CO <sub>2</sub>	8.80	C <sub>6</sub> H <sub>6</sub>	5.30	(CH <sub>3</sub> ) <sub>2</sub> S	6.00
CO	7.90	HF	11.00	toluene	5.00	NH <sub>3</sub>	8.20
BCl <sub>3</sub>	5.64	HCl	8.00	propylene	5.90	CH <sub>4</sub>	10.3
CS	5.23	CH <sub>3</sub> CN	7.50	C <sub>6</sub> H <sub>5</sub> OH	4.80	C(CH <sub>3</sub> ) <sub>4</sub>	8.30
HNO <sub>3</sub>	5.23	CH <sub>2</sub> O	6.20	C <sub>6</sub> H <sub>5</sub> SH	4.60	(CH <sub>3</sub> ) <sub>2</sub> O	8.00
CH <sub>3</sub> NO <sub>2</sub>	5.34	HCO <sub>2</sub> CH <sub>3</sub>	6.40	CH <sub>3</sub> Cl	7.50	(CH <sub>3</sub> ) <sub>3</sub> N	6.30
PF <sub>3</sub>	6.70	CH <sub>3</sub> CHO	5.70	p-xylene	4.80	-	-
HCN	8.00	C <sub>2</sub> H <sub>4</sub>	6.20	1,2,5-trimethylbenzene	4.72	-	-

<sup>a</sup> Experimental values are taken from *Ref.* 25.

**Table 2.** Calculated chemical hardness values of mentioned molecules at HF/6-31++G(d,p) level in vacuum

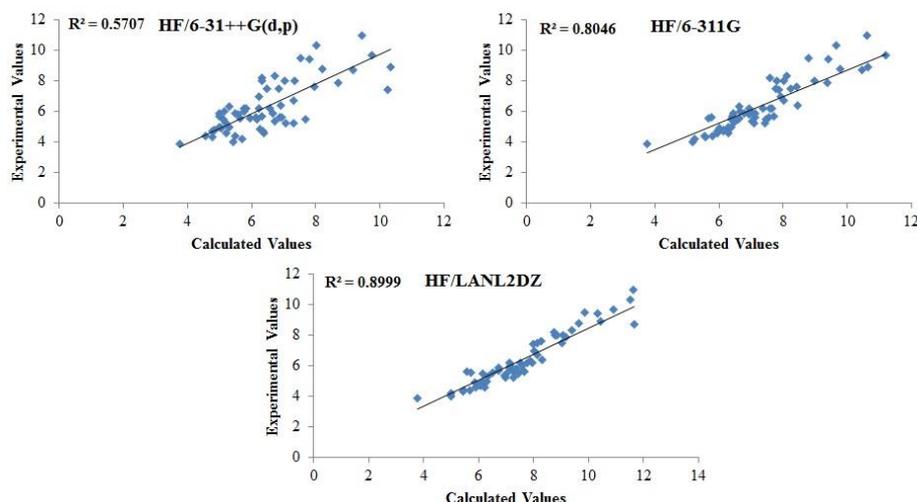
Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$
SF <sub>6</sub>	10.251	BBr <sub>3</sub>	6.275	C <sub>5</sub> H <sub>5</sub> N	5.294	cyclohexene	6.174
BF <sub>3</sub>	9.742	PBr <sub>3</sub>	5.705	butadiene	5.047	DMF	5.592
SO <sub>3</sub>	7.669	S <sub>2</sub>	3.769	H <sub>2</sub> S	5.782	C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub>	4.558
Cl <sub>2</sub>	6.380	C <sub>6</sub> H <sub>5</sub> NO <sub>2</sub>	5.485	C <sub>2</sub> H <sub>2</sub>	6.222	CH <sub>3</sub> CH=C(CH <sub>3</sub> ) <sub>2</sub>	5.110
H <sub>2</sub>	9.156	PCl <sub>3</sub>	6.359	HCONH <sub>2</sub>	6.242	CH <sub>3</sub> F	7.792
SO <sub>2</sub>	6.864	N <sub>2</sub> O	7.945	styrene	4.771	H <sub>2</sub> O	7.515
N <sub>2</sub>	10.341	acrylonitrile	5.938	CH <sub>3</sub> COCH <sub>3</sub>	6.124	(CH <sub>3</sub> ) <sub>3</sub> As	4.987
Br <sub>2</sub>	5.444	CS <sub>2</sub>	5.639	PH <sub>3</sub>	5.770	(CH <sub>3</sub> ) <sub>3</sub> P	5.002
O <sub>2</sub>	6.651	CO <sub>2</sub>	8.223	C <sub>6</sub> H <sub>6</sub>	5.169	(CH <sub>3</sub> ) <sub>2</sub> S	5.151
CO	8.695	HF	9.457	toluene	4.982	NH <sub>3</sub>	6.330
BCl <sub>3</sub>	6.927	HCl	7.032	propylene	5.503	CH <sub>4</sub>	8.028
CS	7.065	CH <sub>3</sub> CN	6.834	C <sub>6</sub> H <sub>5</sub> OH	4.839	C(CH <sub>3</sub> ) <sub>4</sub>	6.721
HNO <sub>3</sub>	7.304	CH <sub>2</sub> O	6.575	C <sub>6</sub> H <sub>5</sub> SH	5.228	(CH <sub>3</sub> ) <sub>2</sub> O	6.310
CH <sub>3</sub> NO <sub>2</sub>	6.736	HCO <sub>2</sub> CH <sub>3</sub>	6.911	CH <sub>3</sub> Cl	6.471	(CH <sub>3</sub> ) <sub>3</sub> N	5.319
PF <sub>3</sub>	7.327	CH <sub>3</sub> CHO	6.327	p-xylene	4.838	-	-
HCN	7.341	C <sub>2</sub> H <sub>4</sub>	5.824	1,2,5-trimethylbenzene	4.773	-	-

