Roughness Coefficient of a Highly Calcinated Penstock

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ABSTRACT

When highly calcinated water is transferred through the penstock of a hydropower plant it leaves a residue on the pipe surface. Accumulated residue over time causes a change in the roughness of the pipe surface thus leads to friction losses in the system. The effect is a change in head and discharge relation for the turbines. A multimethodology is proposed for determining the apparent surface roughness value (ϵ) by means of friction factor f and measuring arithmetic mean deviation of the roughness profile (Ra), root mean square roughness (Rq) and peak and valley roughness (Rz). It is found that a surface roughness value (ϵ) of 0.3mm can be used for calcinated surfaces which is much higher than steel surfaces but smaller than a concrete surface.

Keywords: Friction factor, surface roughness, calcination.

1. INTRODUCTION

Energy output of hydropower plants (HPP) depends on the net head and flow rate supplied to the turbines. Water is conveyed from a reservoir or a head pond to the power house by means of water conduits called penstocks. Systems are designed such that the energy output is maximized while minimizing the cost [1]. Part of the available energy is lost due to pipe friction and other local losses. Available energy conveyed to the turbines, hence the amount of energy produced, depends on the amount left after these losses.

When highly calcinated water is transferred through the penstock of a hydropower plant it leaves a residue on the pipe surface. Such residues accumulate over time forming a thick layer on the surfaces in contact with water. There are two important aspects of this calcination, one is the change in the surface roughness coefficient the other is the change in the actual flow diameter. While the effect of the first one is not known a priori, the second one causes a decrease in flow diameter and an increase in the average velocity, increasing losses in the penstock system.

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Recently, a rehabilitation project for and old powerhouse (KEPEZ 1 HPP), located in the province of Antalya, was started. The Hydropower plant is equipped with three Francis type turbines with an installed capacity of 26.4 MW. It is the sixth largest power house in the region. The power house had been in operation for more than 30 years. The net head of the turbines is 162 m with a discharge of 6.1 m³/s. The aim of the rehabilitation project is to increase efficiency and output of the old turbines in the HPP by replacing them with new ones while renewing all auxiliary systems up to state-of-the-art requirements.

The hydro power plant consists of a head pond and an intake structure and diverts the flow through a pressurized concrete pipe followed by a surge tank and a long steel pipe. A problem concerning quality of water exists in the region, causing heavy calcination of pipes. Operating records of the power house suggests a calcination period that is as short as six months and a calcination thicknesses of up to 30 mm were observed in the penstock. Continuous cleaning of the water conduit is very costly and interrupts energy production because it requires emptying the penstock and hard scrubbing of the full conduit system. Thus, a new turbine to be installed on the old calcinated pipeline system will operate at different head than its design head and at different discharge conditions than its initial design. Therefore, the new turbine design should account for calcination and change in the friction losses in the system for varying flowrates.

Initial design net head and discharge through the turbines are determined using the design drawings. They are calculated from the well-established Darcy-Weisbach relation. When designing a new system, the equivalent roughness values of steel (ε =0.02 - 0.05mm) and concrete pipes (ε =0.5mm) are easily obtained from various engineering tables and the net head available to the turbine can easily be calculated [2]. Roughness coefficients of selected residue materials are also available in the literature [3]. But no information is available in literature for the apparent surface roughness value (ε) of a highly calculated pipe surface. For this reason, a multimethodology is proposed that includes:

- 1.) A one-dimensional numerical model of the existing system which is built to calculate the steady state head and discharge relation for varying apparent surface roughness values (ϵ)
- 2.) Determination of combined friction coefficient based on site measurements of flow rate and turbine inlet pressure and head water level variations
- 3.) Determination of apparent surface roughness using laboratory measurements of surface profile and waviness of a sample calcinated block obtained from the site.

The numerical model is used to observe the variation in the combined friction coefficient of the system by changing the surface roughness values (ϵ) of individual pipes. Then, site measurements are used to calculate the friction coefficient of the system. This coefficient is compared with the surface roughness values (ϵ) of the numerical model to estimate how a calcinated pipe surface behaves for the heavily calcinated penstock so that the turbine operating range can be determined. Lastly, during the dismantling of the old turbines, the penstock is emptied and became accessible to receive samples from the penstock surface. Surface roughness values (ϵ), and measured roughness profiles that point to the same result.

2. NUMERICAL MODEL

A convenient form of the Energy Equation for a steady, incompressible flow with uniformly distributed velocity profiles can be written between the two sections in a straight pipe as:

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + Z_2 + H_L \tag{1}$$

where, P is the pressure, V is the average velocity, Z is the elevation of the pipe axis, ρ is the density of the fluid, g is the gravitational acceleration, and H_L is the frictional head loss between these two sections, given that there are no minor losses. In 1845, Julius Weisbach [4] proposed an equation that predicts the losses due to fluid friction on the pipe wall as;

$$H_L = f \frac{L}{D} \frac{V^2}{2g} \tag{2}$$

$$f = func\left(\frac{\varepsilon}{D}, Re\right) \tag{3}$$

where L is the pipe length, D is the pipe diameter, f is a friction factor, Re is the Reynolds number and is defined by Re=VD/v and v is the kinematic viscosity of the fluid. This equation set the standard for all following engineering text books [2]. With Darcy's estimates of the friction factor [5] and additional work by Colebrook and White [6] on non-uniform roughness, estimates of the friction factor f can be made as functions of Reynold number (Re) and relative roughness (ϵ /D). Later Moody [7] published the famous Moody's chart and Swamee and Jain [8] expanded the form to the explicit equations for pipe diameter, head loss and the discharge through a pipe, based on the Colebrook-White equation [6].

For long penstock systems, friction in each pipe segment can be calculated separately. Pipe diameters, lengths and corresponding Reynolds numbers are different in each pipe segment. Minor losses due to bends, expansions, contractions etc. can be calculated separately as a function of discharge and all of these losses can be added to obtain the system loss. In order to generalize the equation of losses, the Darcy-Weisbach equation can be written such that the head loss due to friction becomes a function of discharge:

$$H_L = (8fL/g\pi^2 D^5)Q^2 = k_{Friction}Q^2$$
(4)

Minor (local) losses such as those due to bends, expansions contractions etc. can also be formulated as a function of discharge;

$$H_{Local} = k_{Local}Q^2 \tag{5}$$

Then the total loss in the system can be calculated by adding all friction and local losses.

$$H_{LossSystem} = \sum k_{Local}Q^2 + \sum k_{Friction}Q^2 = k_{Local}Q^2 + k_{Friction}Q^2 = kQ^2$$
(6)

Where k is a combined friction coefficient for the entire system. A numerical onedimensional model is designed for the existing system as shown in Figure 1, where the head pond is modeled as reservoir 1 (R1). Water is conveyed through a concrete pipe (E1) and a series of steel pipes (P1-P9, B1, S1) to turbine and then to the Tailrace Channel (T1). The model is set up with one turbine in operation in order to compare the results with the measurements.



Figure 1 - Layout of the Kepez 1 HPP

Basic parameters including minor loss coefficients of the pipe system are given in Table 1.

Label	Material	Diameter (cm)	Minor Loss Coefficient	Length (m)
P2	Steel	240	0.040	62.16
P4	Steel	240	0.000	164.60
P6	Steel	210	0.110	103.87
P3	Steel	240	0.006	44.33
P5	Steel	240	0.000	100.50
P1	Steel	240	0.062	23.01
T1	Concrete	500	0.000	5.00
P7	Steel	210	0.019	206.66
P8	Steel	210	0.060	62.88
E1	Concrete	250	0.346	589.00
B1	Steel	130	0.052	1.00
S1	Steel	90	0.169	3.60
P9	Steel	210	0.096	19.97

Table 1 - System parameters

The head pond and tailrace levels are set to constant values for each simulation and the corresponding friction and minor losses are calculated. The discharge passing through the system is controlled by the guide vanes of the Francis turbine. The model is set such that the simulated discharge range covers the operation of the installed Francis turbine. A head discharge curve is used for each guide vane opening for the Francis Turbine. A total of 12 simulations are performed for three discharge sets (Table 2) and four roughness values (Table 3). Simulations are iterated until the discharge values are seen to converge with the preset values.