**Table 3.** Calculated chemical hardness values of mentioned molecules at HF/6-311G level in vacuum

Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$
SF <sub>6</sub>	7.864	BBr <sub>3</sub>	6.248	C <sub>5</sub> H <sub>5</sub> N	6.398	cyclohexene	7.459
BF <sub>3</sub>	11.193	PBr <sub>3</sub>	5.229	butadiene	6.016	DMF	6.945
SO <sub>3</sub>	6.374	S <sub>2</sub>	3.774	H <sub>2</sub> S	6.947	C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub>	5.806
Cl <sub>2</sub>	5.954	C <sub>6</sub> H <sub>5</sub> NO <sub>2</sub>	5.548	C <sub>2</sub> H <sub>2</sub>	7.943	CH <sub>3</sub> CH=C(CH <sub>3</sub> ) <sub>2</sub>	6.591
H <sub>2</sub>	10.458	PCl <sub>3</sub>	5.968	HCONH <sub>2</sub>	7.602	CH <sub>3</sub> F	9.399
SO <sub>2</sub>	5.769	N <sub>2</sub> O	8.424	styrene	5.568	H <sub>2</sub> O	8.796
N <sub>2</sub>	10.647	acrylonitrile	6.648	CH <sub>3</sub> COCH <sub>3</sub>	7.550	(CH <sub>3</sub> ) <sub>3</sub> As	6.405
Br <sub>2</sub>	5.193	CS <sub>2</sub>	5.680	PH <sub>3</sub>	6.979	(CH <sub>3</sub> ) <sub>3</sub> P	6.449
O <sub>2</sub>	6.783	CO <sub>2</sub>	9.769	C <sub>6</sub> H <sub>6</sub>	6.467	(CH <sub>3</sub> ) <sub>2</sub> S	6.648
CO	9.383	HF	10.628	toluene	6.292	NH <sub>3</sub>	7.591
BCl <sub>3</sub>	7.139	HCl	8.017	propylene	7.121	CH <sub>4</sub>	9.646
CS	7.083	CH <sub>3</sub> CN	8.243	C <sub>6</sub> H <sub>5</sub> OH	6.134	C(CH <sub>3</sub> ) <sub>4</sub>	8.117
HNO <sub>3</sub>	7.441	CH <sub>2</sub> O	7.660	C <sub>6</sub> H <sub>5</sub> SH	6.298	(CH <sub>3</sub> ) <sub>2</sub> O	7.802
CH <sub>3</sub> NO <sub>2</sub>	7.033	HCO <sub>2</sub> CH <sub>3</sub>	8.462	CH <sub>3</sub> Cl	7.771	(CH <sub>3</sub> ) <sub>3</sub> N	6.646
PF <sub>3</sub>	8.028	CH <sub>3</sub> CHO	7.719	p-xylene	6.140	-	-
HCN	8.967	C <sub>2</sub> H <sub>4</sub>	7.359	1,2,5-trimethylbenzene	6.143	-	-