	$Q_1 \ (m^{3/s})$	Q ₂ (m ³ /s)	Q ₃ (m ³ /s)
Case	3.0344	5.3758	6.1471

Table 2 - Simulated flowrates

Table 3 - Apparen	t surface	roughness	values
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	$\epsilon_1 (mm)$	$\epsilon_2 (mm)$	$\epsilon_3 (mm)$	$\epsilon_4 (mm)$
Case	0.5	0.3	0.05	0.02

There are various engineering tables that present the apparent roughness values (ε) of different materials [2]. The values of interest in this study are for smooth and rough steel pipes (0.02 mm and 0.05 mm) and concrete (0.3~3 mm). A representative value of 0.5 mm is selected for smooth concrete. A comparative study is performed to observe how the roughness of calcinated surface changes with respect to steel and concrete. So, simulated values for the calcinated pipes included these values in addition to an intermediate value of 0.3mm. Since calcination occurs both in concrete and steel surfaces, roughness values are kept constant for all simulations throughout the system. During measurements, sensor taps were drilled on the steel pipe to install acoustic flow meters. The drilled hole and calcinated layer are shown in Figure 2. The thickness of the calcinated layers can be seen through these holes and found to vary between 11 mm and 15 mm. Although the effect of change in the flow diameter due to this accumulation is small, it is considered in all of the simulations and all pipe diameters presented in Table 1 is reduced by 30mm.



Figure 2 - Calcination in the pipe seen from a sensor tap

Friction and minor losses are calculated for each pipe segment and tabulated for each simulation. These values are summed up to calculate the total loss in each simulation. A sample computation for the flow rate of 6.147 m³/s, head pond elevation of 278.2 m, tailwater elevation of 110.04 m and an apparent roughness values (ϵ) of 0.3 mm is given in Table 4.

Label	Material	Velocity (m/s)	Headloss (m)	Headloss (Friction) (m)	Headloss (Minor) (m)
P2	Steel	1.39	0.038	0.034	0.004
P4	Steel	1.39	0.090	0.090	0.000
P6	Steel	1.77	0.123	0.105	0.018
P3	Steel	1.39	0.025	0.024	0.001
P5	Steel	1.39	0.055	0.055	0.000
P1	Steel	1.39	0.019	0.013	0.006
T1	Concrete	0.31	0.000	0.000	0.000
P7	Steel	1.77	0.213	0.210	0.003
P8	Steel	1.77	0.073	0.064	0.010
E1	Concrete	1.28	0.289	0.260	0.029
B1	Steel	4.85	0.076	0.014	0.063
S1	Steel	9.77	1.122	0.301	0.821
P9	Steel	1.77	0.036	0.020	0.015
Sum			2.157	1.188	0.969

Table 4 - Solution values for a case

In order to calculate the combined system friction constant k for each apparent roughness value (ϵ), total head loss in each simulation is calculated and tabulated against flowrate and square of the flowrate. Results of all simulations are summarized in Table 5.

	$\epsilon_1 (mm)$	$\epsilon_2 (mm)$	ε ₃ (mm)	ε ₄ (mm)
Q (m ³ /s)	0.5	0.3	0.05	0.02
6.1471	2.275	2.157	1.898	1.835
5.3758	1.742	1.653	1.459	1.413
3.0344	0.559	0.532	0.477	0.465

Table 5 - Head loss values in meters for 12 cases

As the head loss changes linearly with Q^2 value according to Darcy-Weisbach equation, results are plotted and a line is fitted to obtain friction head loss slope coefficient as shown in Figure 3. Coefficient values of 0.0488, 0.0504, 0.0572 and 0.0603 are obtained for roughness values of 0.02 mm, 0.05mm, 0.3mm and 0.5mm respectively.