**Table 4.** Calculated chemical hardness values of mentioned molecules at HF/LANL2DZ level in vacuum

Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$
SF <sub>6</sub>	7.980	BBr <sub>3</sub>	6.242	C <sub>5</sub> H <sub>5</sub> N	6.288	cyclohexene	7.459
BF <sub>3</sub>	10.906	PBr <sub>3</sub>	4.986	butadiene	5.869	DMF	7.381
SO <sub>3</sub>	6.150	S <sub>2</sub>	3.765	H <sub>2</sub> S	7.766	C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub>	5.691
Cl <sub>2</sub>	5.892	C <sub>6</sub> H <sub>5</sub> NO <sub>2</sub>	5.460	C <sub>2</sub> H <sub>2</sub>	8.036	CH <sub>3</sub> CH=C(CH <sub>3</sub> ) <sub>2</sub>	7.023
H <sub>2</sub>	11.680	PCl <sub>3</sub>	6.070	HCONH <sub>2</sub>	7.951	CH <sub>3</sub> F	10.320
SO <sub>2</sub>	5.568	N <sub>2</sub> O	8.279	styrene	5.422	H <sub>2</sub> O	9.869
N <sub>2</sub>	10.425	acrylonitrile	6.508	CH <sub>3</sub> COCH <sub>3</sub>	7.672	(CH <sub>3</sub> ) <sub>3</sub> As	6.738
Br <sub>2</sub>	5.008	CS <sub>2</sub>	5.727	PH <sub>3</sub>	7.578	(CH <sub>3</sub> ) <sub>3</sub> P	7.134
O <sub>2</sub>	6.735	CO <sub>2</sub>	9.644	C <sub>6</sub> H <sub>6</sub>	6.338	(CH <sub>3</sub> ) <sub>2</sub> S	7.147
CO	9.164	HF	11.635	toluene	6.166	NH <sub>3</sub>	8.748
BCl <sub>3</sub>	7.265	HCl	8.784	propylene	7.121	CH <sub>4</sub>	11.504
CS	6.997	CH <sub>3</sub> CN	9.051	C <sub>6</sub> H <sub>5</sub> OH	6.022	C(CH <sub>3</sub> ) <sub>4</sub>	9.389
HNO <sub>3</sub>	7.268	CH <sub>2</sub> O	7.523	C <sub>6</sub> H <sub>5</sub> SH	6.237	(CH <sub>3</sub> ) <sub>2</sub> O	8.851
CH <sub>3</sub> NO <sub>2</sub>	6.942	HCO <sub>2</sub> CH <sub>3</sub>	8.314	CH <sub>3</sub> Cl	8.143	(CH <sub>3</sub> ) <sub>3</sub> N	7.876
PF <sub>3</sub>	8.140	CH <sub>3</sub> CHO	7.626	p-xylene	6.029	-	-
HCN	9.082	C <sub>2</sub> H <sub>4</sub>	7.117	1,2,5-trimethylbenzene	6.054	-	-



**Fig. 1.** Distribution graphs between experimental and calculated values at HF/6-31++G(d,p), HF/6-311G and HF/LANL2DZ levels in vacuum.