Figure 3 - Calculation of friction head loss slope for different roughness coefficients

3. CALCULATION OF FRICTION COEFFICIENT BASED ON SITE MEASUREMENT

Kepez HPP has been in operation for more than 30 years. During this period significant improvement in turbine design was achieved with the help of computational fluid dynamics (CFD)[9]. Efficiency and cavitation characteristics of runner is investigated and characteristics over operating region of the old Kepez turbine is determined by means of CFD [10][12]. Design of the new turbine is significantly improved to better characterize the current operating regime [13]. The new turbine efficiency is obtained by means of both CFD [13] and model tests [14] performed at ETU HYDRO Turbine Design and Test Center. Although these works give significant insight on the turbine performance, project requirements dictate comparison of efficiencies with in-situ site measurements. For this reason, an efficiency measurement setup is installed at site as part of the project[15]. Using this setup, hydraulic efficiency of the turbine is measured at different operating points [15]. Available hydraulic energy to the turbine and power output of the generator are required to calculate efficiency of the turbine generator set. To obtain the available hydraulic energy, the turbine net head and flowrate must be known. Pressure measurement taps are installed for measuring the inlet and outlet pressures before and after the turbine. An ultrasonic flow measurement system is installed for measuring the flow rate. For efficiency calculations, the mechanical power out of the turbine must also be determined. Power output of the generator can be measured through the current and voltage transformers. Energy analyzers were installed at outputs of generator current and voltage transformers to obtain the electrical output of the generator. With known generator efficiency curve and output of the generator, shaft power can be

calculated. So, hydraulic efficiency of the turbine can be calculated from available hydraulic energy and mechanical power. Using this methodology efficiency of the old turbine is measured [15]. Via these pressure taps and ultrasonic flow meters, the pressure at the turbine inlet as well as the discharge passing through the system is readily available and given in Table 6.

Q [m³/s]	P (kPa)	$\Delta H_{HPL}\left(m ight)$
6.1471	1619.67	0.65
6.0696	1619.90	0.77
5.7974	1622.51	0.77
5.6236	1626.25	0.20
5.5628	1626.44	0.69
5.3758	1627.50	0.77
5.1572	1629.19	0.12
4.8804	1630.61	0.00
4.2254	1636.40	0.65
3.0344	1642.69	0.74

Table 6 - Flowrate, Pressure and Change in Head pond levels

Q [m ³ /s]	V ² /2g (m)	P/γ (m)	H _{inlet} (m)	H_{inlet} - ΔH_{HPL} (m)
6.1471	1.094	165.296	166.390	165.740
6.0696	1.067	165.319	166.386	165.616
5.7974	0.973	165.586	166.559	165.789
5.6236	0.916	165.967	166.883	166.683
5.5628	0.896	165.986	166.883	166.193
5.3758	0.837	166.095	166.932	166.162
5.1572	0.770	166.267	167.037	166.917
4.8804	0.690	166.412	167.101	167.101
4.2254	0.517	167.003	167.520	166.870
3.0344	0.267	167.645	167.911	167.171

This data set is used to calculate the head discharge relation of the system and the friction slope coefficient of the conduit. An additional data, head pond level, is required to calculate

a system curve. Since no digital measurement system for the head pond levels was available, hourly operating records of head pond level change with respect to crest elevation using a rod installed at the head pond is used. The change in the reservoir level is measured and tabulated below together with flowrate and pressure (Table 6).

System losses are calculated from the slope of the curve $H_{inlet} -\Delta H_{HPL}$ vs Q^2 . The corresponding values are obtained by adding the velocity head, pressure head and subtracting the variation in the head pond level as given in Table 7.

Results are plotted for total head vs square of flowrate and a line is fitted to obtain friction slope coefficient from measurements as shown in Figure 4. As the head loss changes linearly with Q^2 value according to Darcy-Weisbach equation, a line is fitted and slope is calculated as -0.0562 (Figure 4).