**Table 5.** Calculated chemical hardness values of mentioned molecules at B3LYP/6-31++G(d,p) level in vacuum

Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$
SF <sub>6</sub>	2.190	BBr <sub>3</sub>	2.973	C <sub>5</sub> H <sub>5</sub> N	3.186	cyclohexene	1.192
BF <sub>3</sub>	5.337	PBr <sub>3</sub>	1.856	butadiene	3.239	DMF	3.520
SO <sub>3</sub>	1.618	S <sub>2</sub>	0.435	H <sub>2</sub> S	4.940	C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub>	3.131
Cl <sub>2</sub>	1.711	C <sub>6</sub> H <sub>5</sub> NO <sub>2</sub>	2.180	C <sub>2</sub> H <sub>2</sub>	5.532	CH <sub>3</sub> CH=C(CH <sub>3</sub> ) <sub>2</sub>	4.130
H <sub>2</sub>	11.664	PCl <sub>3</sub>	2.232	HCONH <sub>2</sub>	3.409	CH <sub>3</sub> F	6.671
SO <sub>2</sub>	1.405	N <sub>2</sub> O	3.502	styrene	3.006	H <sub>2</sub> O	6.127
N <sub>2</sub>	4.913	acrylonitrile	3.562	CH <sub>3</sub> COCH <sub>3</sub>	3.041	(CH <sub>3</sub> ) <sub>3</sub> As	4.309
Br <sub>2</sub>	1.446	CS <sub>2</sub>	2.726	PH <sub>3</sub>	5.412	(CH <sub>3</sub> ) <sub>3</sub> P	4.566
O <sub>2</sub>	0.894	CO <sub>2</sub>	4.591	C <sub>6</sub> H <sub>6</sub>	3.828	(CH <sub>3</sub> ) <sub>2</sub> S	4.076
CO	4.606	HF	6.500	toluene	3.719	NH <sub>3</sub>	6.996
BCl <sub>3</sub>	3.369	HCl	5.486	propylene	4.529	CH <sub>4</sub>	11.090
CS	2.981	CH <sub>3</sub> CN	5.405	C <sub>6</sub> H <sub>5</sub> OH	3.179	C(CH <sub>3</sub> ) <sub>4</sub>	8.519
HNO <sub>3</sub>	3.255	CH <sub>2</sub> O	3.008	C <sub>6</sub> H <sub>5</sub> SH	3.690	(CH <sub>3</sub> ) <sub>2</sub> O	5.701
CH <sub>3</sub> NO <sub>2</sub>	2.441	HCO <sub>2</sub> CH <sub>3</sub>	3.510	CH <sub>3</sub> Cl	4.431	(CH <sub>3</sub> ) <sub>3</sub> N	5.931
PF <sub>3</sub>	3.388	CH <sub>3</sub> CHO	3.042	p-xylene	3.620	-	-
HCN	5.581	C <sub>2</sub> H <sub>4</sub>	4.529	1,2,5-trimethylbenzene	3.593	-	-

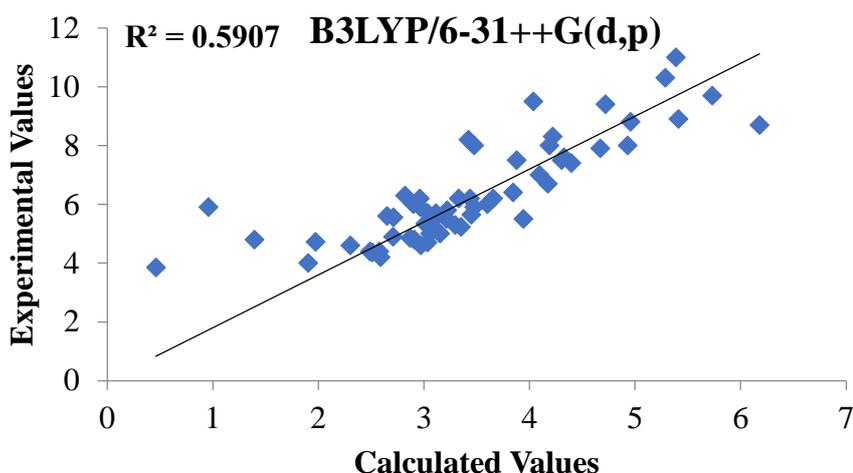
According to HF results, calculated chemical hardness values are mainly in agreement with experimental results except results in HF/6-31++G(d,p) and HF/LANL2MB levels. In these levels, there are big deviations in results.