Figure 4 - Calculation of friction slope from measurements

The curve represents the change in the total head with increasing discharge, thus a negative value. Absolute value of this slope is 0.0562 which is compared with the various roughness values calculated and plotted via the numerical model, the surface roughness value (ϵ), 0.3mm shows a similar a slope of 0.0572.

4. LABORATORY MEASUREMENTS OF SURFACE ROUGHNESS

Once the design and manufacturing of the new turbine was completed, dismantling of the old turbine system was started. Energy production interrupted, the penstock was emptied. The old turbine system as well as the inlet valve was removed. At that stage, access to the penstock was available. A sample block of calcinated residue is carefully taken for testing purposes

without disturbing the surface, size and thickness of the calcinated sample taken from the penstock are shown in Figure 5.



Figure 5 - Calcinated sample from penstock

Sides of the block are grinded and the block is attached to a clamp. A Zeiss Surfcom 130 A surface profiler is used to measure the surface profile of the block.



Figure 5 - Measurement of Surface profile

A sampling section is measured with a length of 38 mm. A probe with a tip radius of 2 μ m, a speed of 0.6mm/s is used. The primary (total) profile, which is the surface height measured throughout the sampling section, is measured and shown in Figure 6. The waviness component is obtained from an electronic low-pass filtering of the primary profile with a cut off wavelength value of 8.0 mm (Figure 6). Finally, roughness profile is obtained (Figure 7). By doing so, the measured profile is filtered for large scale waviness effects and a representative data set for the surface characteristics that effect friction is obtained. This data set is necessary to calculate measurable surface roughness characteristics Ra, Rq and Rz.



Figure 6 - Total profile and waviness



Figure 7 - Roughness profile

Once the roughness profile is obtained, standard surface roughness parameters (Ra, Rq, Rz) are calculated using equations 7, 8 and 9. The first parameter Ra represents the arithmetical

mean of the absolute values of the profile deviations from the mean line of the roughness and is given by:

$$Ra = \frac{1}{L} \int_0^L |z(x)| dx \tag{7}$$

whereas the root mean square roughness Rq is given by:

$$Rq = \sqrt{\frac{1}{L} \int_0^L z^2(x) dx}$$
(8)

The last parameter Rz is called ten-point height roughness which gives the average absolute value of five highest peaks and five lowest valleys over the evaluation length.

$$Rz = \sum_{i=1}^{5} \frac{z_{max}(i) - z_{min}(i)}{5}$$
(9)

These three measured parameters are the parameters that are commonly used to describe the surface finish of materials. The calculated values for each of these parameters are given in Table 8.

Ra (µm)	Rq (µm)	Rz (µm)
47.20	59.46	287.45

 Table 8 - Surface roughness parameters

The surface roughness value (ϵ) is not directly measurable. The friction factor given by Moody's chart derived from the friction coefficient of various fluid experiments conducted originally by Nikuradse by the evaluation of loss terms and equivalent sand roughness. There are numerous studies that relate the directly measurable quantities Ra, Rq and Rz to the surface roughness values (ϵ) used to calculate the friction factor f in Darcy-Weisbach equation.

Computational models that utilize surface roughness values (ϵ) for pipes, pumps and turbines simulate roughness data acquired from experiments that include many different roughness characterizations. On the other hand, manufacturers use directly measurable quantities Ra, Rq and Rz to represent the surface texture of their products. Equations available in literature [16-31] that try to relate these parameters vary greatly and there is no consensus on a single relation on these parameters. Equations proposed by [19-24] mostly use sand grains, emery papers or machined surfaces to produce the empirical equations using Ra, while suggested equations for groove height or liquid crystal surfaces, Rq [26-27] is mostly used for surfaces with sprayed particles as an alternative.

Naturally occurring calcination deposits were not studied in any of these works; however, for a wide range of surfaces, a general trend is to use Rz, peak to valley roughness height, equal to surface roughness value (ϵ) (Rz $\approx \epsilon$) [16][17]. This corresponds to 287.45 µm for the

calcinated surface sample. Regardless, a table is prepared from available literature to calculate and check surface roughness values (ϵ) using all three parameters Ra, Rq, Rz. Values of surface roughness (ϵ) are calculated using these three parameters as given in Table 9 [16-31].