### 3.2. Chemical Hardness in B3LYP Method

The fully optimizations of related molecules are performed in each basis set. In this method, the best results are calculated by using B3LYP/6-31++G(d,p) level in vacuum. Calculated hardness

values of related molecules are given in Table 5 at B3LYP/6-31++G(d,p) level.

Experimental and calculated results are used to plot the distribution graph. It is represented in Fig. 2 and it is seen that correlation coefficient ( $R^2$ ) values is 0.5907. As for the other results in B3LYP method, correlation coefficient is calculated as lower than 0.5907. Therefore, performance of B3LYP in calculations of chemical hardness is under the expectations. Calculated results in 6-311G, LANL2DZ, LANL2MB SDD and SDDALL basis sets are given in Supp. Table S4 – S8, respectively.



**Fig. 2.** Distribution graphs between experimental and calculated values at B3LYP/6-31++G(d,p) levels in vacuum.

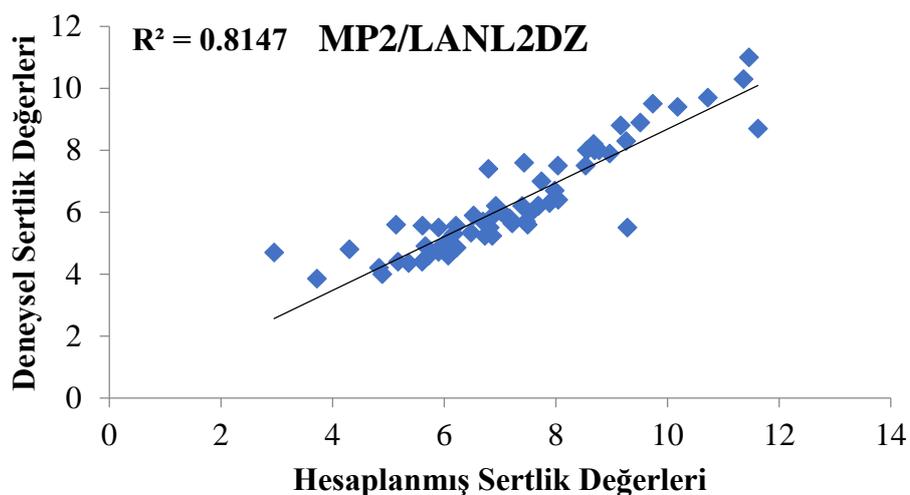
**Table 6.** Calculated chemical hardness values of mentioned molecules at MP2/LANL2DZ level in gas phase

Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$	Molecule	$\eta$
SF <sub>6</sub>	6.792	BBr <sub>3</sub>	6.219	C <sub>5</sub> H <sub>5</sub> N	6.072	cyclohexene	9.281
BF <sub>3</sub>	10.725	PBr <sub>3</sub>	4.832	butadiene	5.664	DMF	7.173
SO <sub>3</sub>	5.900	S <sub>2</sub>	3.719	H <sub>2</sub> S	7.678	C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub>	5.602
Cl <sub>2</sub>	5.721	C <sub>6</sub> H <sub>5</sub> NO <sub>2</sub>	5.174	C <sub>2</sub> H <sub>2</sub>	7.743	CH <sub>3</sub> CH=C(CH <sub>3</sub> ) <sub>2</sub>	6.817
H <sub>2</sub>	11.620	PCl <sub>3</sub>	2.956	HCONH <sub>2</sub>	7.689	CH <sub>3</sub> F	10.183
SO <sub>2</sub>	5.136	N <sub>2</sub> O	7.433	styrene	5.360	H <sub>2</sub> O	9.738
N <sub>2</sub>	9.510	acrylonitrile	6.210	CH <sub>3</sub> COCH <sub>3</sub>	7.493	(CH <sub>3</sub> ) <sub>3</sub> As	6.695
Br <sub>2</sub>	4.893	CS <sub>2</sub>	5.610	PH <sub>3</sub>	7.561	(CH <sub>3</sub> ) <sub>3</sub> P	7.098
O <sub>2</sub>	6.526	CO <sub>2</sub>	9.162	C <sub>6</sub> H <sub>6</sub>	6.168	(CH <sub>3</sub> ) <sub>2</sub> S	7.030
CO	8.965	HF	11.461	toluene	6.013	NH <sub>3</sub>	8.678
BCl <sub>3</sub>	7.216	HCl	8.692	propylene	6.880	CH <sub>4</sub>	11.363
CS	6.727	CH <sub>3</sub> CN	8.535	C <sub>6</sub> H <sub>5</sub> OH	5.895	C(CH <sub>3</sub> ) <sub>4</sub>	9.256
HNO <sub>3</sub>	6.862	CH <sub>2</sub> O	7.397	C <sub>6</sub> H <sub>5</sub> SH	6.071	(CH <sub>3</sub> ) <sub>2</sub> O	8.774
CH <sub>3</sub> NO <sub>2</sub>	6.480	HCO <sub>2</sub> CH <sub>3</sub>	8.042	CH <sub>3</sub> Cl	8.039	(CH <sub>3</sub> ) <sub>3</sub> N	7.887
PF <sub>3</sub>	7.982	CH <sub>3</sub> CHO	7.468	p-xylene	4.302	-	-
HCN	8.557	C <sub>2</sub> H <sub>4</sub>	6.922	1,2,5-trimethylbenzene	5.901	-	-

### 3.3. Chemical Hardness in MP2 Method

The optimizations of related molecules are done in each basis set. In this method, the best results are calculated by using MP2/LANL2DZ level in gas phase. Calculated hardness values of related molecules are given in Table 6 for MP2/LANL2DZ level.

A graph is plotted by using experimental and calculated chemical hardness values and it is represented in Fig. 3. It is seen that correlation coefficient ( $R^2$ ) values is 0.8147. Calculated chemical hardness values in 6-31++G(d,p), 6-311G, LANL2MB, SDD and SDDALL basis sets are given in Supp. Table S9 – S13, respectively.



**Fig. 3.** Distribution graphs between experimental and calculated values at MP2/LANL2DZ levels in gas phase.

**Table 7.** Calculated scale factor ( $\lambda_{Average}$ ) and correlation coefficient ( $R^2$ ) values for each level

Basis Set	HF		B3LYP		MP2	
	$\lambda_{Average}$	$R^2$	$\lambda_{Average}$	$R^2$	$\lambda_{Average}$	$R^2$
6-31++G(d,p)	0.9825	0.5707	2.0241	0.5907	0.9916	0.5863
6-311G	0.8598	0.8046	1.9667	0.4986	0.9459	0.7200
LANL2DZ	0.8375	0.8999	1.9526	0.3803	0.8754	0.8147
LANL2MB	0.7404	0.5388	1.8528	0.5630	0.7606	0.5630
SDD	0.8313	0.8970	1.9923	0.2719	0.8646	0.6057
SDDALL	0.8426	0.8178	1.9534	0.3611	0.8764	0.7708

### 3.4. Scale Factor for Chemical Hardness

Scale factors are mainly used in vibrational spectroscopy to determination of anharmonic frequencies. In this study, scale factor is calculated for determination of accuracy and harmony. Scale factor ( $\lambda_{Hardness}$ ) is calculated for each level by using Eq. (7) and (8).

$$\lambda_{Hardness} = \frac{\eta_{experimental}}{\eta_{calculated}} \quad (7)$$

$$\lambda_{Average} = \frac{\sum_0^N \lambda_{Hardness}}{N} \quad (8)$$

It is expected that scale factor is equal to one. If scale factor is equal to one, it is expected that accuracy and harmony is high. Calculated scale factor and  $R^2$  values are given in Table 7.