These values are averaged to find a single representative number for ε which is found to be 281.70 µm. The calculated average surface roughness (ε) value of 281.70 µm is also found to be very close to simulated 300 µm roughness value which corresponds to combined friction coefficient of 0.0572 for the system.

Reference	Equation proposed	ϵ (calculated)
[18]	ε=Rz/5	57.49
[18]	ε=Rz/2.56	112.29
[19]	ε=2Ra	94.40
[19]	ε=7Ra	330.41
[20]	ε=6Ra	283.21
[21]	ε=2.2Ra ^{0.88}	65.39
[22]	ε=8.9Ra	420.09
[23]	ε=2Ra	94.40
[24]	ε=16Ra	755.22
[16]	ε=Rz	287.45
[17]	ε=Rz	287.45
[25]	ε=4Ra	188.80
[26]	ε=2.1Rq	124.87
[27]	ε=4.8Rq	285.41
[28]	ε=10Ra	472.01
[29]	ε=8.9Ra	420.09
[30]	ε=1.9Rz	546.16
[31]	ε=5.2Ra	245.45
	Average	281.70

Table 9 - Calculated values of surface roughness (ε) in μm

5. CONCLUSIONS

For turbine rehabilitation, roughness of old penstocks must be known in order to calculate head-discharge characteristics of the system. The case of interest is the roughness of highly calcinated pipeline system for which no prior information is available in the literature. A multimethodology is proposed to obtain apparent surface roughness coefficient (ϵ) of

calcinated pipes. For this reason, a one-dimensional numerical model of the existing system is built to calculate the steady state head and discharge relation by varying apparent surface roughness values. A set of curves are obtained for the system to specify the relation between friction coefficient and apparent surface roughness. Friction coefficient is also calculated based on site measurements of flow rate, head pond level and inlet pressure of turbines. The measured friction slope is compared with the slopes obtained from the numerical model. The closest match points to a roughness value of 0.3 mm for calcinated surfaces. Lastly, a sample calcinated block is obtained from site to measure surface roughness parameters at the laboratory. Measurable surface roughness parameters of arithmetic mean deviation of the roughness profile (Ra), root mean square roughness (Rq) and peak and valley roughness (Rz) are obtained. Empirical equations available in literature that relate these parameters to apparent surface roughness (ε) are used to find an average roughness value of 0.282 mm for the sample. It is determined that, for all practical purposes, a surface roughness value of 0.3 mm can be used for calcinated surfaces which is much higher than steel surfaces but smaller than concrete.

Surface roughness values of both steel and concrete is widely used in both the theoretical studies in literature and practical applications. However, the obtained value for the surface roughness of calcinated pipes based on site measurements, laboratory experiments and the numerical study presented here, is different than the values of both of these materials. This study clearly shows that the surface roughness of the calcinated pipe is 0.3 and the design process for rehabilitation and output of turbines and related equipment is affected drastically, if the change in surface roughness is not considered where calcination is present. Therefore, utilization of the methodology presented here, would provide the hydraulic power equipment designer the information necessary for rehabilitation works.

Symbols

D	Diameter of the pipe segment
f	Darcy - Weisbach friction factor
H_L	Head loss
k	Combined friction coefficient
$\mathbf{k}_{\mathrm{Friction}}$	Friction coefficient caused by friction losses in the pipe
$\mathbf{k}_{\mathrm{Local}}$	Friction coefficient caused by local losses
L	Length of the pipe segment
Р	Pressure
Ra	Arithmetic mean deviation of roughness height
Re	Reynolds number
Rq	Root mean square roughness height
Rz	10 point roughness height (peak and valley roughness height)

- V Average velocity in pipe
- Z Elevation head
- g Gravitational acceleration
- z Height of each measured surface
- ΔH_{HPL} $\,$ Deviation in elevation of the head pond level
- ε Apparent surface roughness
- ρ Density of water

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