To determine the best method in calculation of chemical hardness, both scale factor and correlation coefficient must be taken into consideration. Scale

factor and correlation coefficient must be equal or close to “1”. Therefore, results in HF method are better than those of B3LYP and MP2. Additionally, HF method is better in calculation of molecular orbital energies than those of B3LYP and MP2, since chemical hardness is calculated by using HOMO and LUMO energies.

### 4. Conclusion

62 molecules are optimized at three different methods and six different basis set in gas phase. Chemical hardnesses are calculated in each level by taking into considerations Koopmans theorem. Distribution graphs are plotted in each level and correlation coefficient are calculated for each graph. In addition to these results, average scale factor for chemical hardness are calculated by using experimental and calculated hardness values. As a results, HF method is better in calculation of chemical hardness and molecular orbital energy than B3LYP and MP2 methods.

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### References

- [1] P. Jankowski, W. Wiczorek, P. Johansson, SEI-forming electrolyte additives for lithium-ion batteries: development and benchmarking of computational approaches, *J Mol Model* 23:6 (2017) 3-9.
- [2] Juan Frau, Noemi Hernández-Haro, Daniel Glossman-Mitnik, Computational prediction of the pKas of small peptides through Conceptual DFT descriptors, *Chemical Physics Letters* 671 (2017) 138–141.
- [3] Meryem Evecen, Hasan Tanak, DFT quantum chemical studies of (E)-4-Bromo-N-(2-chlorobenzylidene)-aniline, *Appl. Phys. A*, 123: 91 (2017) 1-6.
- [4] Samaneh Bagheri Novir, Seyed Majid Hashemianzadeh, Quantum chemical investigation of structural and electronic properties of trans- and cis-structures of some azo dyes for dye-sensitized solar cells, *Computational and Theoretical Chemistry* 1102 (2017) 87–97.
- [5] Sadegh Kaviani, Mohammad Izadyar, Mohammad Reza Housaindokht Kaviani, A DFT study on the complex formation between desferrithiocin and metal ions (Mg<sup>2+</sup>, Al<sup>3+</sup>, Ca<sup>2+</sup>, Mn<sup>2+</sup>, Fe<sup>3+</sup>, Co<sup>2+</sup>, Ni<sup>2+</sup>, Cu<sup>2+</sup>, Zn<sup>2+</sup>), *Computational Biology and Chemistry* 67 (2017) 114–121.
- [6] Mehmet Ferdi Fellah, A DFT study of hydrogen adsorption on Be, Mg and Ca frameworks in erionite zeolite, *Applied Surface Science* 394 (2017) 9–15.
- [7] H. Moustafa, Mohamed E. Elshakre, Salwa Elramly, Electronic structure and nonlinear optical properties (NLO) of 2,4-di-aryl-1,5-benzothiazepine derivatives using DFT approach, *Journal of Molecular Structure* 1136 (2017) 25-36.
- [8] Subhajit Mukherjee, Venkata P. Reddy B., Ishani Mitra, Sankar Ch. Moi, In vitro kinetic based adduct formation mechanism of a cytotoxic Pt(II) complex with sulfur containing bio-relevant molecules and a theoretical approach, *Polyhedron* 124 (2017) 251–261.
- [9] Jonas Šarlauskas, Jelena Tamulienė, Narimantas Čėnas, Aziridinyl-substituted benzo-1,4-quinones: A preliminary investigation on the theoretical and experimental studies of their structure and spectroscopic properties, *Spectrochimica Acta Part A: Molecular and Biomolecular Spectroscopy* 178 (2017) 136–141.
- [10] R. G. Pearson, Hard and Soft Acids and Bases, *J. Am. Chem. Soc.* 85 (1963) 3533.
- [11] John J Gilman, Chemical and physical “hardness”, *Mat. Res. Innovat.* 1 (1997) 71.
- [12] Robert G Parr, Ralph G Pearson, Absolute hardness: companion parameter to absolute electronegativity. *J. Am. Chem. Soc.* 105 (1983) 7512.
- [13] Mihai V. Putz, Nino Russo, Emilia Sicilia, On the Applicability of the HSAB Principle through the Use of Improved Computational Schemes for Chemical Hardness Evaluation, *Journal of Computational Chemistry* 25 (2004) 994-1003.
- [14] K. Sayın, S. E. Kariper, T. A. Sayın, D. Karakaş, Theoretical spectroscopic study of seven zinc (II) complex with macrocyclic Schiff-base ligand. *Spectrochimica Acta Part A: Molecular and Biomolecular Spectroscopy* 133 (2014) 348-356.
- [15] W. Loued, J. Wéry, A. Dorlando, K. Alimi, A combined study based on experimental analyses and theoretical calculations on properties of poly (lactic acid) under annealing treatment, *Journal of Molecular Structure* 1081 (2015) 486–493
- [16] Huicen Zhu, Weimin Guo, Zhemin Shen, Qingli Tang, Wenchao Ji, Lijuan Jia, QSAR models for degradation of organic pollutants in ozonation process under acidic condition, *Chemosphere* 119 (2015) 65–71.
- [17] Walaa H. Mahmoud, Nessma F. Mahmoud, Gehad G. Mohamed, Ashraf A. El-Bindary, Adel Z. El-Sonbati, Supramolecular structural, thermal properties and biological activity of 3-(2-methoxyphenoxy)propane-1,2-diol metal complexes, *Journal of Molecular Structure* 1086 (2015) 266–275.

- [18] A.Z. El-Sonbati, M.A. Diab, A.A. El-Bindary, M.M. Ghoneim, M.T. Mohesien, M.K. Abd El-Kader, Polymeric complexes — LXI. Supramolecular structure, thermal properties, SS-DNA binding activity and antimicrobial activities of polymeric complexes of rhodanine hydrazone compounds, *Journal of Molecular Liquids* 215 (2016) 711–739.
- [19] A.Z. El-Sonbati, M. A. Diab, A. A. El-Bindary, M. A. El-Mogazy, Polymer complexes. LXVI, thermal, spectroscopic studies and supramolecular structure of N-[ $\beta$ -(ethylamino)] acrylamide polymer complexes, *Journal of Molecular Liquids*, 219 (2016) 1044-1057.
- [20] A. A. El-Bindary, M. M. Ghoneim, M. A. Diab, A. Z. El-Sonbati, L. S. Serag, Thermodynamic studies of N-allylrhodanine derivatives and their metal complexes, *Journal of Molecular Liquids* 223 (2016) 448-461.
- [21] M. A. Diab, A. Z. El-Sonbati, A. A. El-Bindary, S. M. Morgan, M. A. El-Kader, Geometrical structures, molecular docking, spectroscopic characterization of mixed ligand and Schiff base metal complexes, *Journal of Molecular Liquids*, 218 (2016) 571-585.
- [22] R. D. Dennington II, T.A. Keith, J.M. Millam, GaussView 5.0, Wallingford CT, 2009.
- [23] Gaussian 09, Revision D.01 Linux (Gaussian Inc., Wallingford, CT, USA) 2009.
- [24] Gaussian 09, Revision A.02 Windows (Gaussian Inc., Wallingford, CT, USA) 2009.
- [25] Ralph G Pearson, Absolute electronegativity and Hardness: Application to Inorganic Chemistry, *Inorganic Chemistry* 27 (1988) 734-740.